

# **Transport in mesoscopic topological insulators: Antidot lattices and nanowires made from strained 3D HgTe**



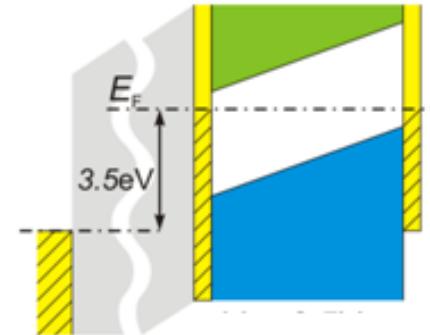
Dieter Weiss

Universität Regensburg

## Outline

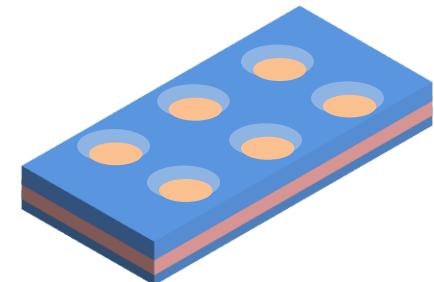
### ● Brief reminder

Transport and capacitance measurements



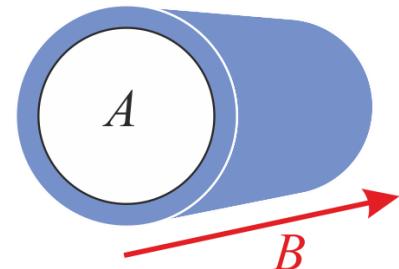
### ● Transport in antidot arrays

Resonances probe directly  $k_F$  and confirm topological nature of surface states



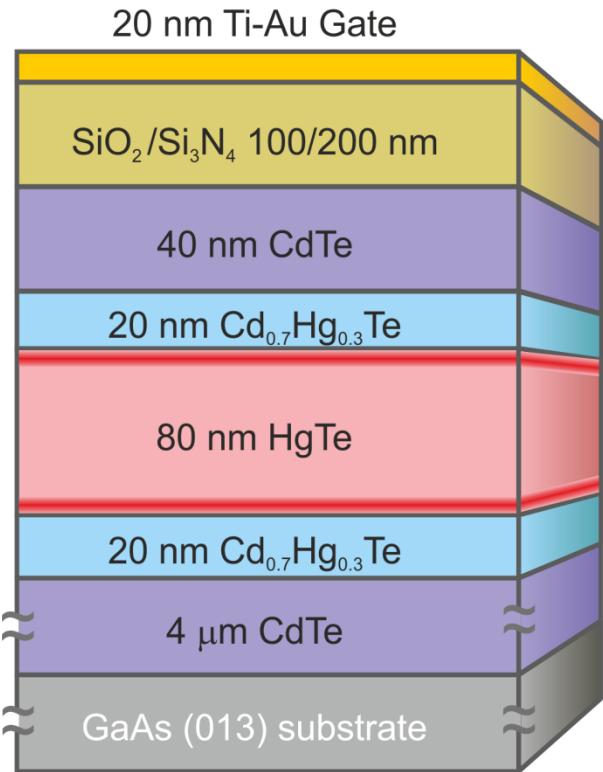
### ● TI nanowires

Confirmation of topological surface states  $\Rightarrow$   
Promising system to search for Majorana bound states





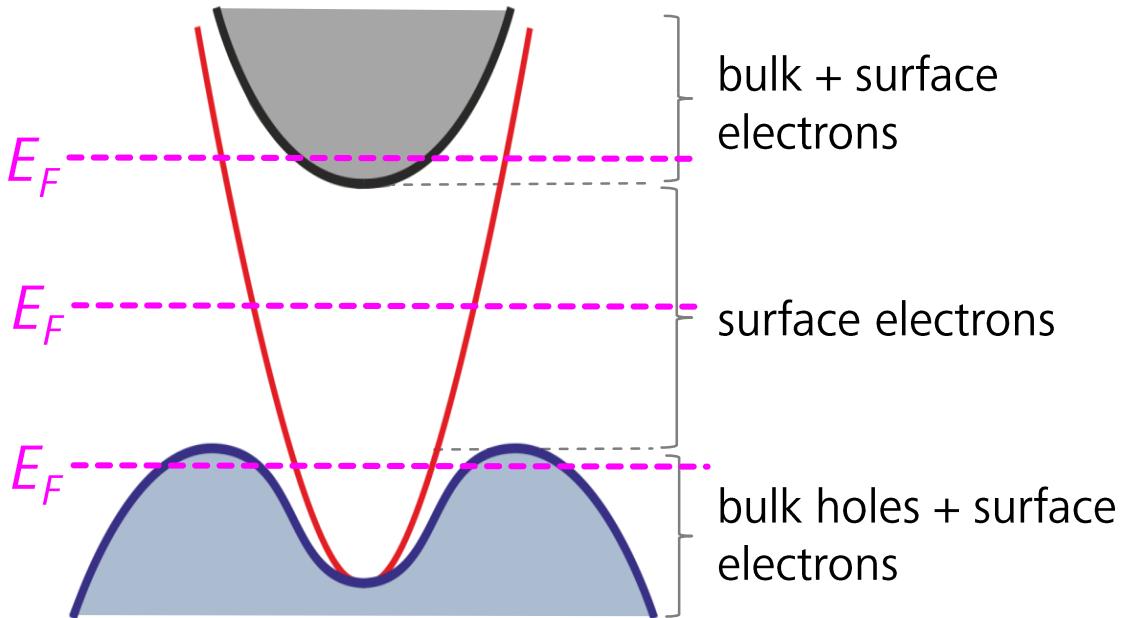
# Devices



HgTe tensile strained

high mobility: up to  $4 \cdot 10^5 \text{ cm}^2/\text{Vs}$

## schematic band structure



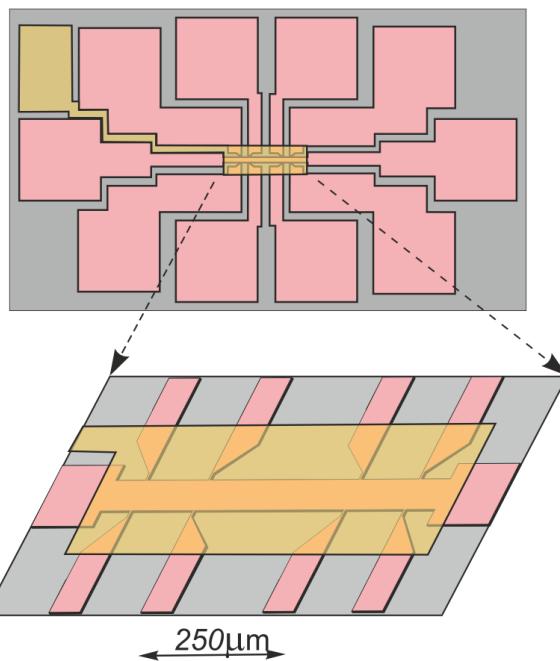
**HgTe material:**

Nikolai Mikhaylov, Sergey Dvuretsky, Novosibirsk  
See supplemental material for more details

