

# What is The Ultimate Conductance of Hydrodynamic Electrons?

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Weizmann Institute of Science*



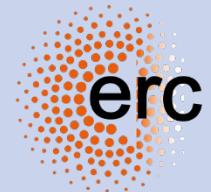
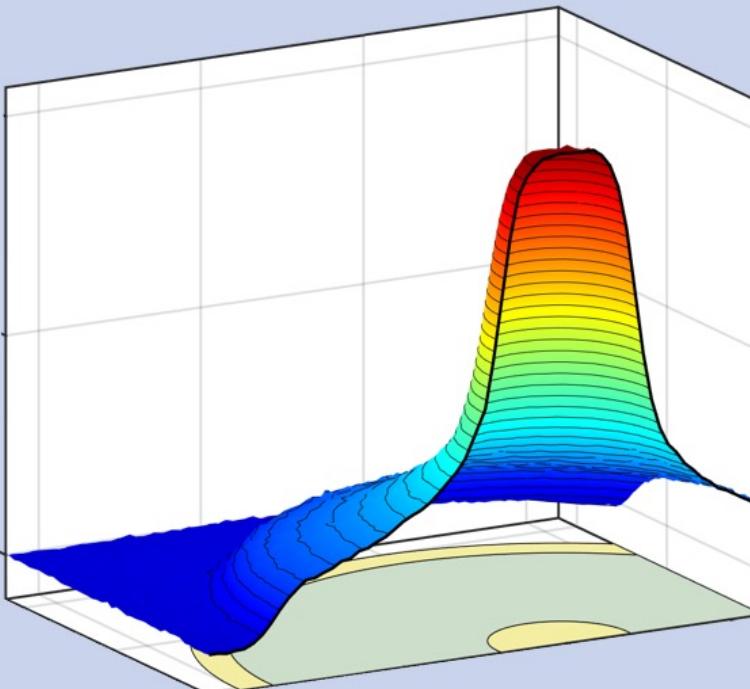
Chandan Kumar



John Birkbeck



Joseph Sulpizio



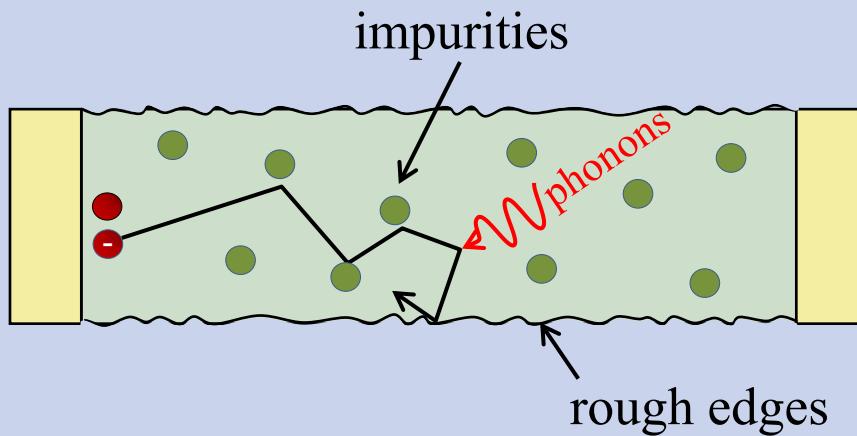
**Experimental collaboration:** Dave Perello, Andre Geim (Manchester)

**Theory collaboration:** Oren Reuven, Ady Stern (Weizmann) Thomas Scaffidi (Toronto)

**hBN crystals:** Takashi Taniguchi, Kenji Watanabe

# Electrical resistance comes from momentum relaxation

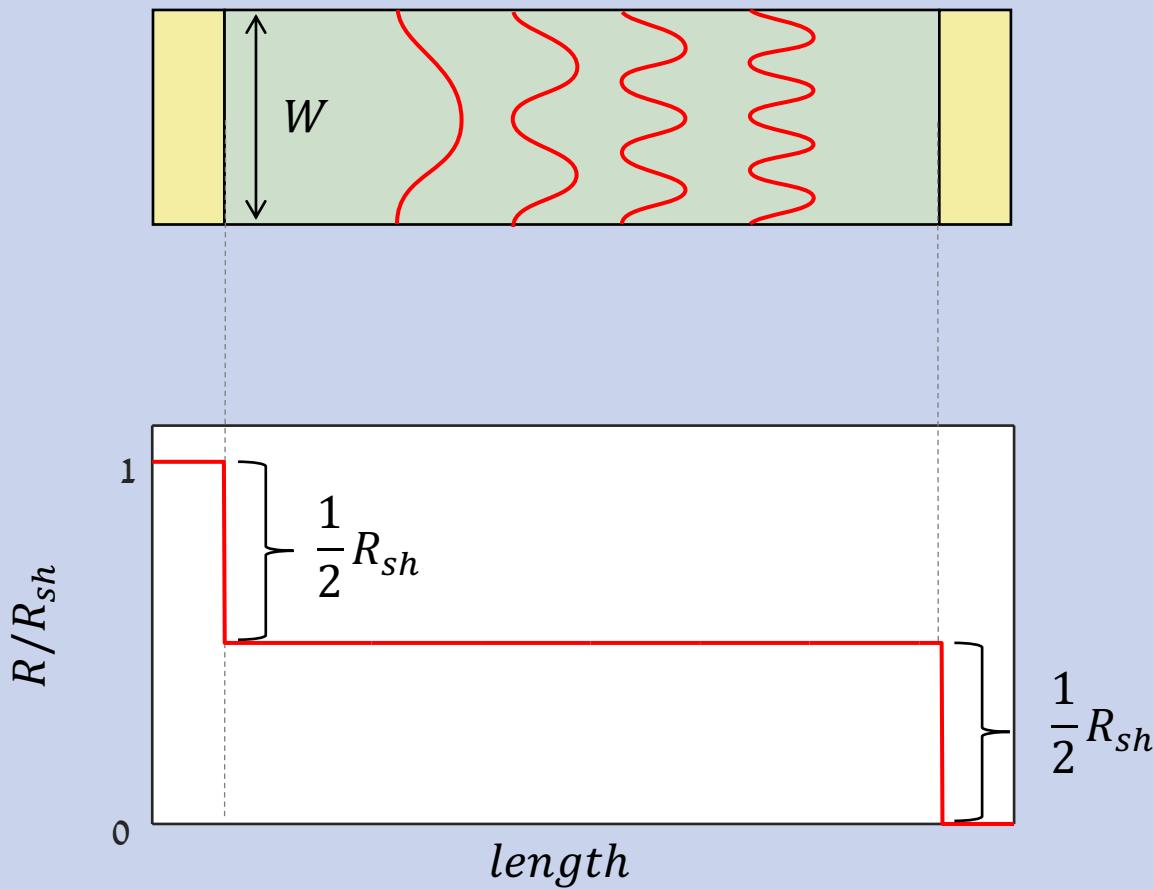
electrical resistance = momentum back-scattering



# Landauer (1957) and Sharvin (1965)

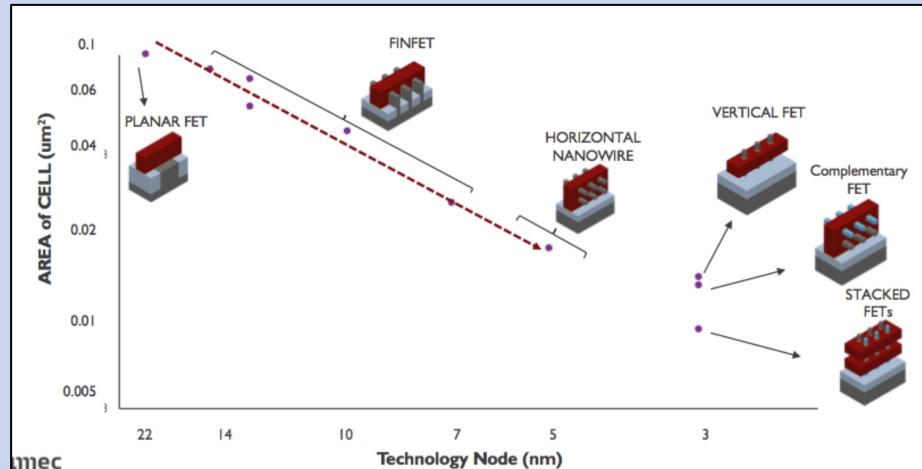
**Landauer:**  $N = W/\lambda_F$  modes       $R_{2probe} = \frac{1}{N} \frac{h}{e^2} \equiv R_{sh}$

**Sharvin:** At the interface with the contacts



# The resistive bottleneck

Moore's law



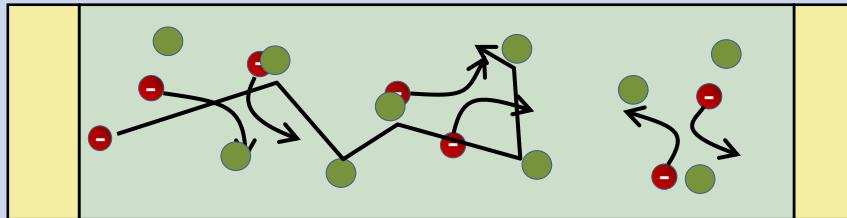
Scaling down continues

The bottleneck is the contact resistances

Ultimate bound - Landauer-Sharvin resistance

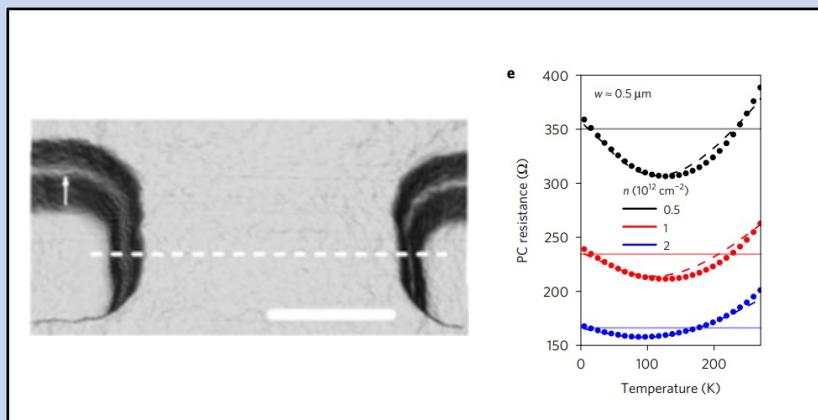
Can this fundamental limit be broken electron hydrodynamics?  
By how much?

# Electron hydrodynamics

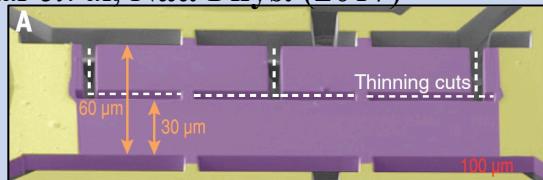


## Hydrodynamics in high mobility wires

De-jong and Molenkamp, PRB (1994)

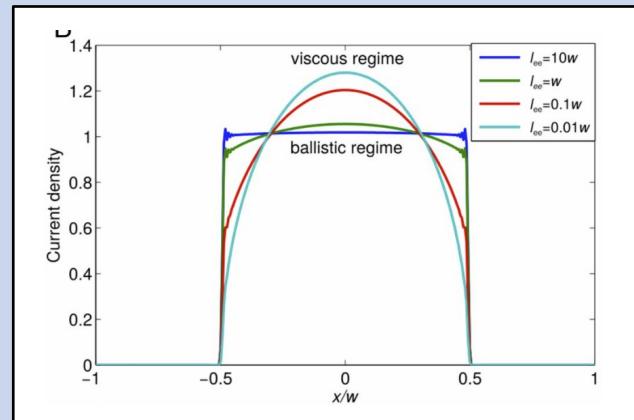


Kumar et. al, Nat. Phys. (2017)



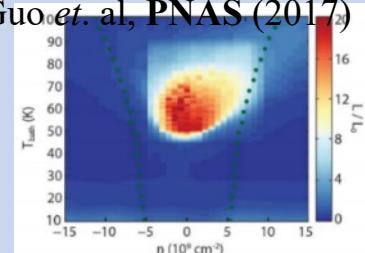
## Negative local resistance

Bandurin et. Al, Science (2016)