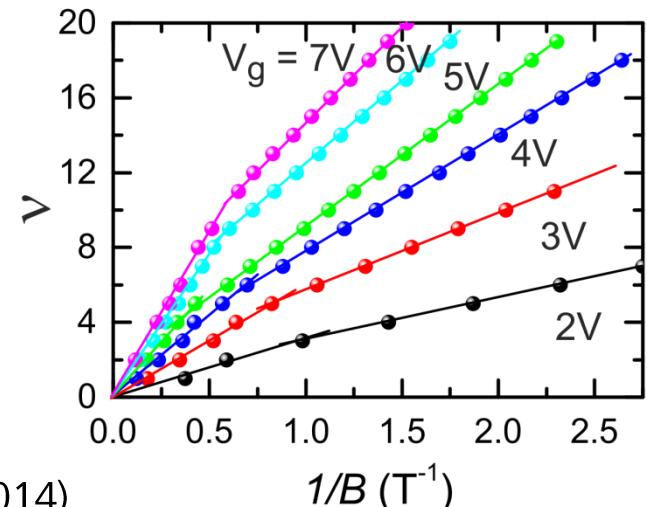
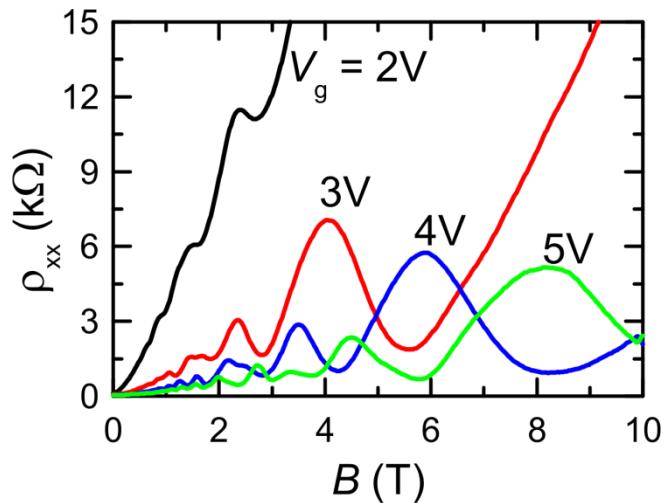
# Transport and (magneto-)capacitance experiments

## Sample Layout

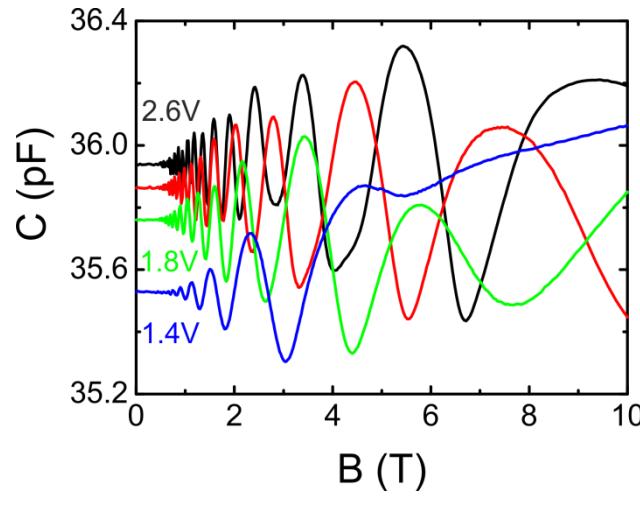
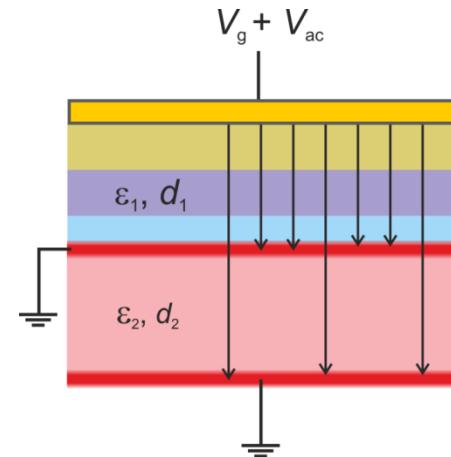
Top view



## Transport



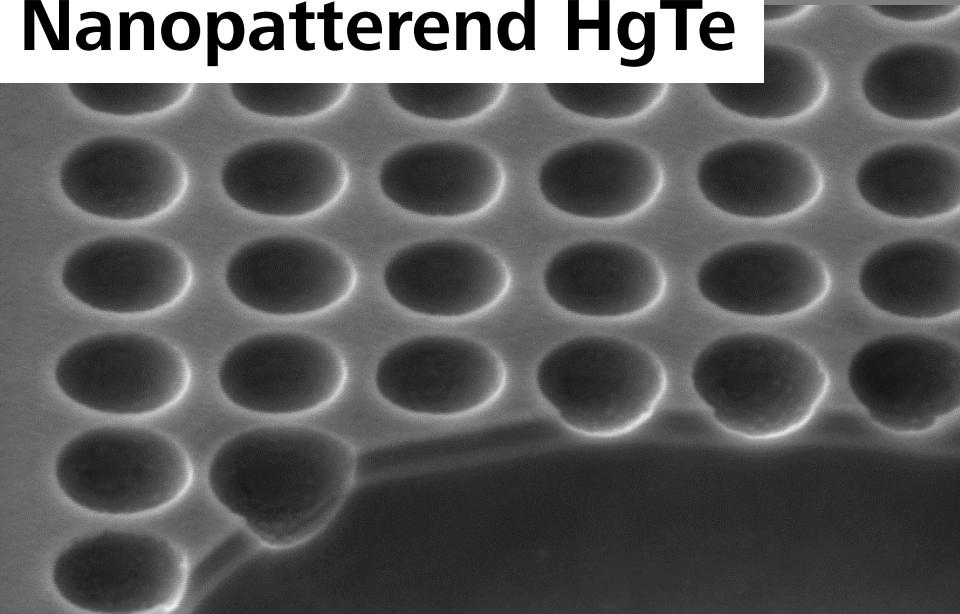
## Capacitance



More:

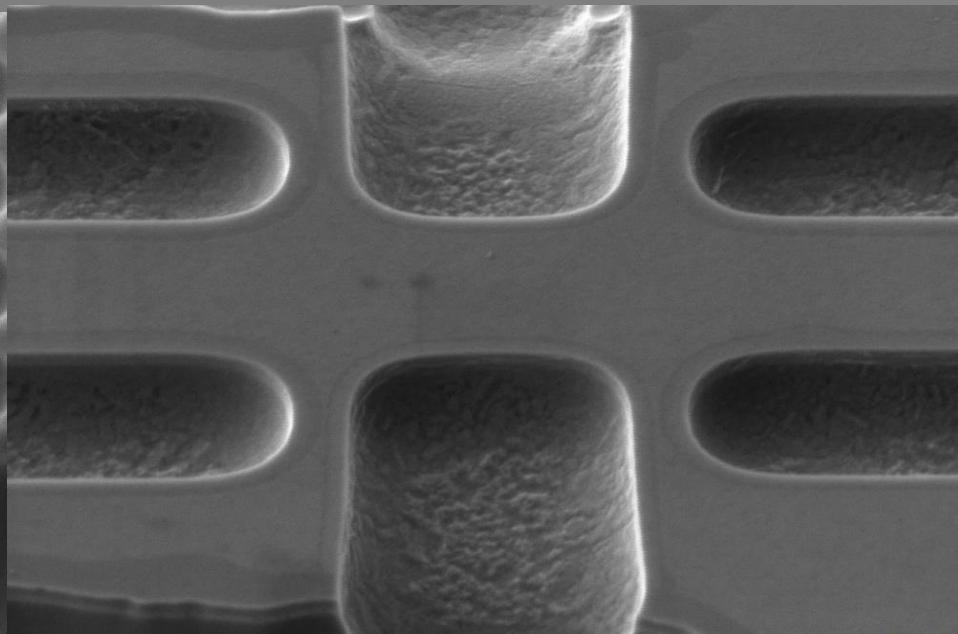
Kozlov et al. PRL **112**, 196801 (2014)Kozlov et al. PRL **116**, 166802 (2016)

# Nanopatterend HgTe



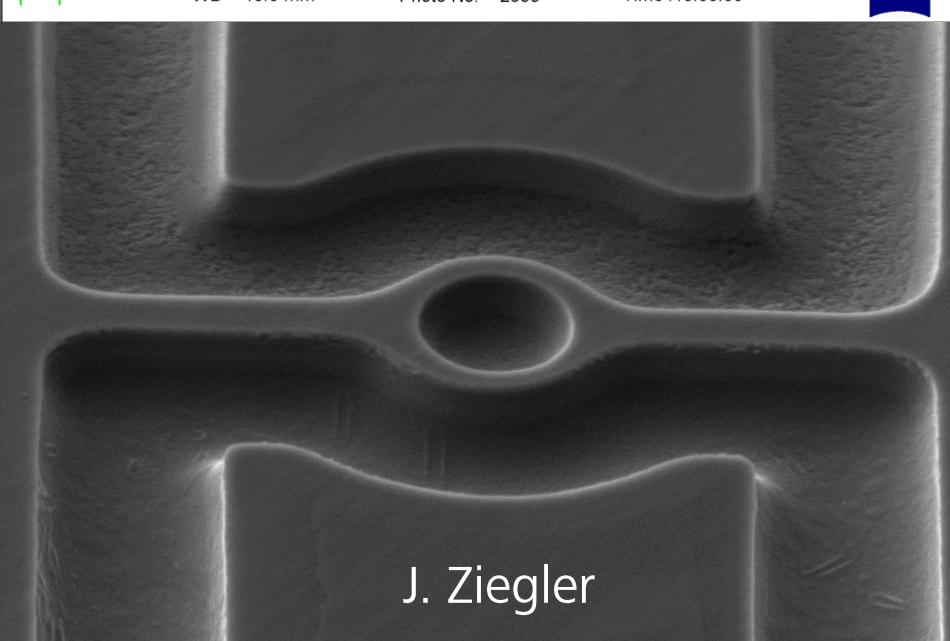
100 nm  
 H

EHT = 3.00 kV      Signal A = SE2  
WD = 10.0 mm      Date :25 Aug 2015  
Photo No. = 2653      Time :13:35:59



200 nm  
 H

EHT = 3.00 kV      Signal A = SE2  
WD = 11.0 mm      Date :13 Aug 2015  
Photo No. = 2641      Time :13:59:16



J. Ziegler

200 nm  
 H

EHT = 3.00 kV      Signal A = SE2  
WD = 8.0 mm      Date :25 Aug 2015  
Photo No. = 2643      Time :13:25:06

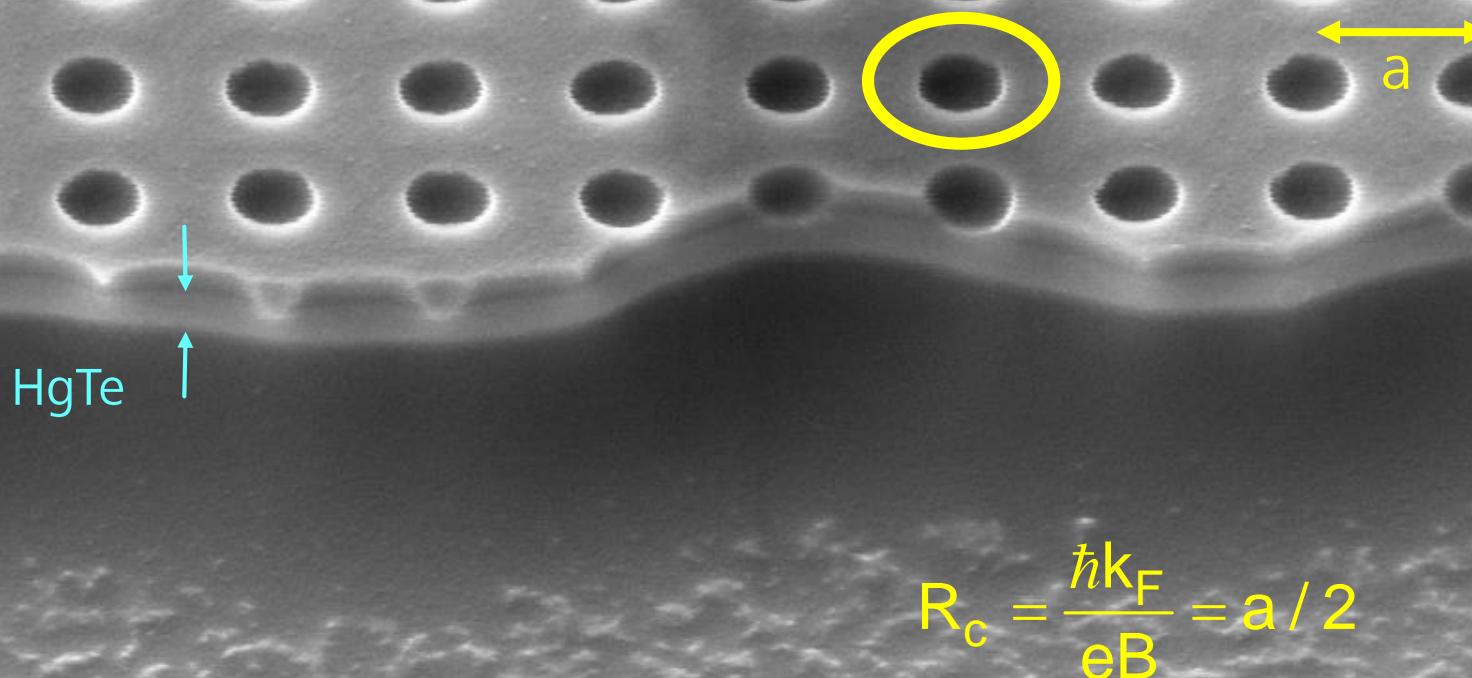


1 μm  
 H

EHT = 3.00 kV      Signal A = InLens  
WD = 4.0 mm      Date :25 Aug 2015  
Photo No. = 2605      Time :12:52:14