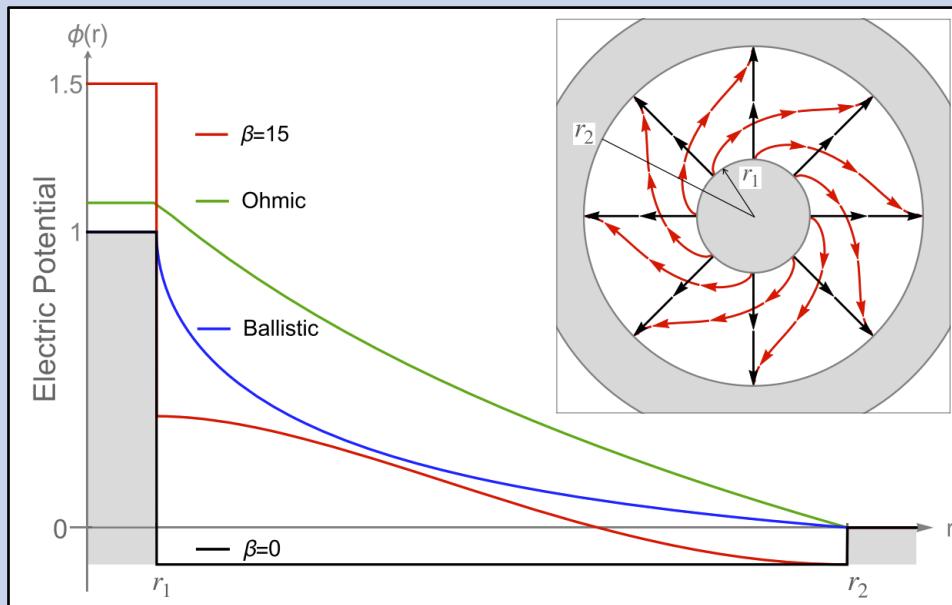
d

Guo et. al, PNAS (2017)



See also: Z.J. Krebs, V.W. Brar et. al, arXiv (2021)

# Freely Flowing Currents and Electric Field Expulsion in Viscous Electronics

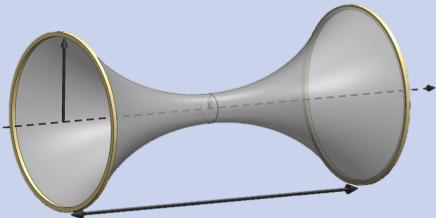


M. Shvait, A. Shytov and G. Falkovich, **PRL** (2019)

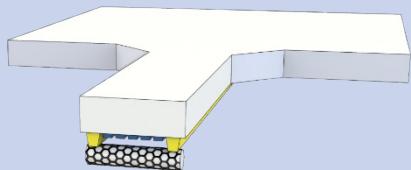
See also:

Q. Hong, M. Davidova, E. Kiselev, L. Levitov, **arXiv** (2020)  
A. Levchenko, J. Schmallian, **Annal of Physics** (2020)

# Outline



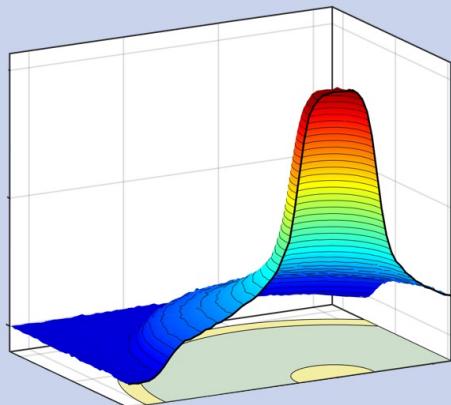
Theory: How hydrodynamics can eliminate resistance



Technique: imaging flowing Electrons



Imaging Poiseuille flow of hydrodynamic electrons



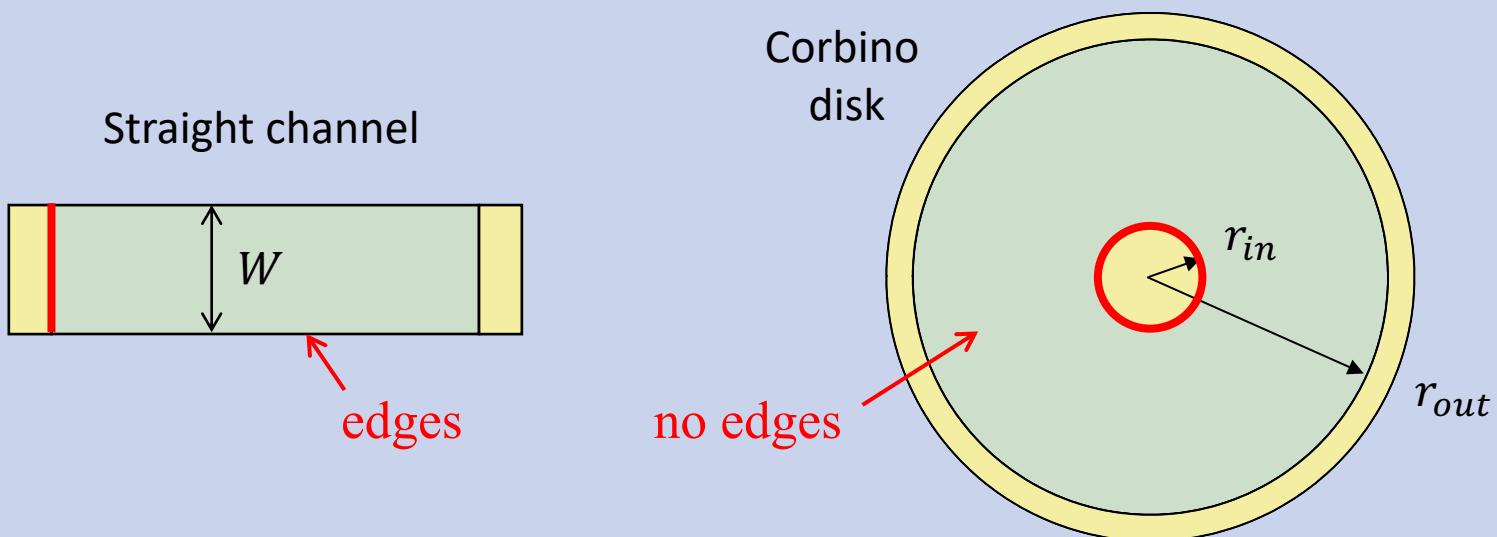
Imaging Corbino disk flow

Ballistic

Hydrodynamic

Magneto - hydrodynamic

# Corbino disk – Ballistic conductance



$R_{2probe}$  given by the narrowest region of the channel

$$R_{sh} = \frac{\pi h}{4e^2} \frac{1}{k_F W}$$

$$R_{sh}^{in} = \frac{\pi h}{4e^2} \frac{1}{k_F (2\pi r_{in})}$$

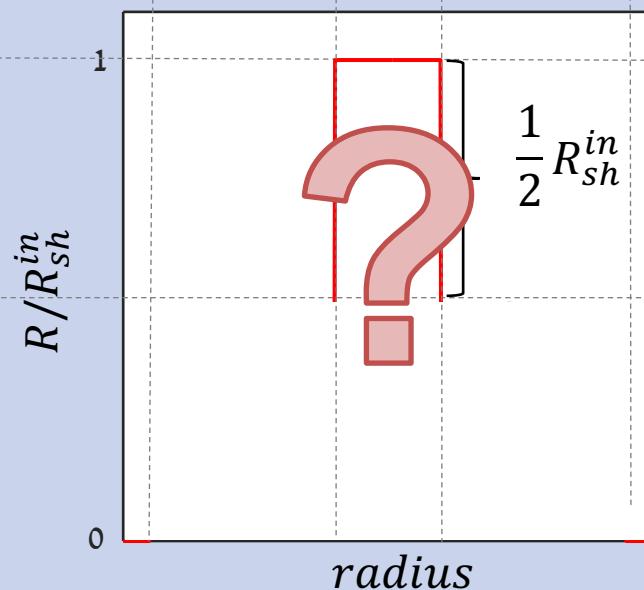
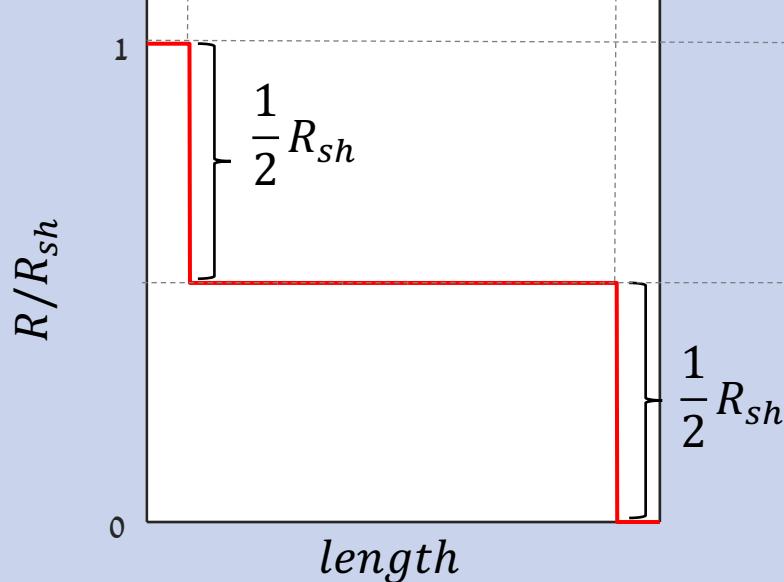
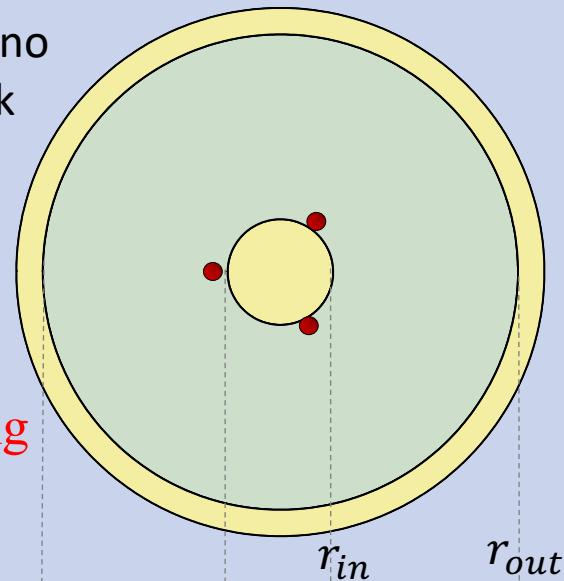
# Corbino disk – Ballistic conductance

Straight channel

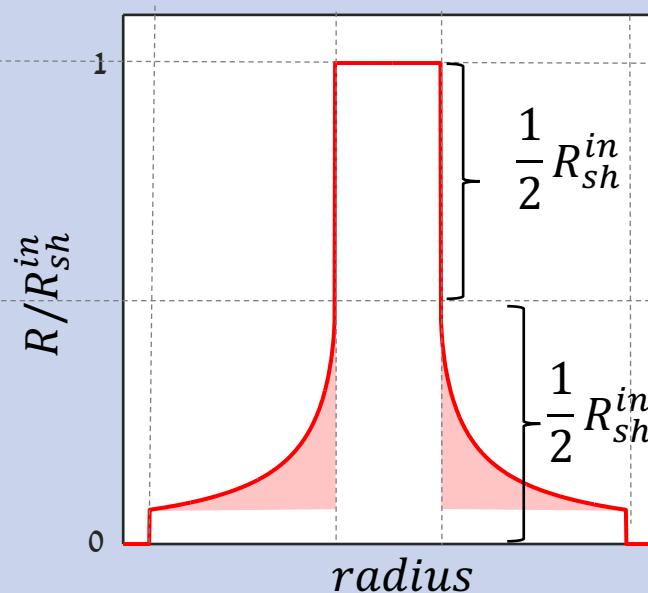
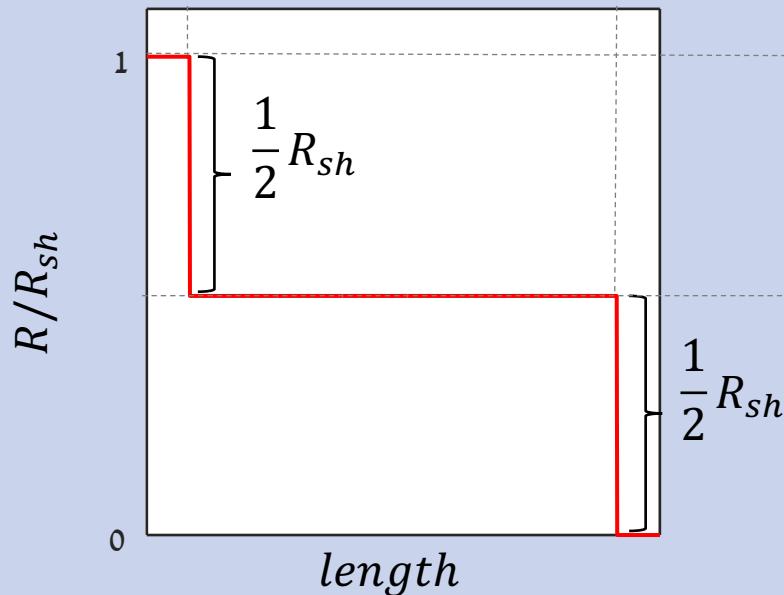
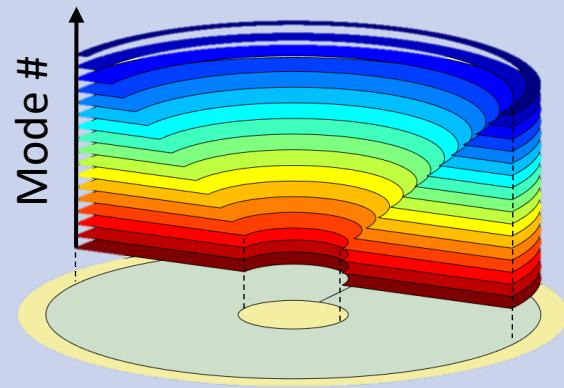
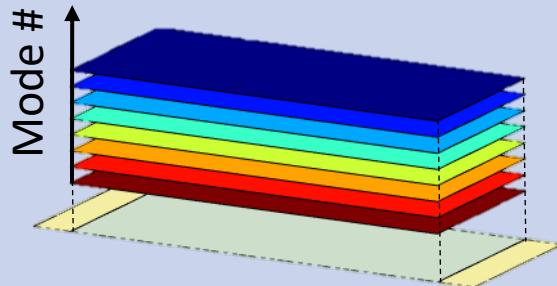


Corbino  
disk

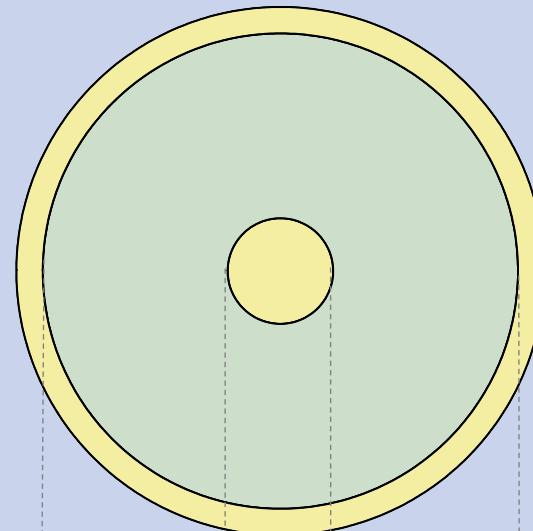
No back-scattering



# Corbino disk – Ballistic conductance



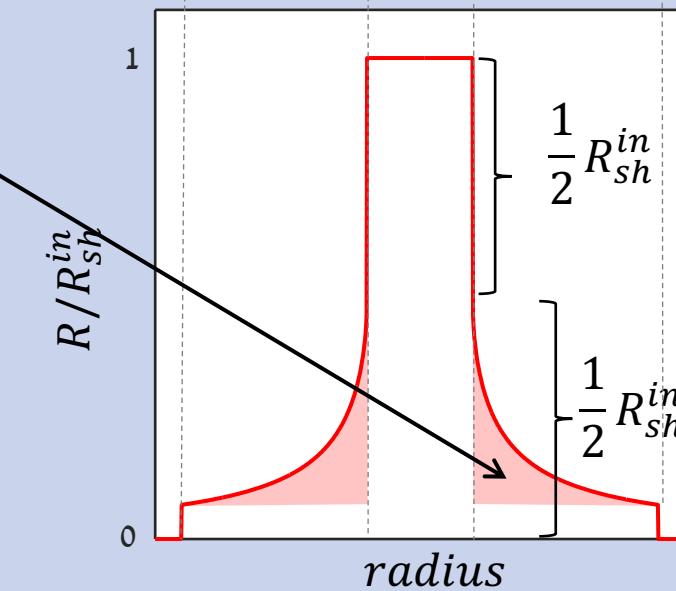
# Corbino disk – Ballistic conductance



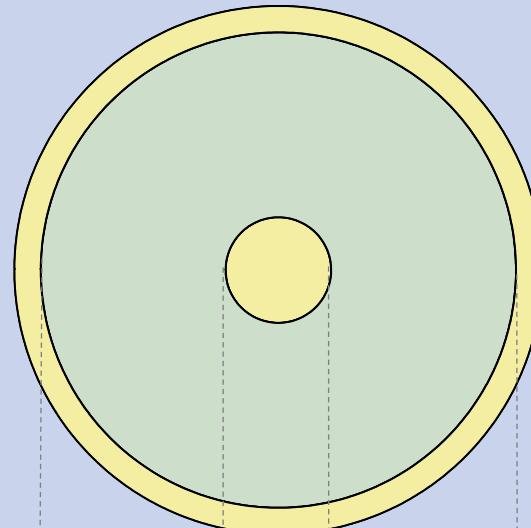
Bulk Landauer-Sharvin resistance

$$R_{LS}(r)/R_{sh}^{in} = \frac{1}{\pi} \arcsin \left( \frac{r_{in}}{r} \right)$$

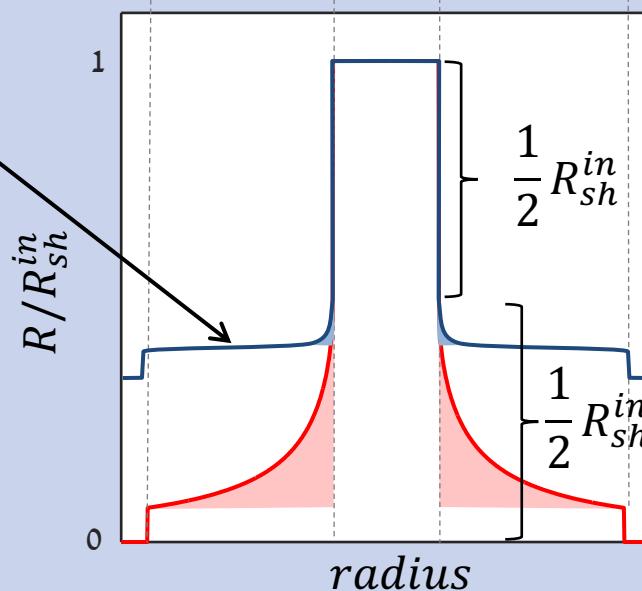
A geometrical/phase-space resistance



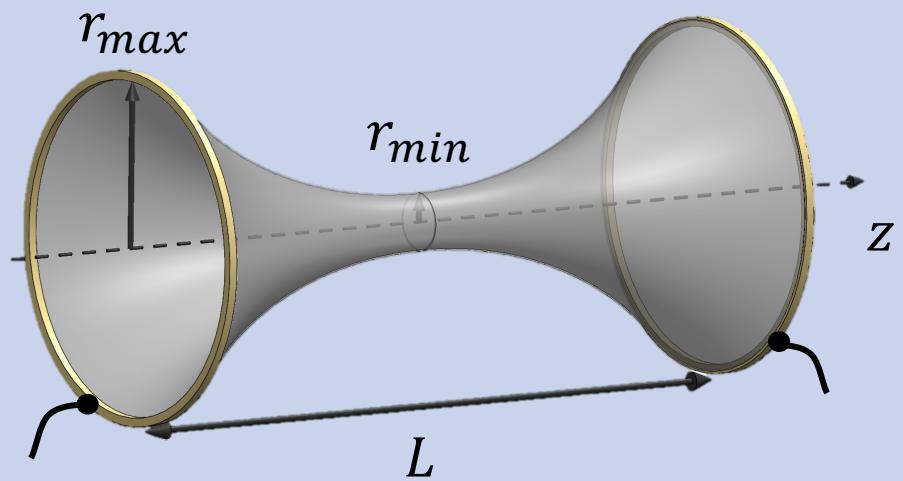
# Hydrodynamics – Shavit/Shytov/Falkovich prediction



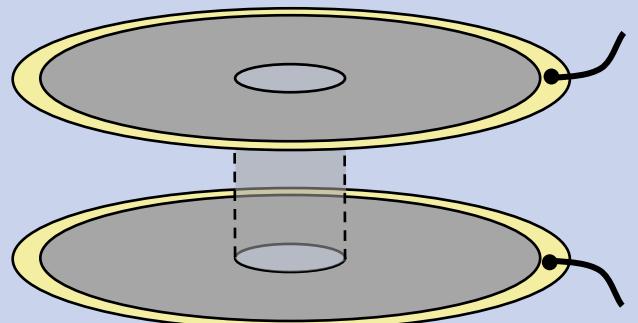
Hydrodynamically  
Half of the Landauer-Sharvin  
resistance is eliminated !!