# Antidot lattice



300 nm  
—

Mag = 25.44 K X

WD = 10.6 mm

EHT = 5.00 kV

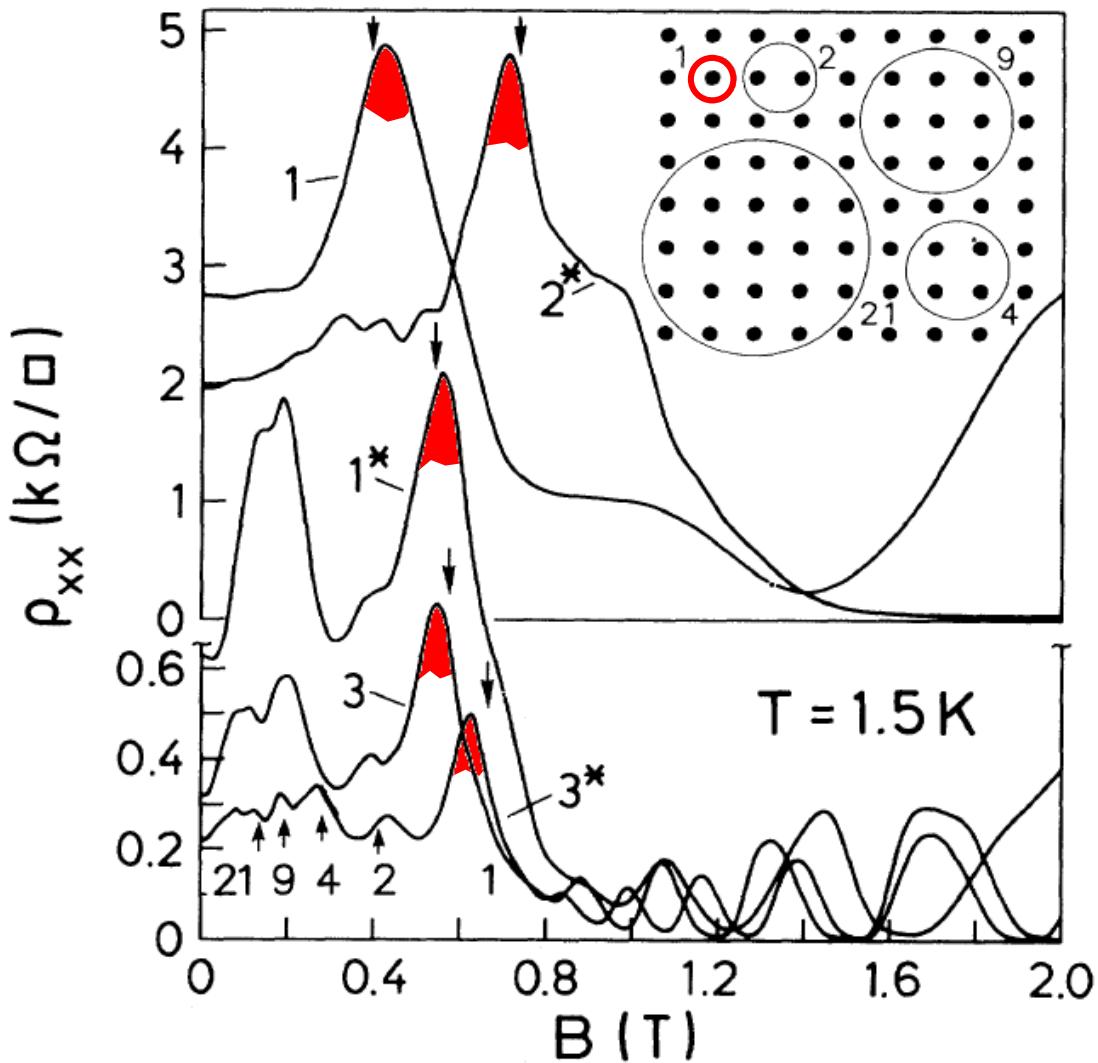
Signal A = SE2

Date : 3 Sep 2015



# Geometric resonances in an antidot lattice \*

\*periodic array of holes punched through 2DES



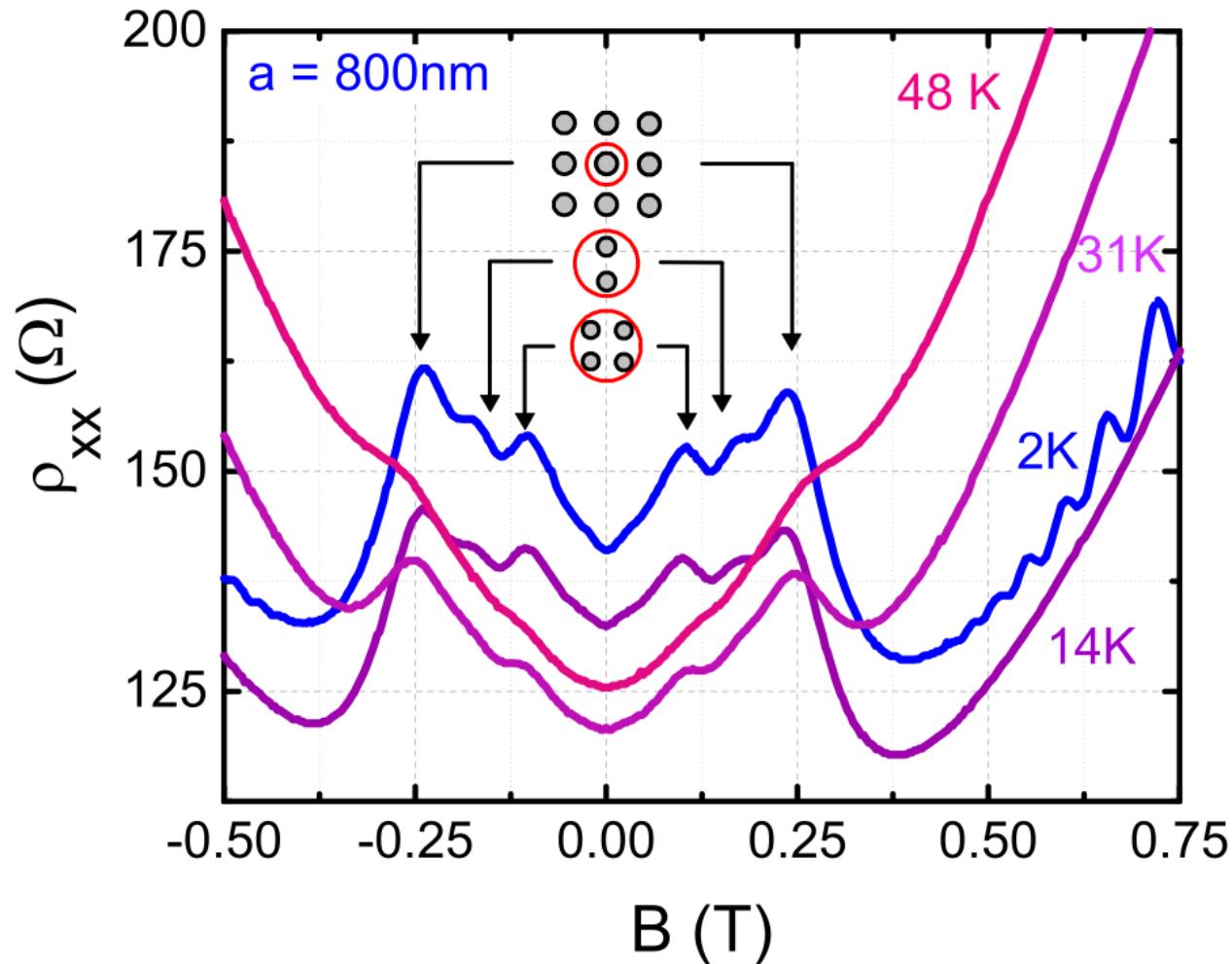
Mean free path  $\gg a$

Resistance peaks whenever cyclotron orbit  $R_c$  can orbit around group of antidots

Fundamental peak at  $2R_c = a$

$$R_c = \frac{\hbar \sqrt{2\pi n_s}}{eB}$$

# Antidot resonances in HgTe – T dependence

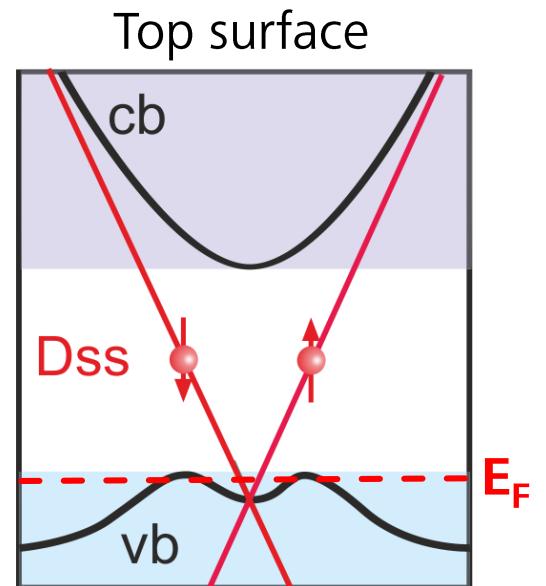
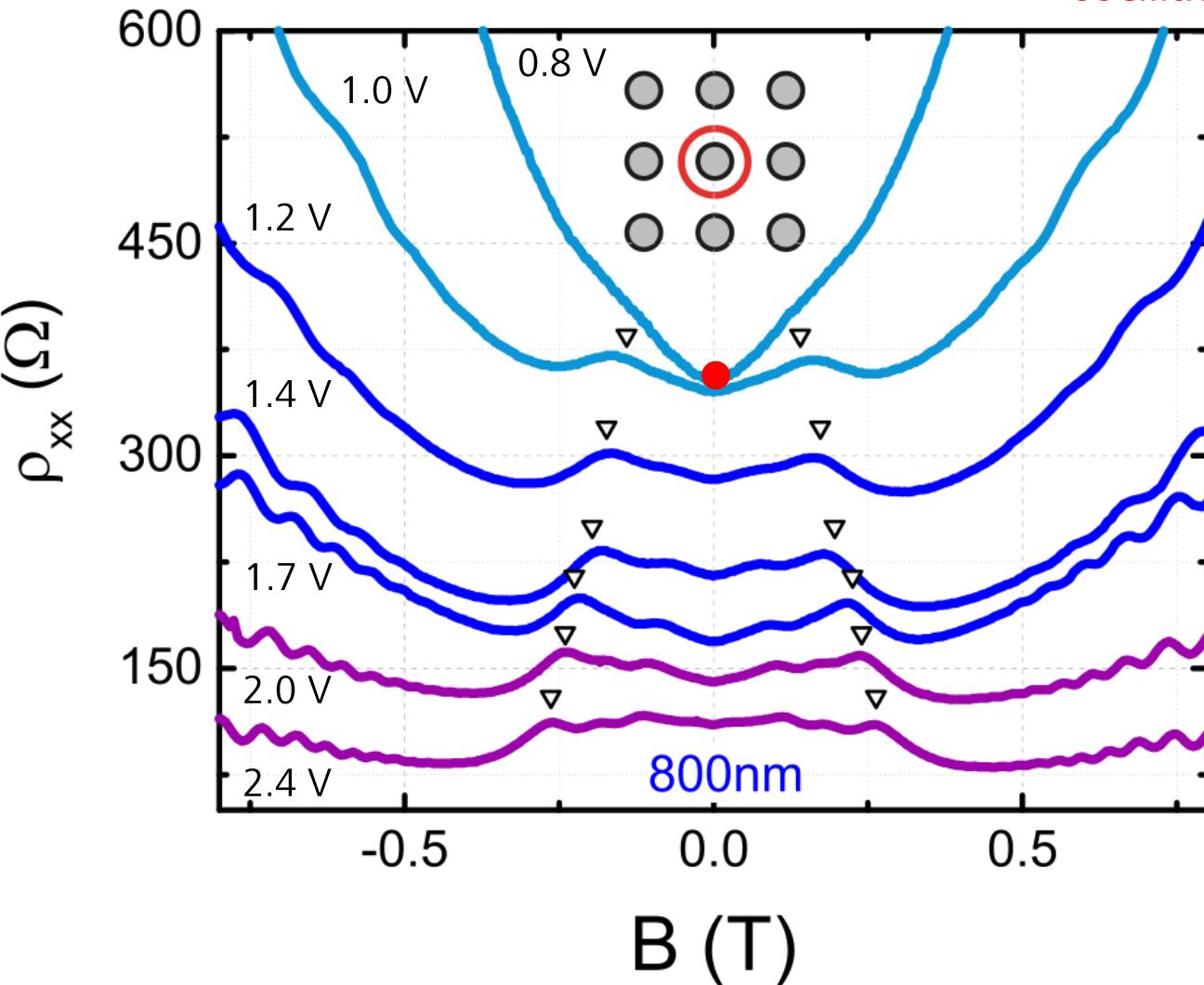