# Can Landauer-Sharvin resistance be eliminated completely?



wormhole,  $r(z)$

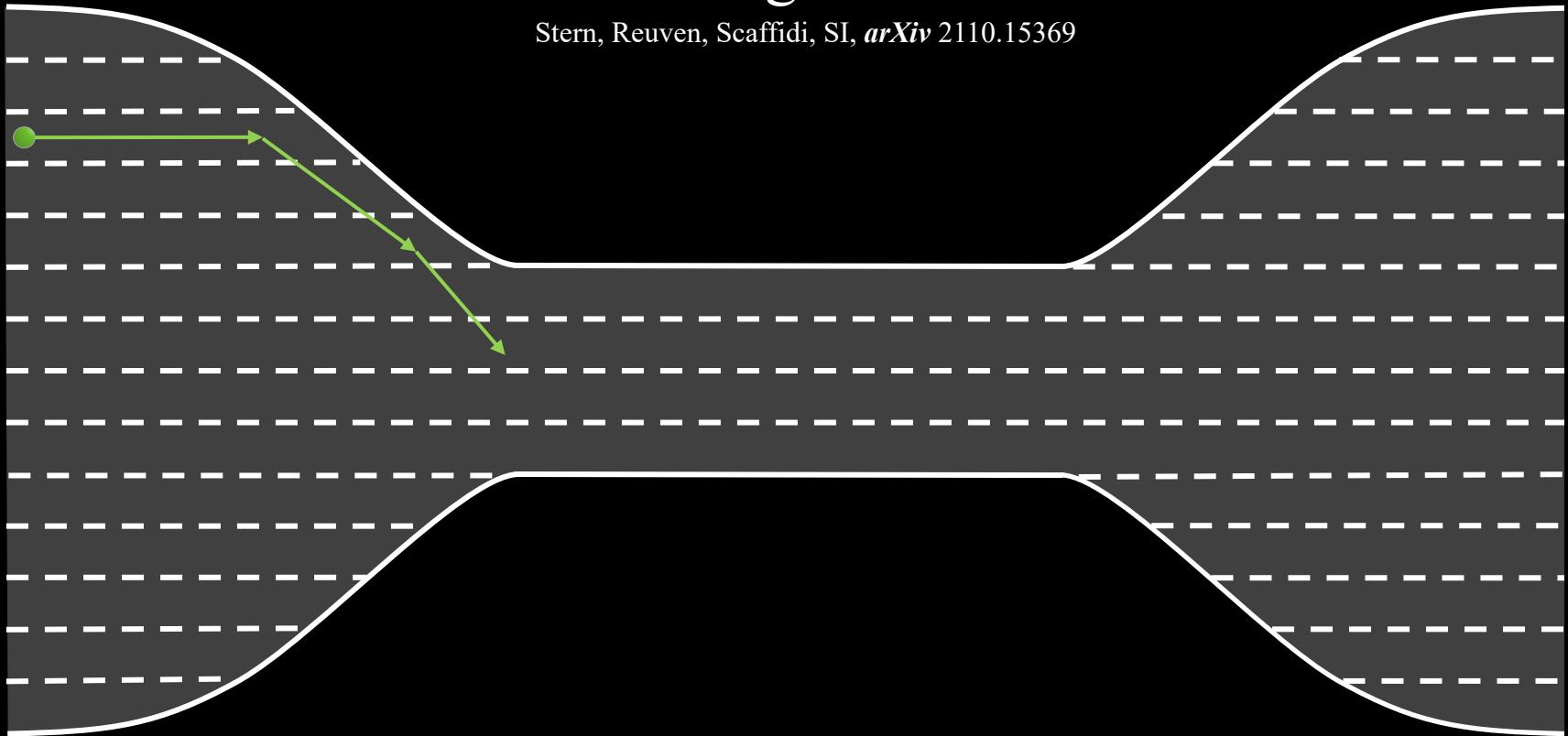


# A quantum mechanical traffic jam



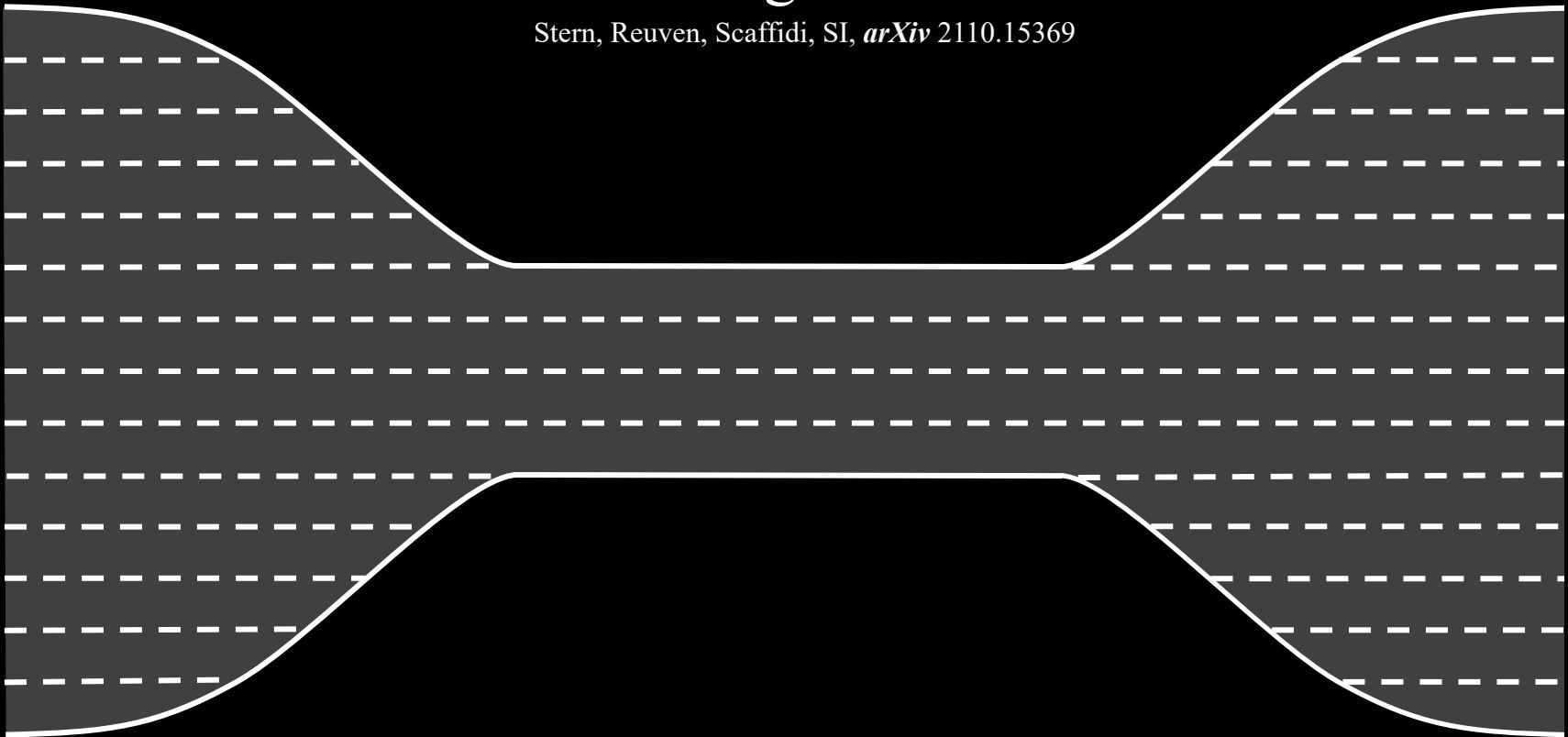
# Breaking the limit

Stern, Reuven, Scaffidi, SI, *arXiv* 2110.15369



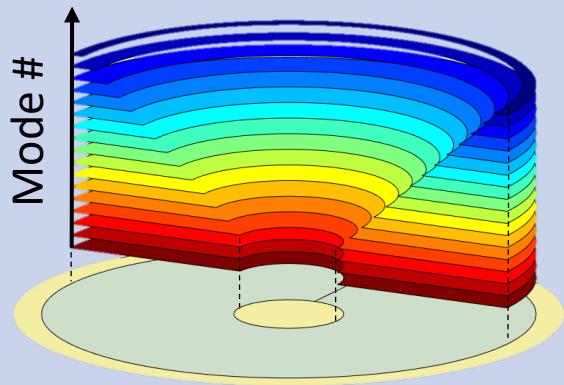
# Breaking the limit

Stern, Reuven, Scaffidi, SI, *arXiv* 2110.15369



# Corbino is an ideal half of the wormhole

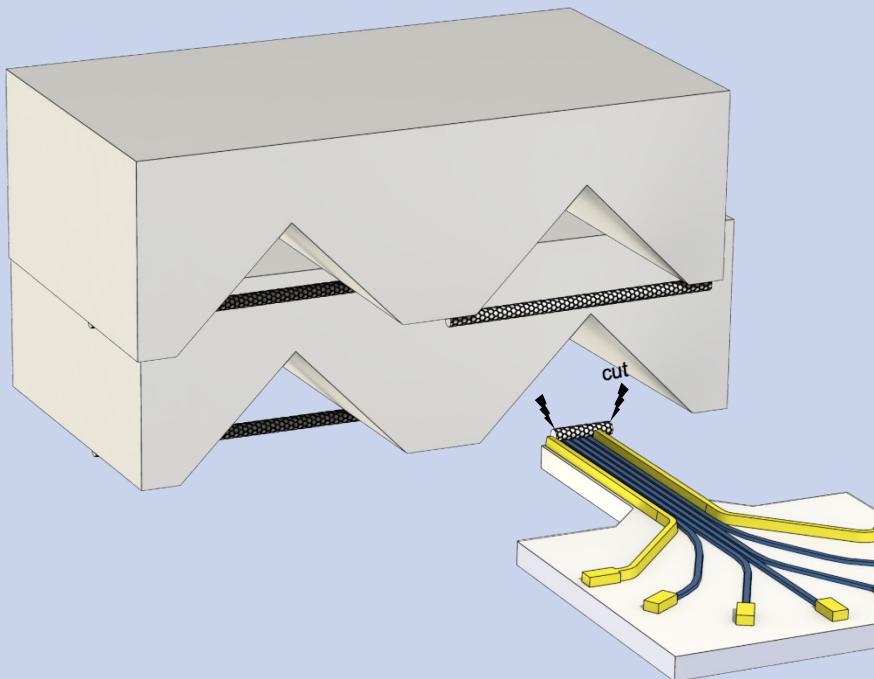
Stern, Reuven, Scaffidi, SI, **arXiv** 2110.15369



$$R_{ballistic} \sim r(z)'$$

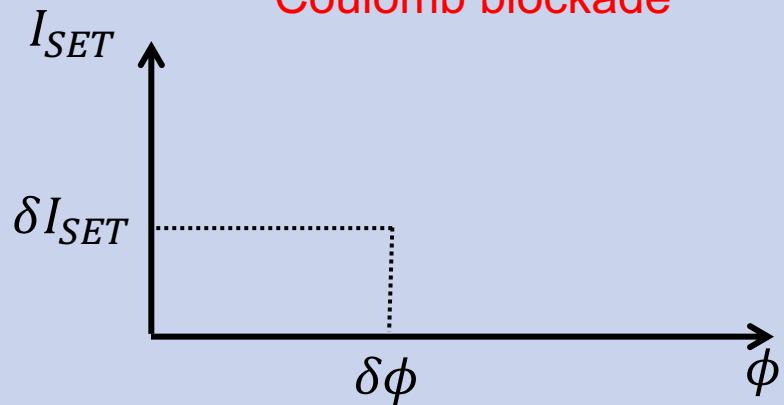
$$R_{hydro} \sim r(z)''$$

# A scanning nanotube single electron transistor (SET)

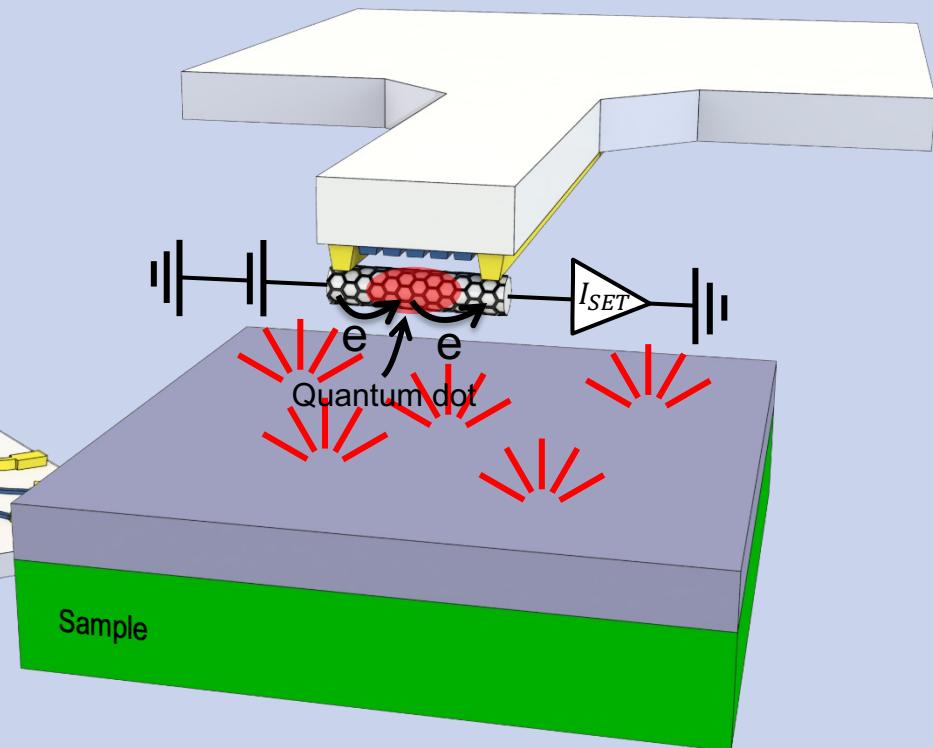


J. Waissman, SI et. al, **Nature Nanotechnology** (2013)

Coulomb blockade

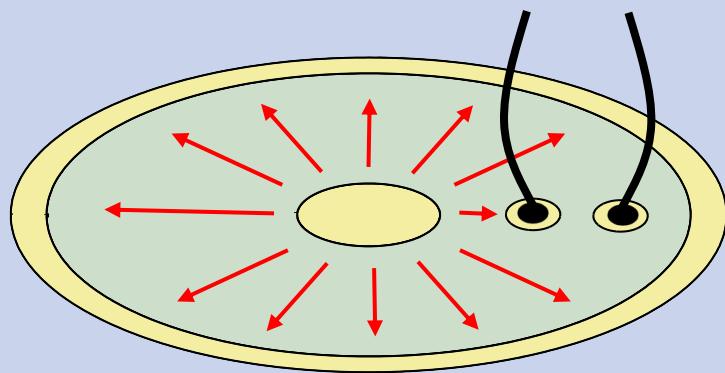
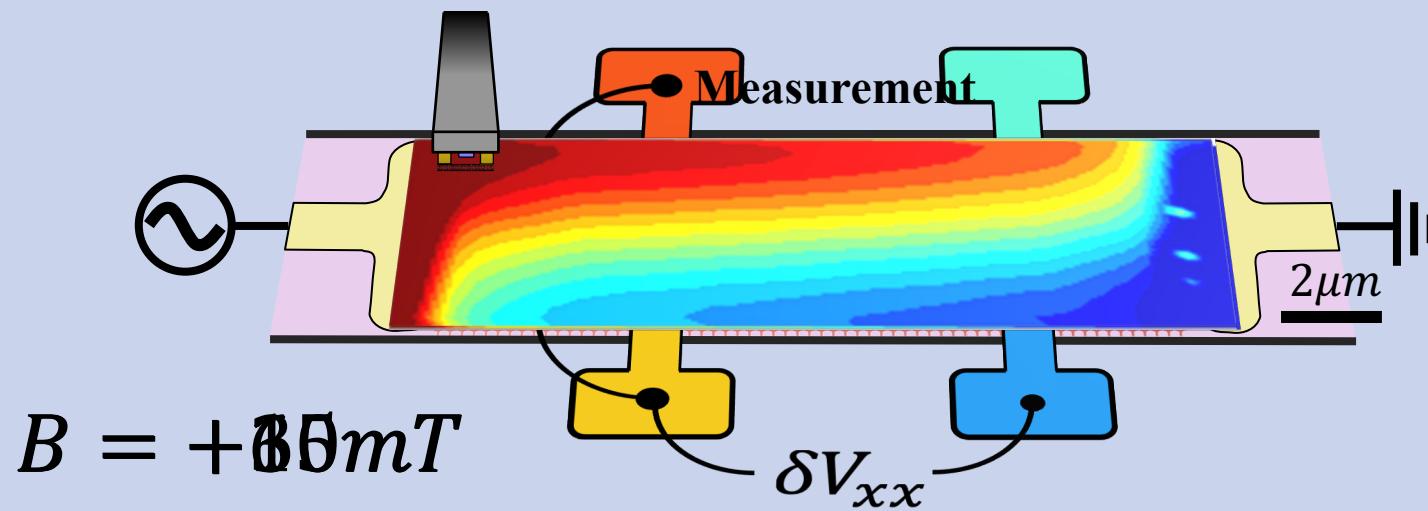


M. Honig, SI et. al, **Nature Materials** (2013)

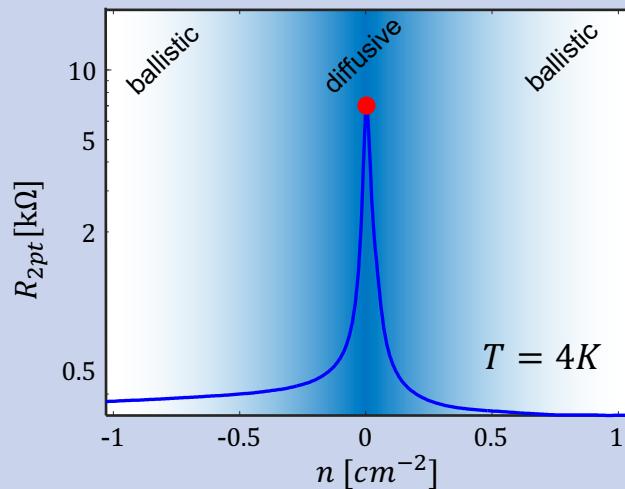


can measure:  
 $10^{-5} - 10^{-6}$  electron charge/ $\sqrt{\text{Hz}}$

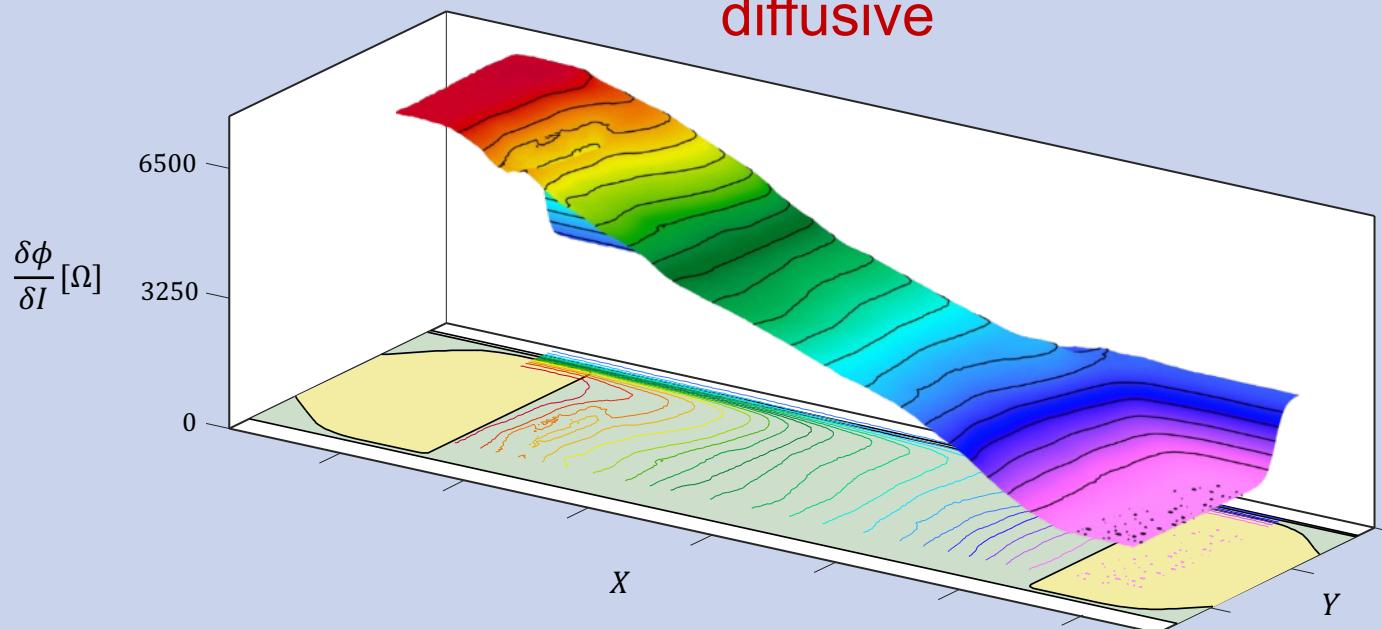
# Imaging flowing electrons (“Scanning Transport”)



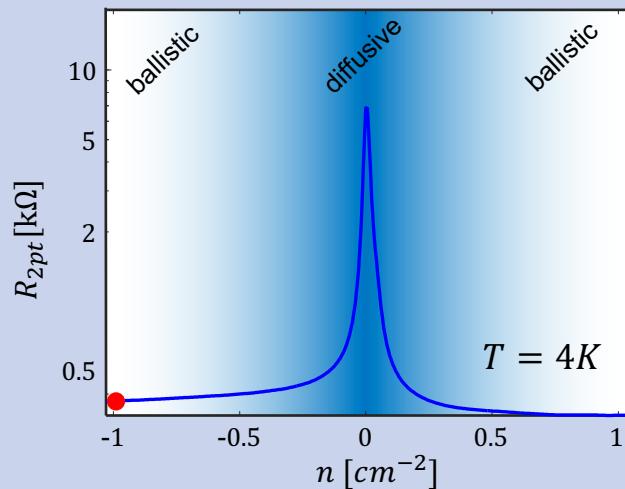
# Where is the resistance?



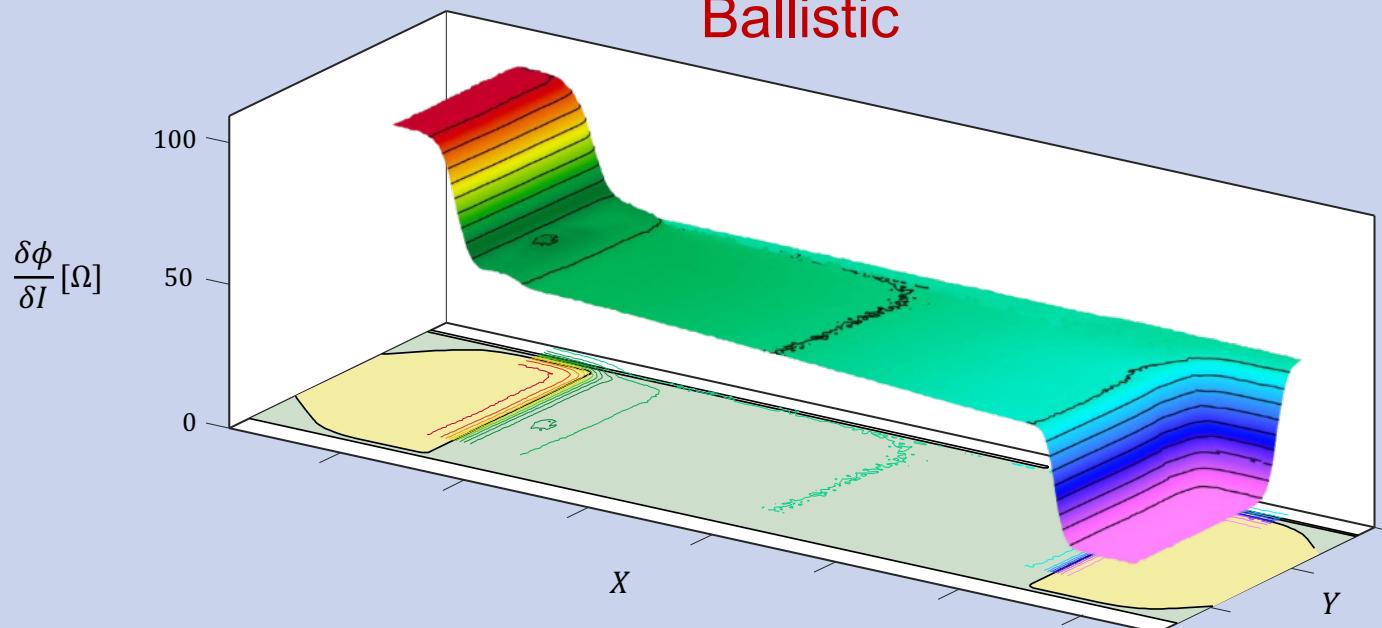
diffusive



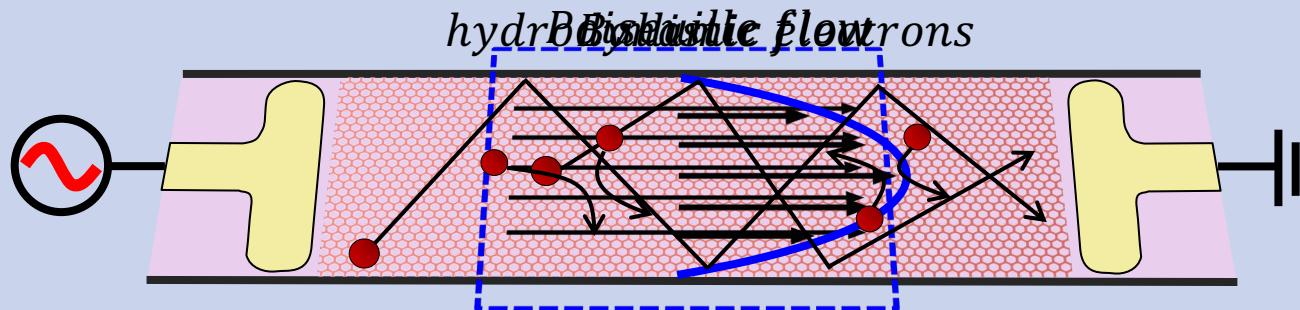
# Where is the resistance?