H. Maier et al.  
*Nature Commun.* **8**,  
2023 (2017)

Peak positions calculated from:  $R_c = 0.5a$    $0.8a$    $1.14a$   ;  $R_c = \frac{\hbar\sqrt{4\pi n_s}}{eB}$

# Antidot resonances – $n_s$ dependence

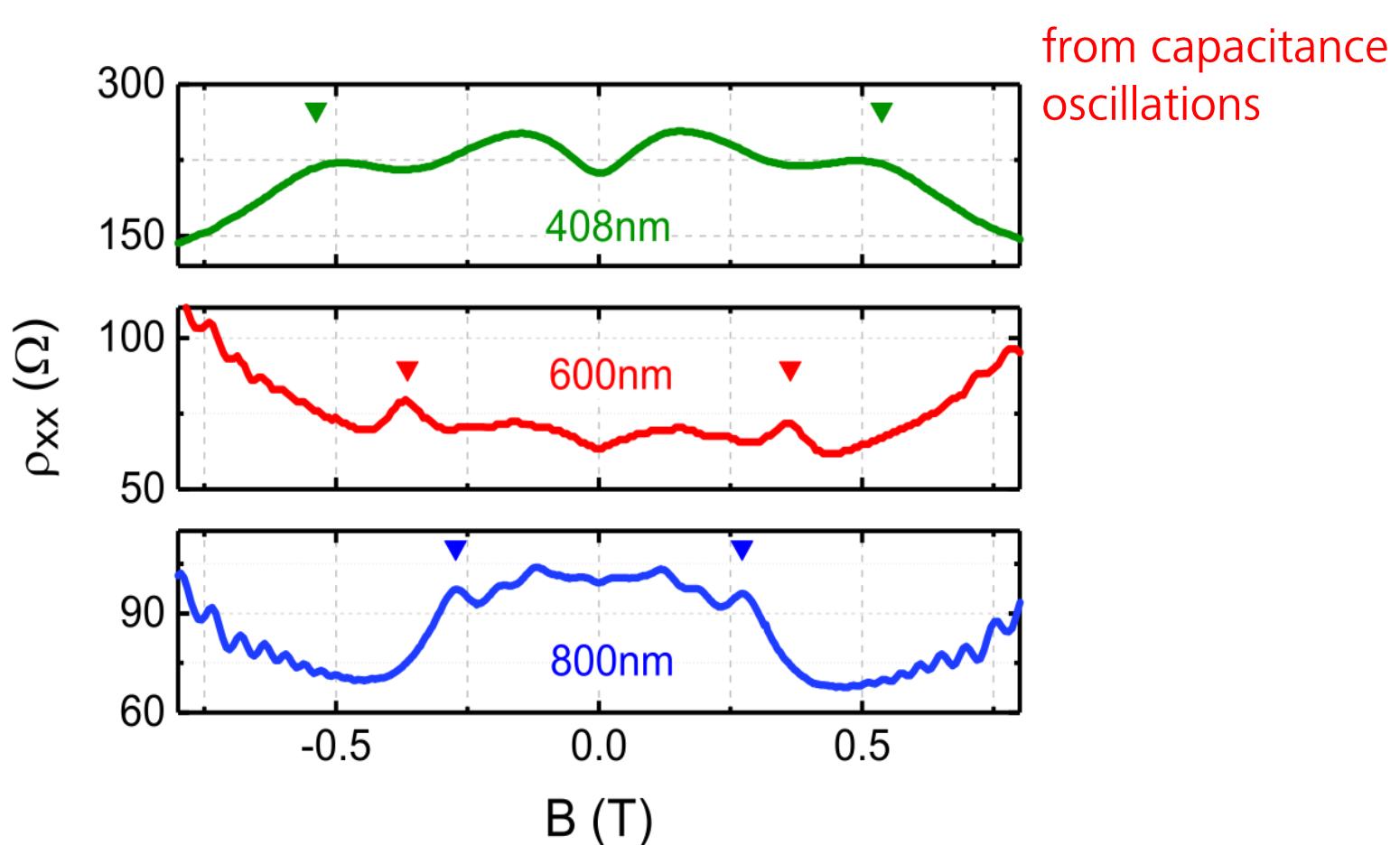
↑ from capacitance oscillations



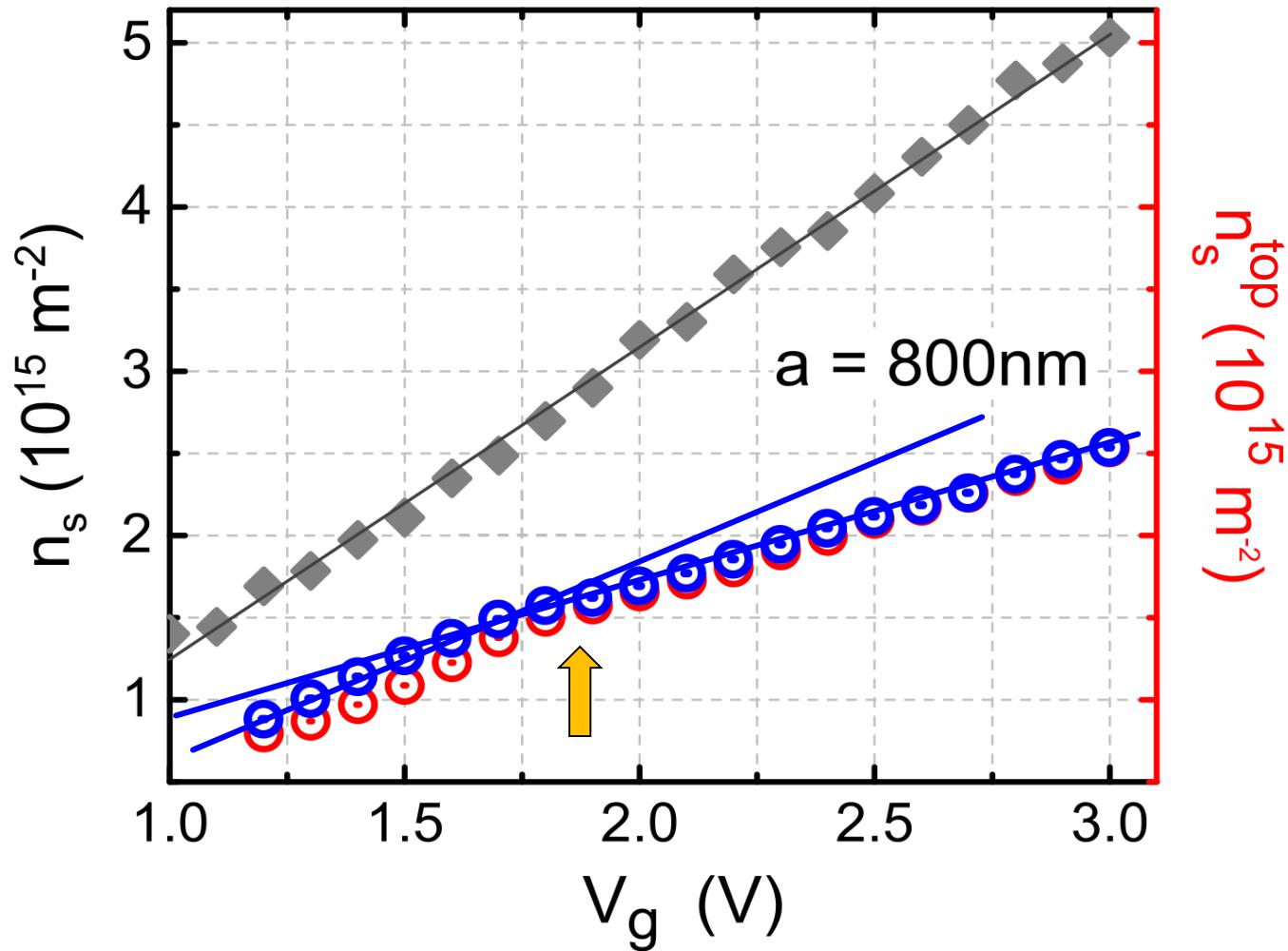
▽  $2R_c = a$   
(calculated)