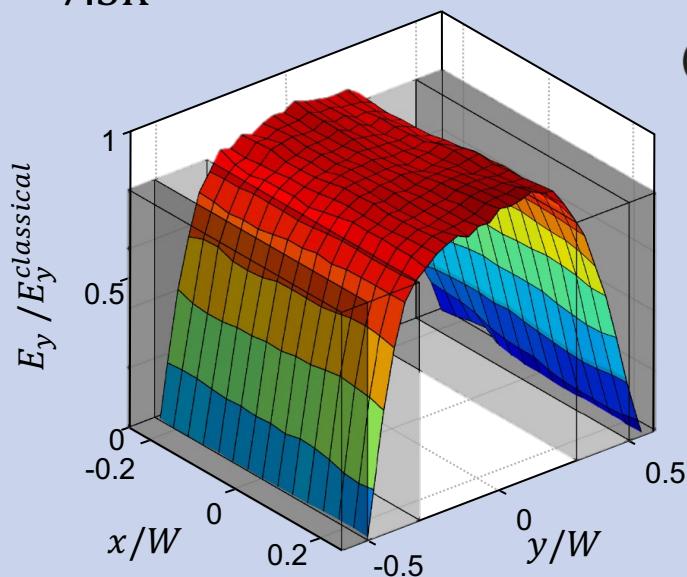
Ballistic



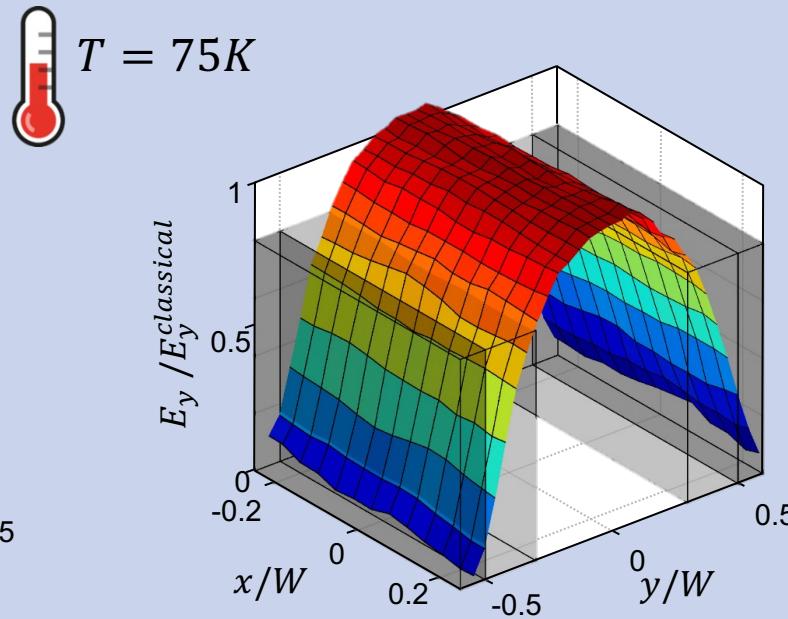
# Imaging hydrodynamic electrons in graphene



$T = 7.5K$



$T = 75K$

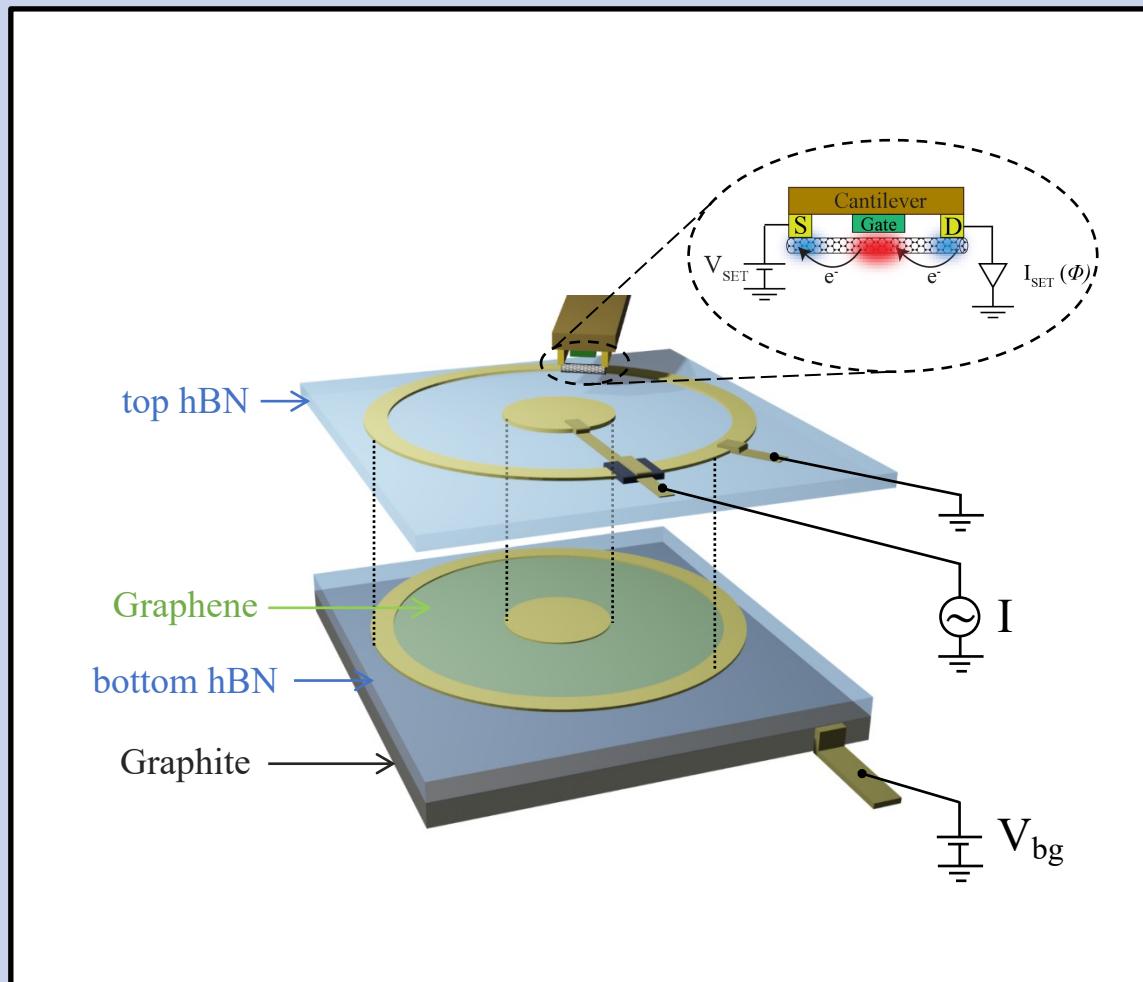


J.A. Sulpizio, SI et. al, L. Ella, A. Rozen, J. Birkbeck, D.J. Perello, D. Dutta, M. Ben-Shalom, T. Taniguchi, K. Watanabe, T. Holder, R. Queiroz, A. Stern, T. Scalfidi, A.K. Geim and SI, **Nature** 576, 75 (2019)

Imaging Poiseuille flow with NV centers: Ku, Yacoby et. al, **Nature** 583, 537 (2020)

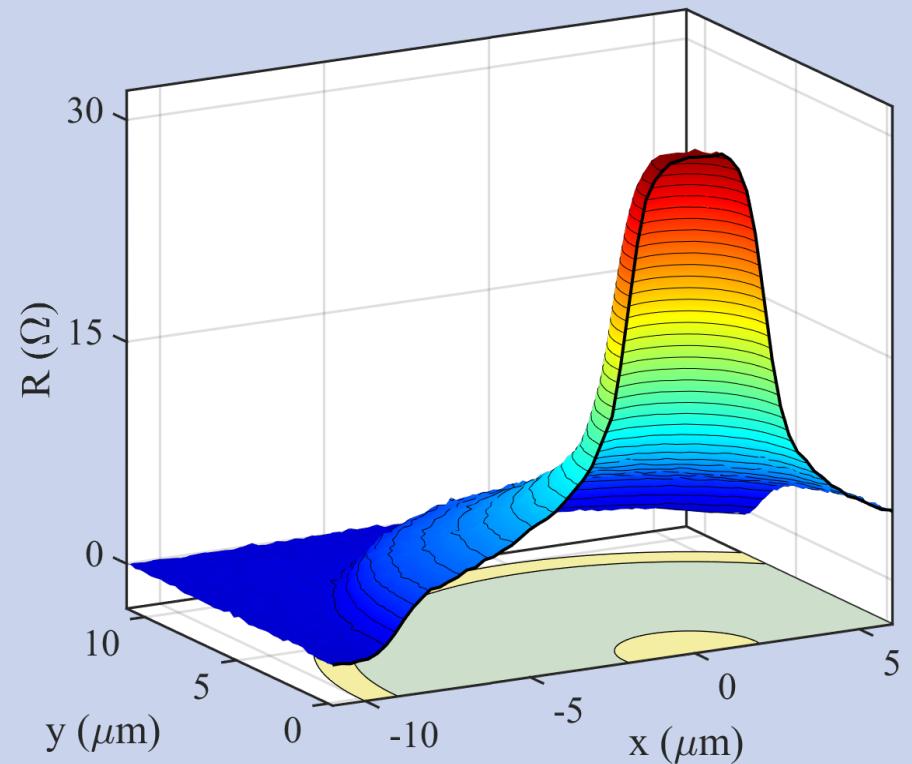
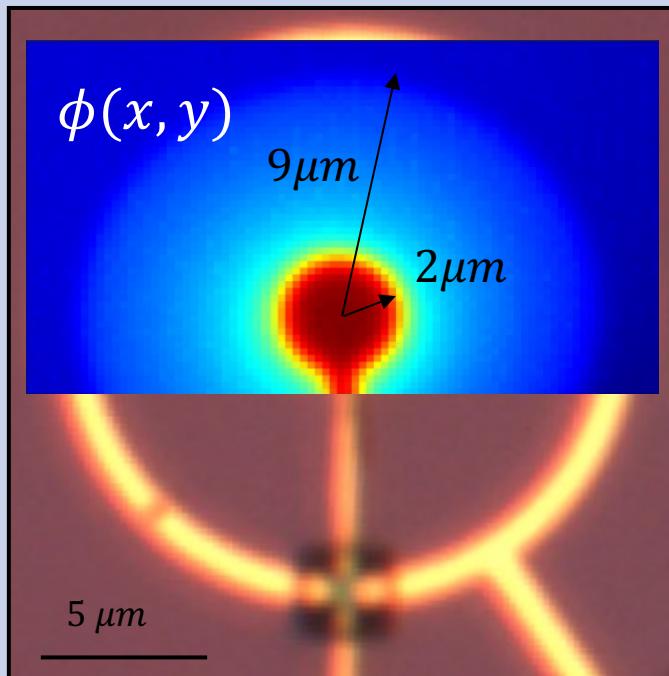
See also: Jenkins, Young, Bleszynski Jayich, et. al, **arXiv** 05065 (2020)