# Antidot resonances – ‘a’ dependence

Arrow positions calculated from:  $R_c = 0.5a$   ;  $R_c = \frac{\hbar\sqrt{4\pi n_s}}{eB}$

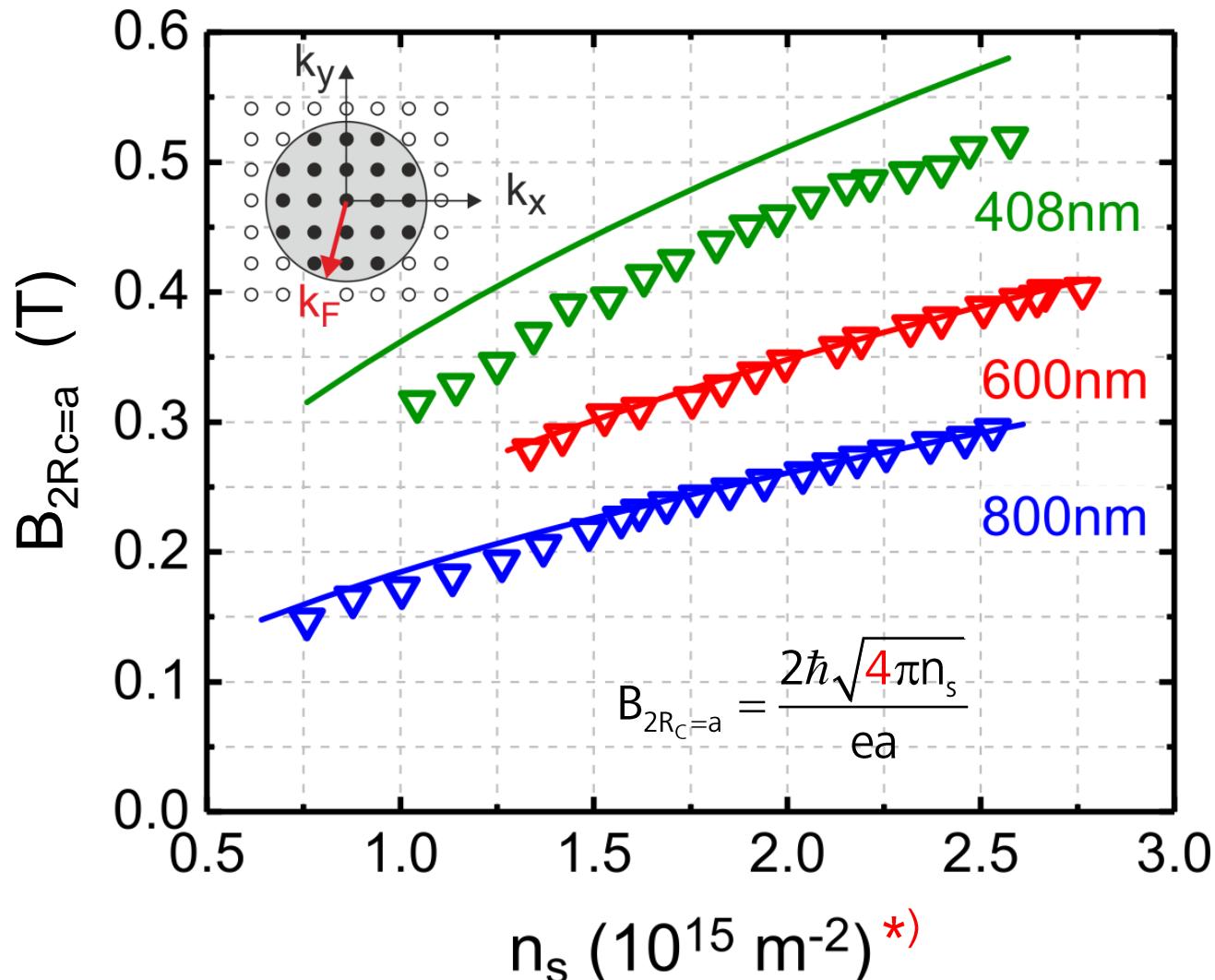


## Carrier density: from QHE ◆, antidot resonance ◎ and capacitance ○

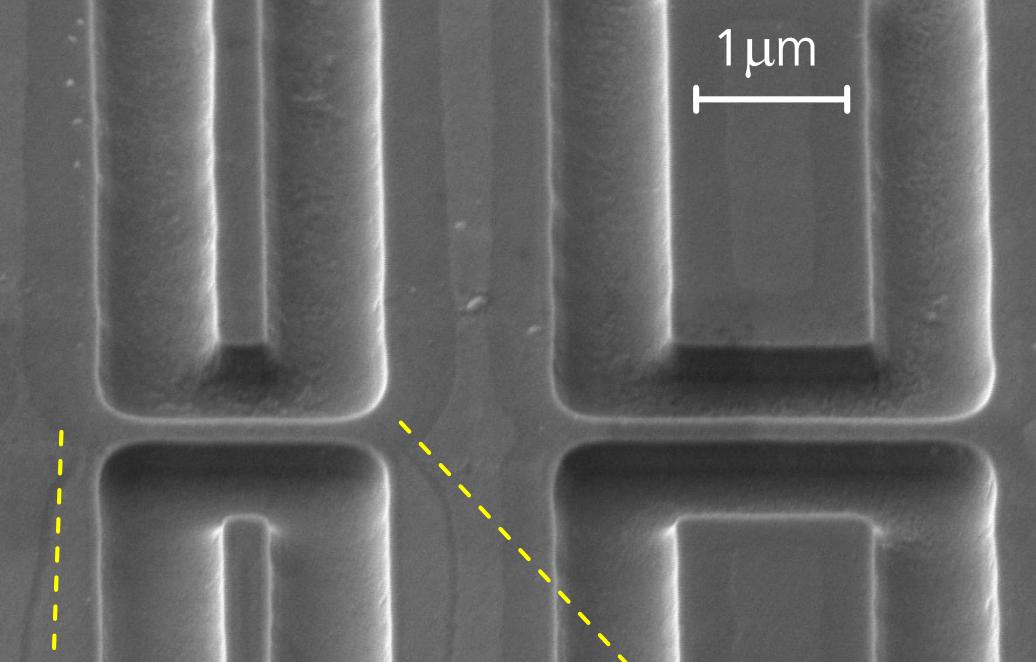


Both, antidot resonances and capacitance oscillations probe **single** TI surface