# Experimental setup

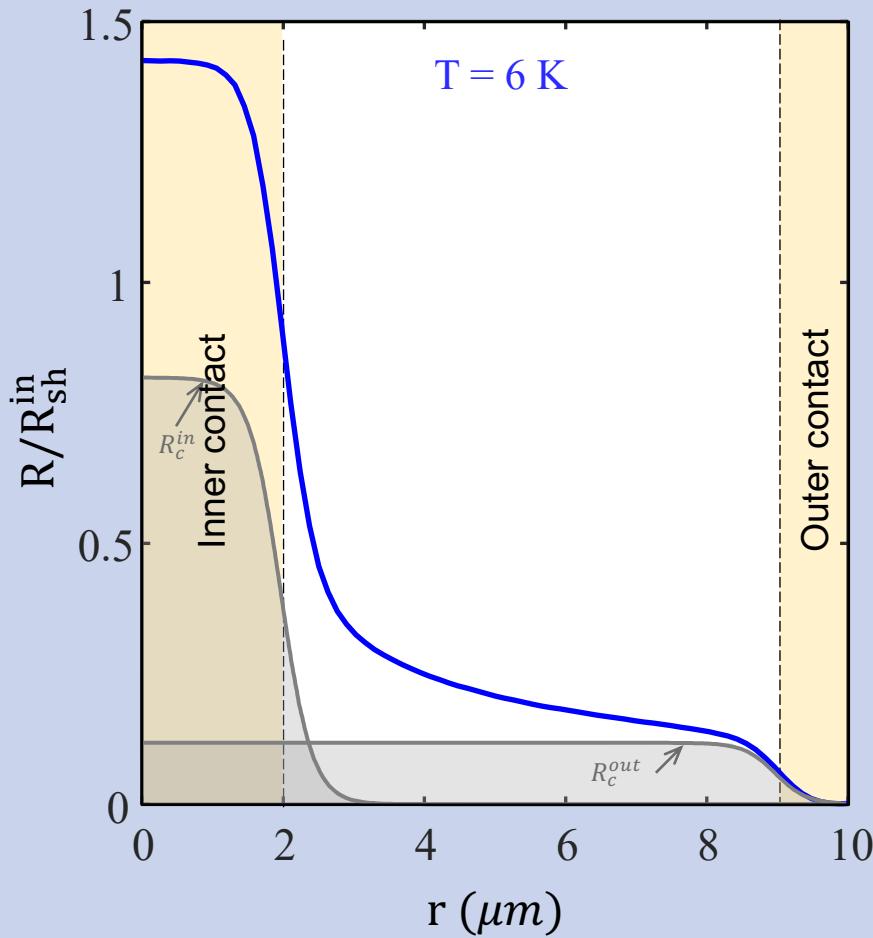


# Imaging of Corbino flow

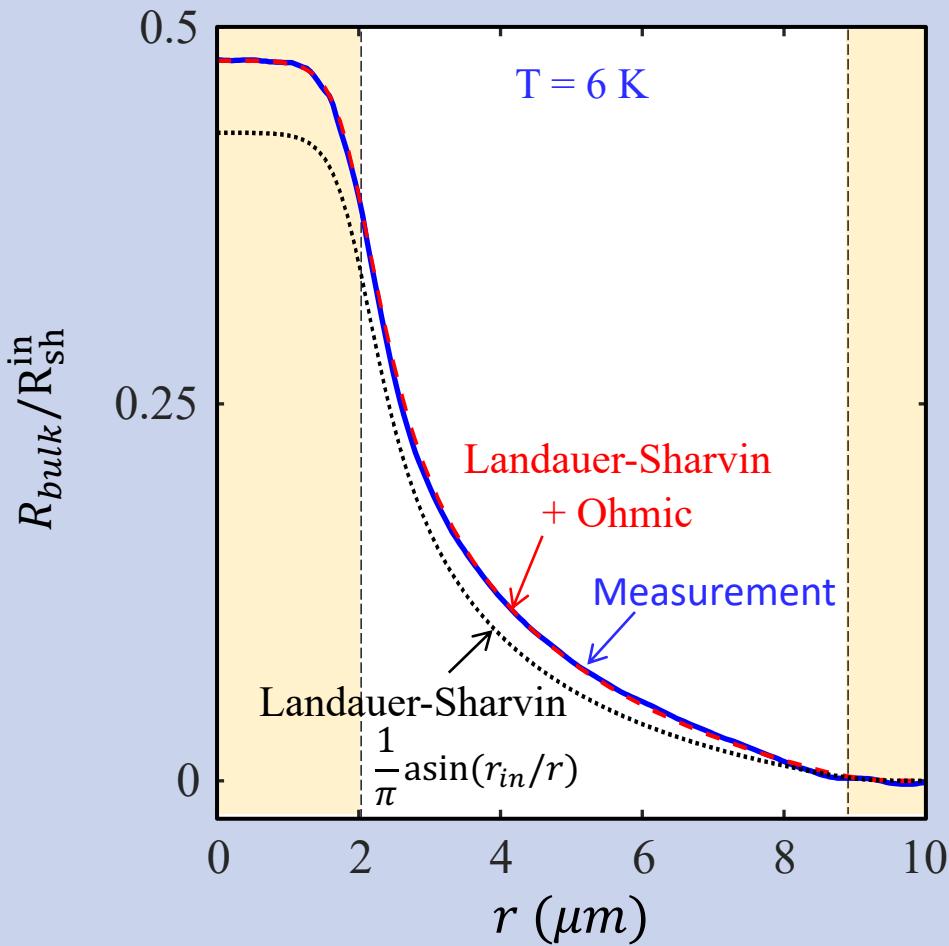
$$R(x, y) = \phi(x, y)/I$$



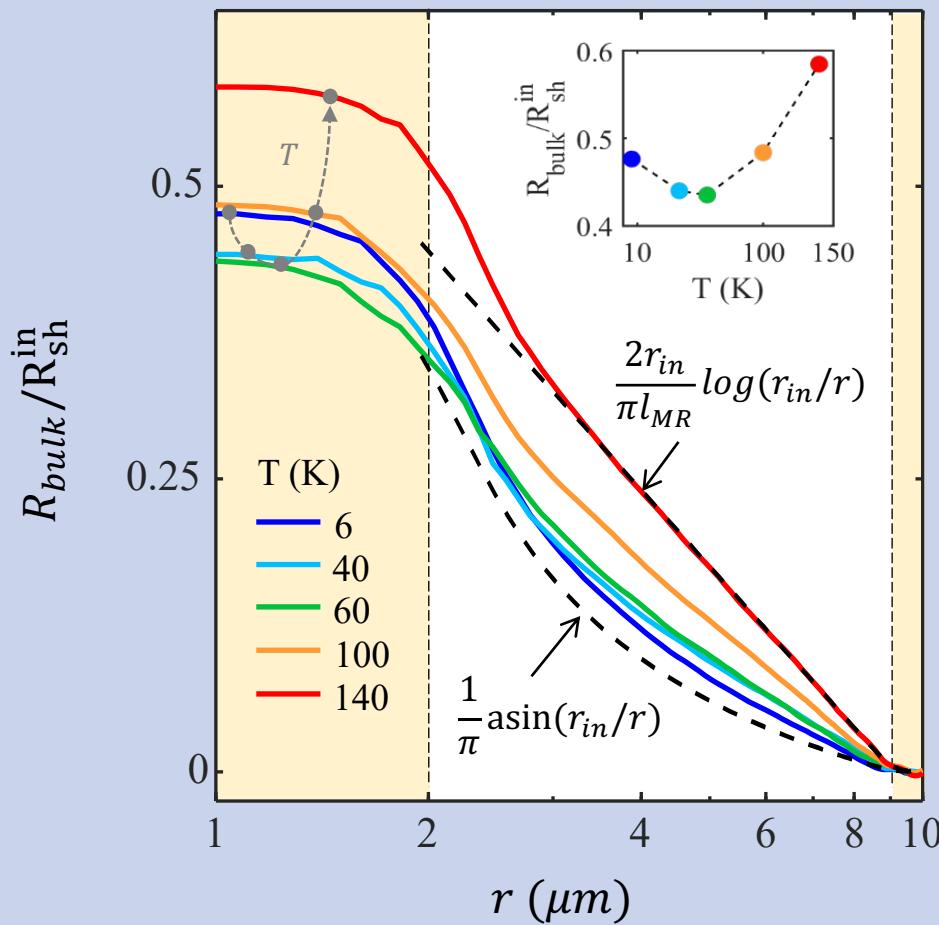
# The flow profile



# Bulk resistance profile



# Temperature dependence



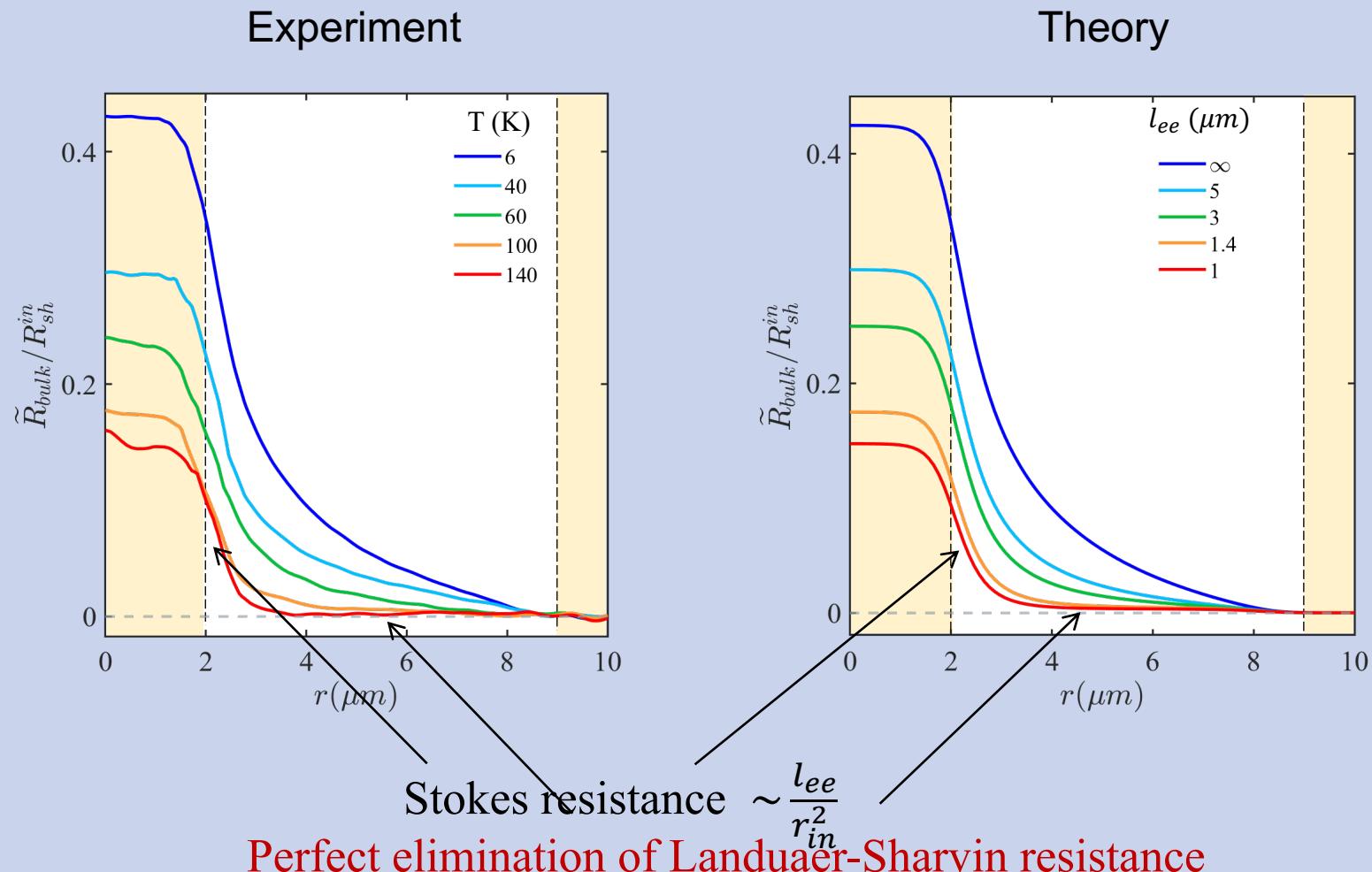
# A powerful identity for Corbino geometry

With azimuthal symmetry:

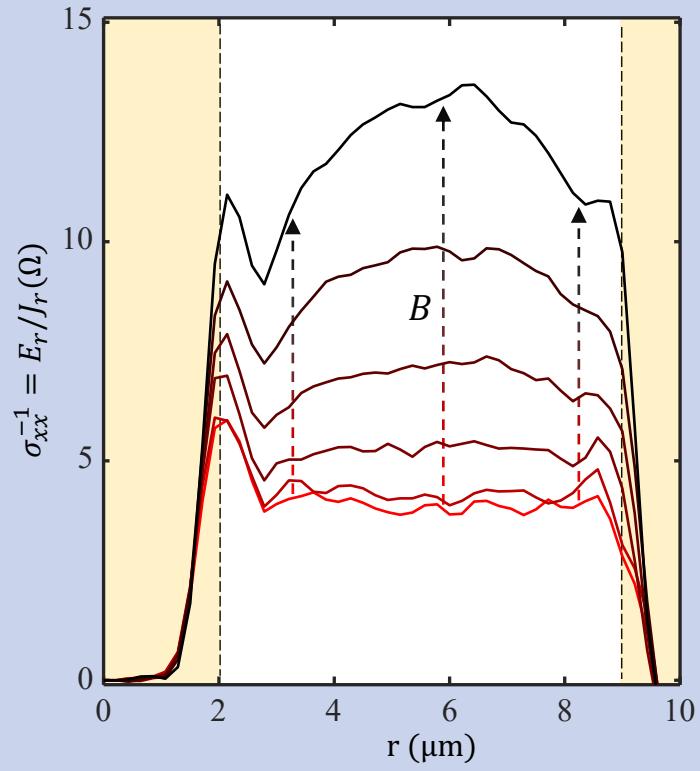
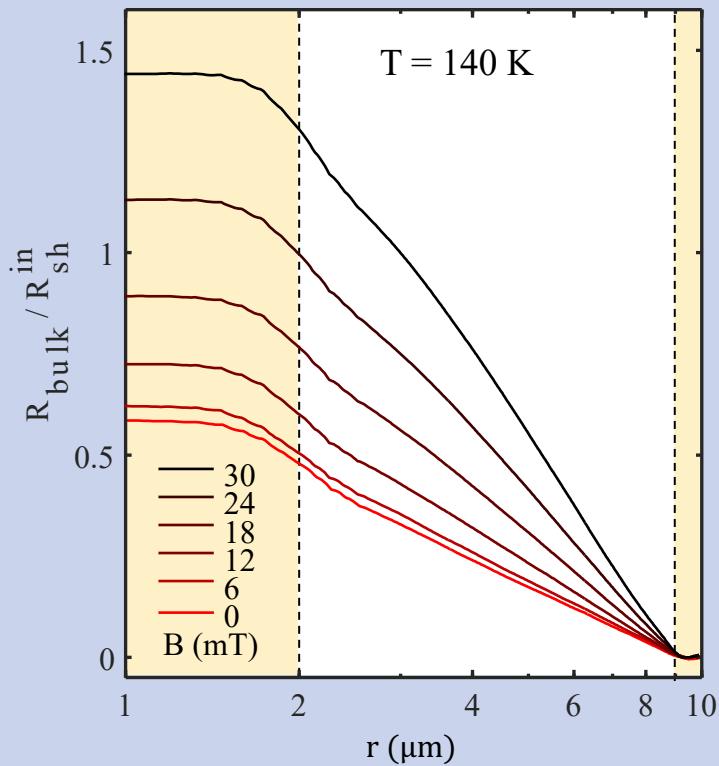
$$\tilde{R}(r)^{L_{MR}=\infty}_{L_{ee}=(l_{ee}^{-1}+l_{MR}^{-1})^{-1}} = R(r)^{L_{MR}=l_{MR}}_{L_{ee}=l_{ee}} - \frac{\hbar}{2e^2 k_F l_{MR}} \log(r_{in}/r)$$

Clean-limit hydrodynamic profile      with momentum relaxing scattering      Finite  $R_c$  experiments give  $l_{MR}$   
 $\tan(\theta_H) = l_{MR}/R_c$

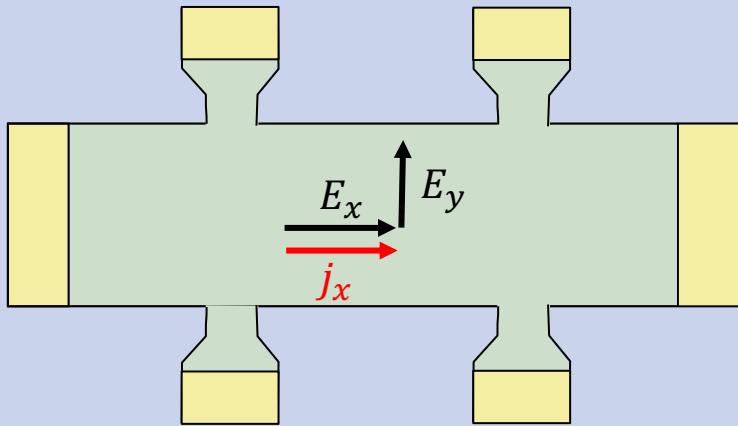
# Clean-limit Hydrodynamic profiles



# Hydrodynamics in magnetic Field

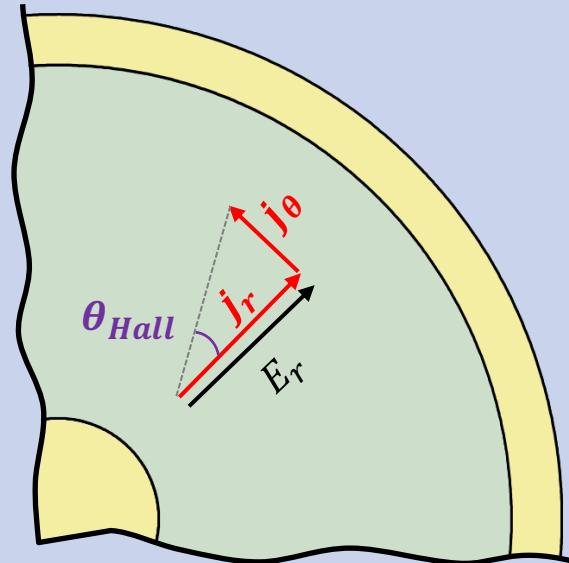


# What is measured in a Corbino geometry?



$$\rho_{xx}$$

resistivity

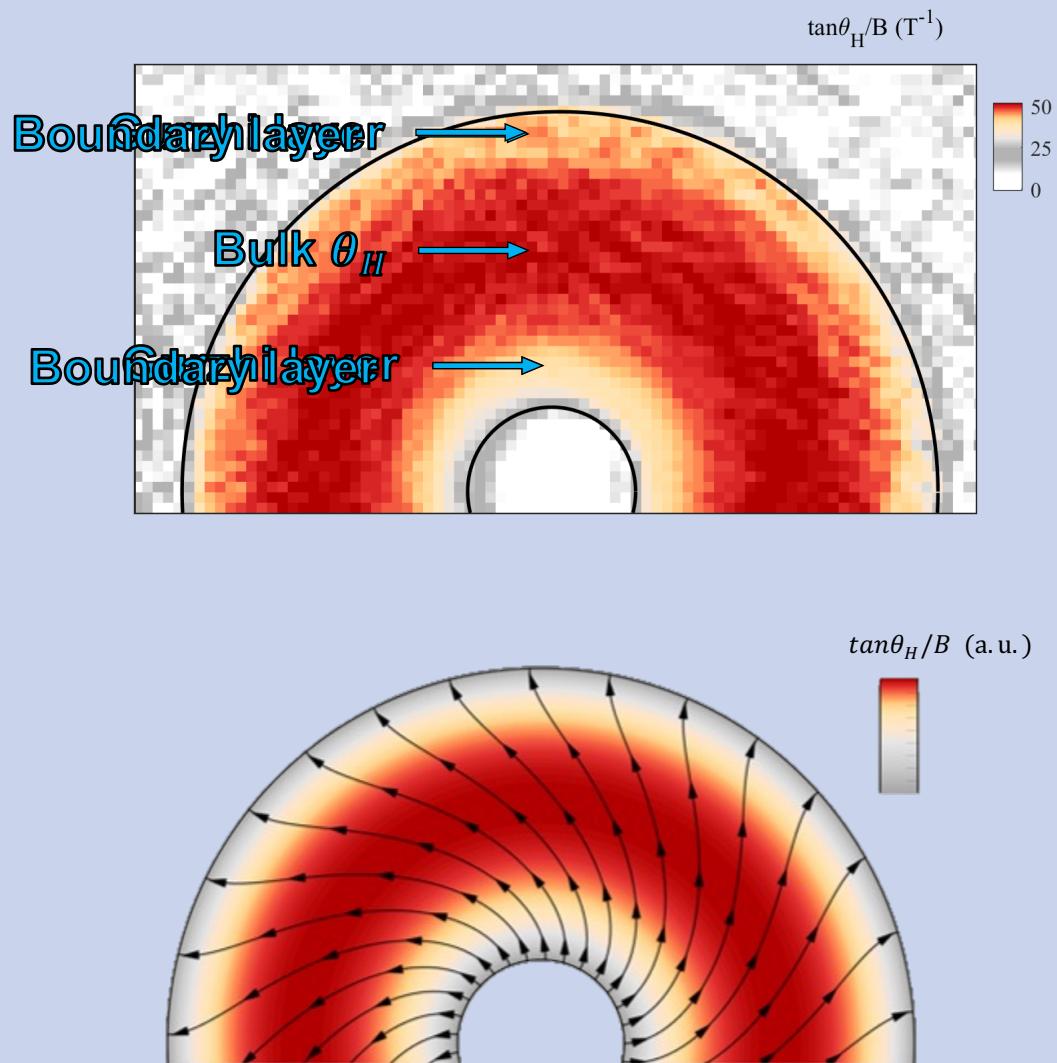
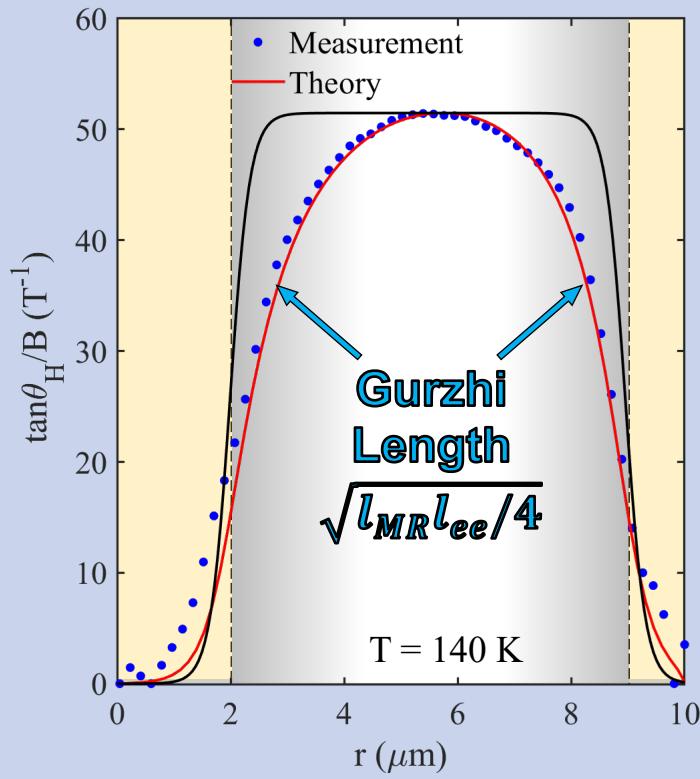


$$\sigma_{xx}^{-1}$$

inverse conductivity

$$\sigma_{xx}^{-1} = \frac{\rho_{xx}^2 + \rho_{xy}^2}{\rho_{xx}} = \rho_{xx}(1 + \tan^2(\theta_H))$$

# Flow in magnetic Field



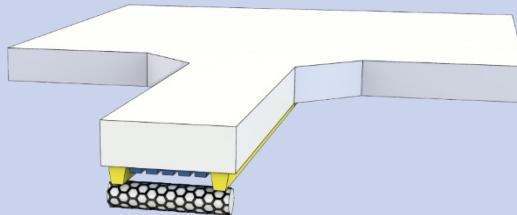
Kumar, Birkbeck, Sulpizio, Perello, Taniguchi, Watanabe, Reuven, Scaffidi, Stern, Geim, SI, [arXiv 2111.06412](#)

Shvait, A. Shytov and G. Falkovich, PRL (2019)

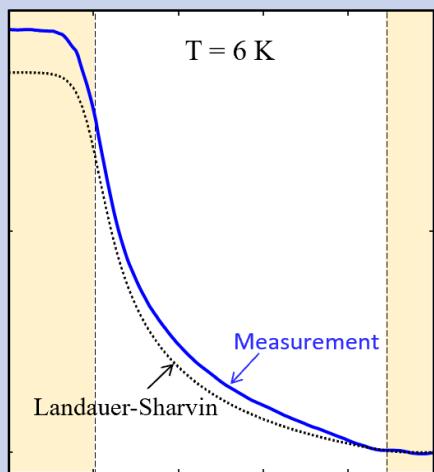
A. Levchenko, J. Schmallian, Annal of Physics (2020)

# Summary

## Geometrical Landau-Sharvin bulk resistance

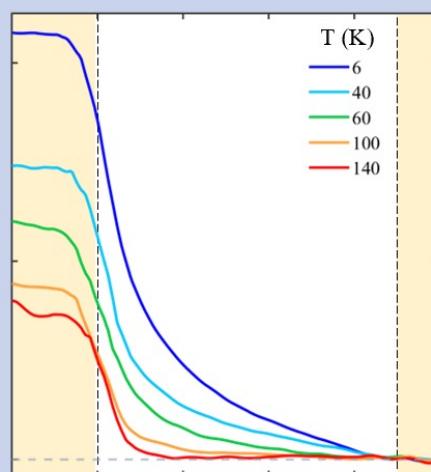


### Ballistic



Observation of LS bulk resistance

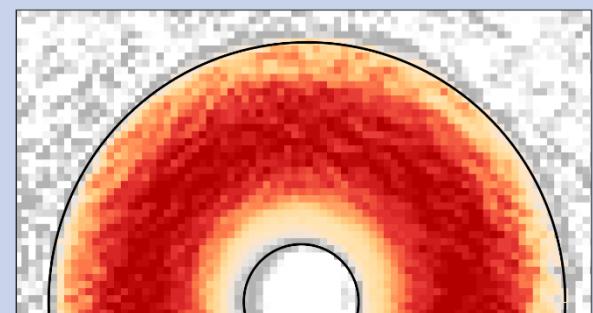
### Hydrodynamic



Stokes resistance

Perfect elimination of LS resistance in the bulk

### Magneto-hydrodynamic



Magnetic ‘viscometer’

Observation of the emergent Gurzhi length