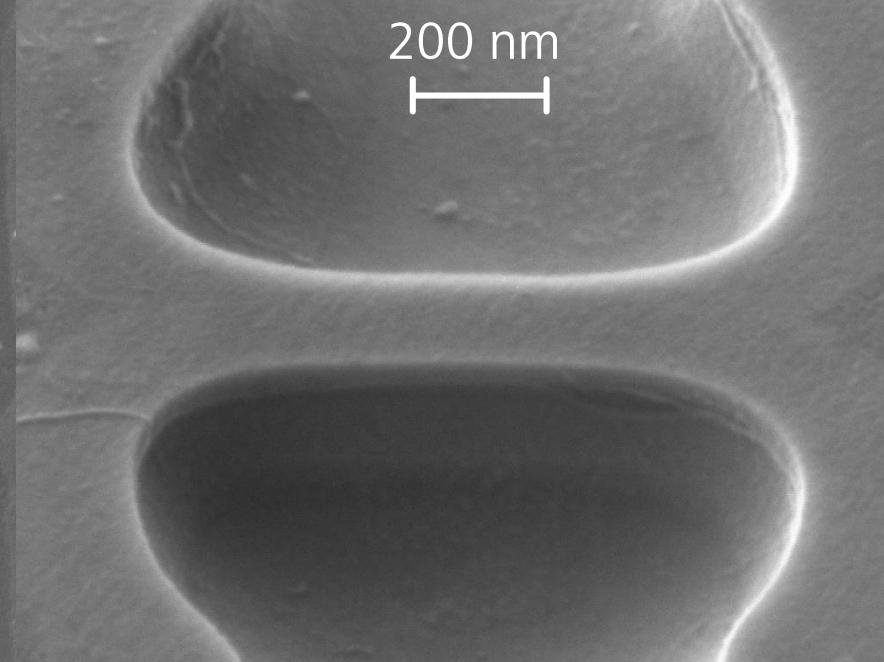
# Position of fundamental antidot resonance



<sup>\*)</sup> from C(B) oscillations H. Maier et al., *Nature Commun.* **8**, 2023 (2017)

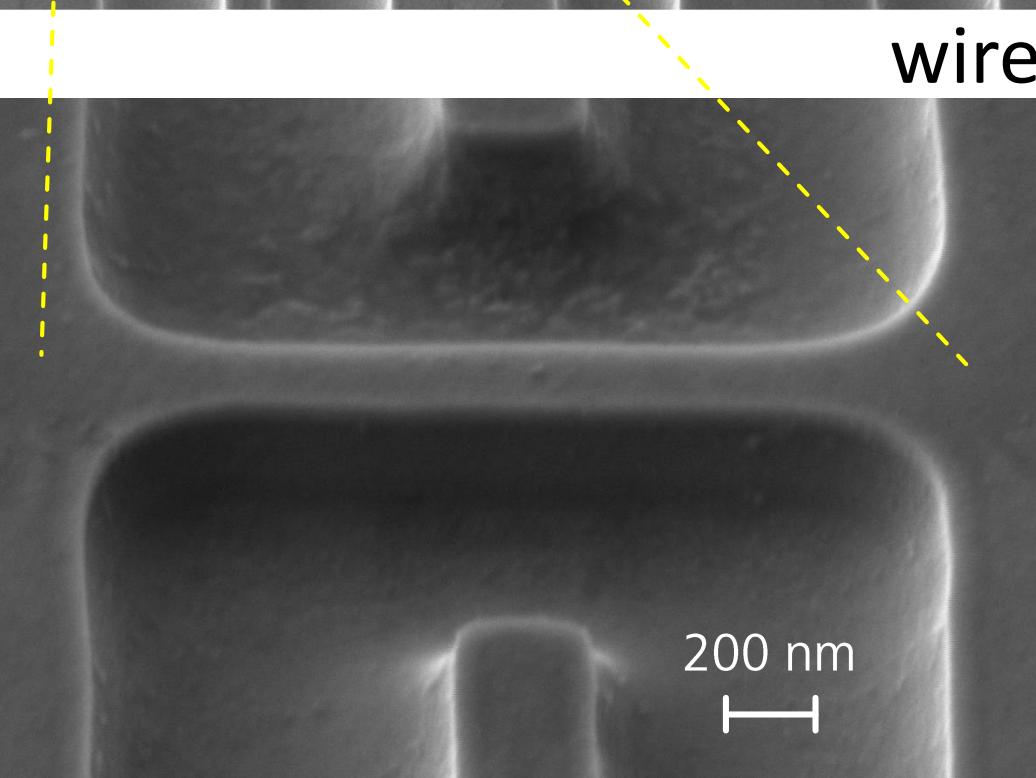


1  $\mu$ m

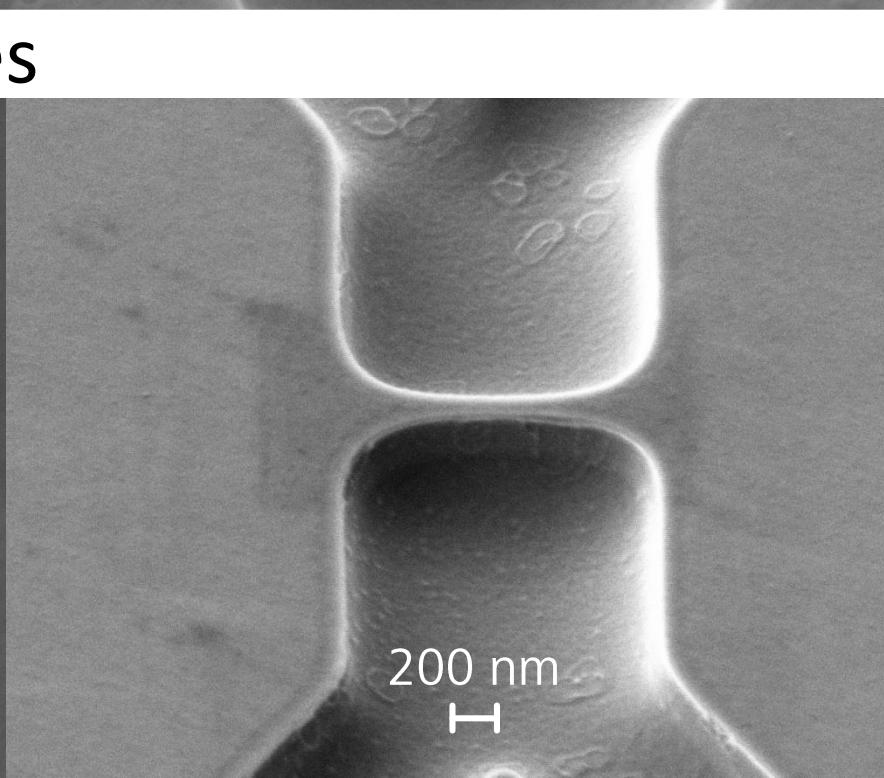


200 nm

wires



200 nm



200 nm

# Majorana fermions (artists view)



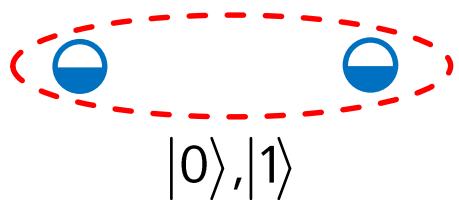
## Majorana bound states (MBS)

A Majorana quasi-particle is a superposition of an electron (particle) and a hole (antiparticle)



Two majorana bound states form one fermion (electron, hole)

Majorana bound states come in pairs – if spatially separated they are topologically protected → qubit

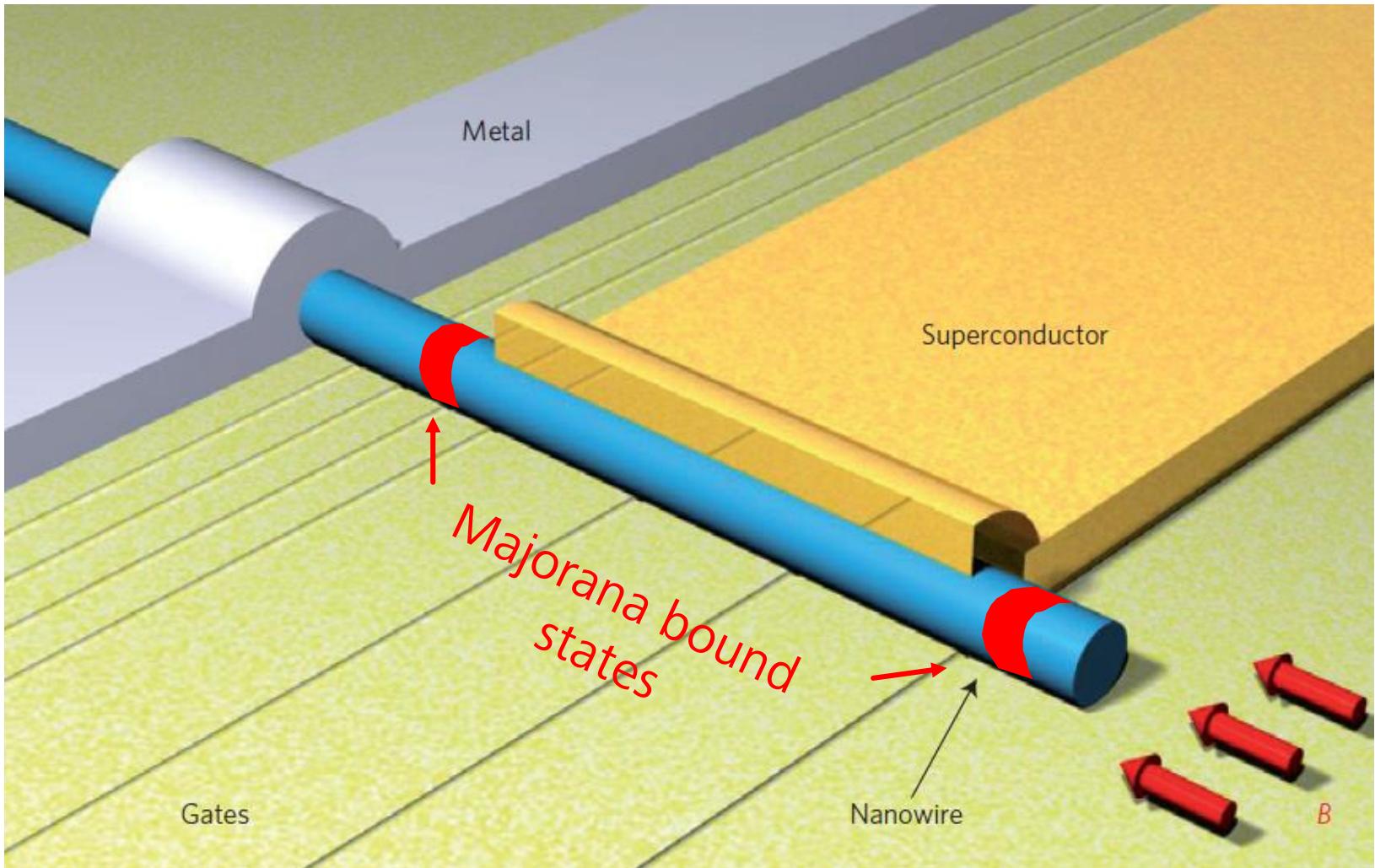


Fermion encoded in a *non-local* way:  
protected from local perturbation

Suitable system to look for MBS: proximity induced superconductors in semiconductors and TI wires.

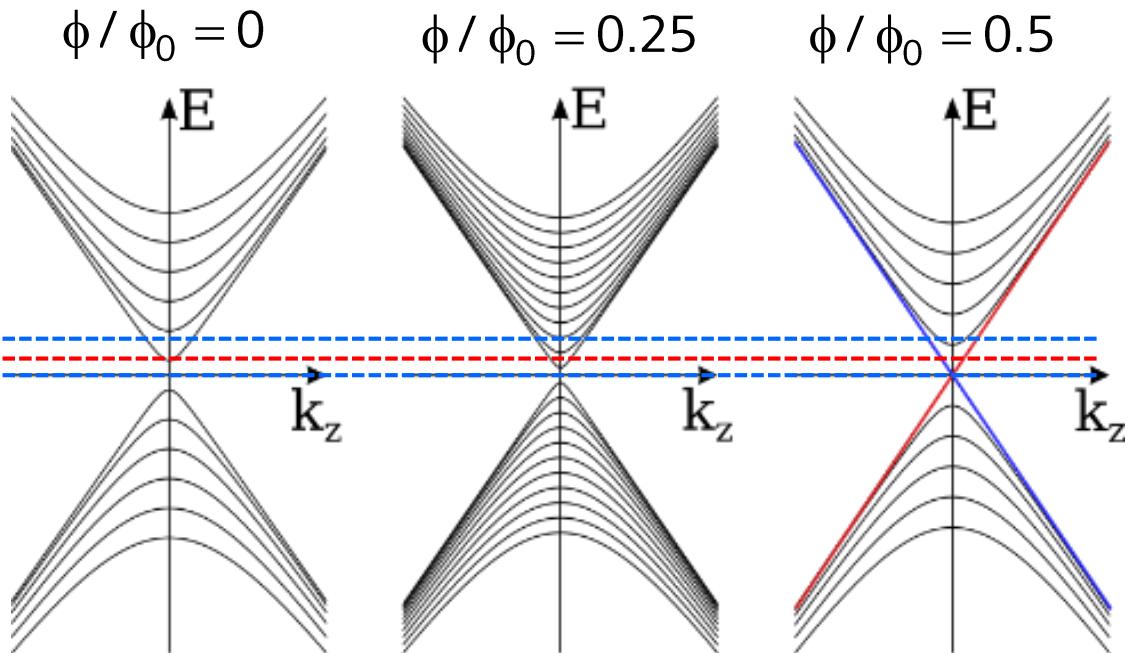
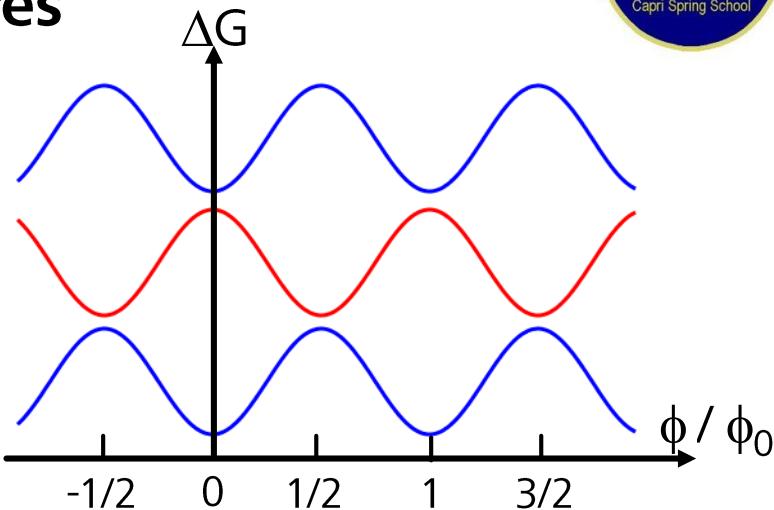
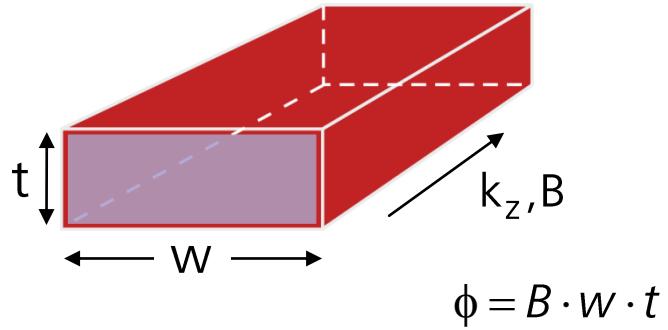
So far signatures of MBS in semiconductor nanowires but existence of MBS not yet unambiguously shown.

# TI wires for probing Majorana bound states



M. Franz, Nature Nano. **8**, 149 (2013)  
A. Cook, M. Franz, PRB **84**, 201105(R) (2011)

# Bandstructure of TI nanowires



Energy spectrum:

$$E = \pm \hbar v_F \sqrt{k_z^2 + k_\ell^2} \text{ with}$$

$$k_\ell = \Delta k_\ell \left( \ell + \frac{1}{2} - \frac{\phi}{\phi_0} \right)$$

$\in \mathbb{Z}$    Berry-phase   magnetic  
flux

$$\Delta k_\ell = 2\pi / P$$

$$P = \text{perimeter}$$

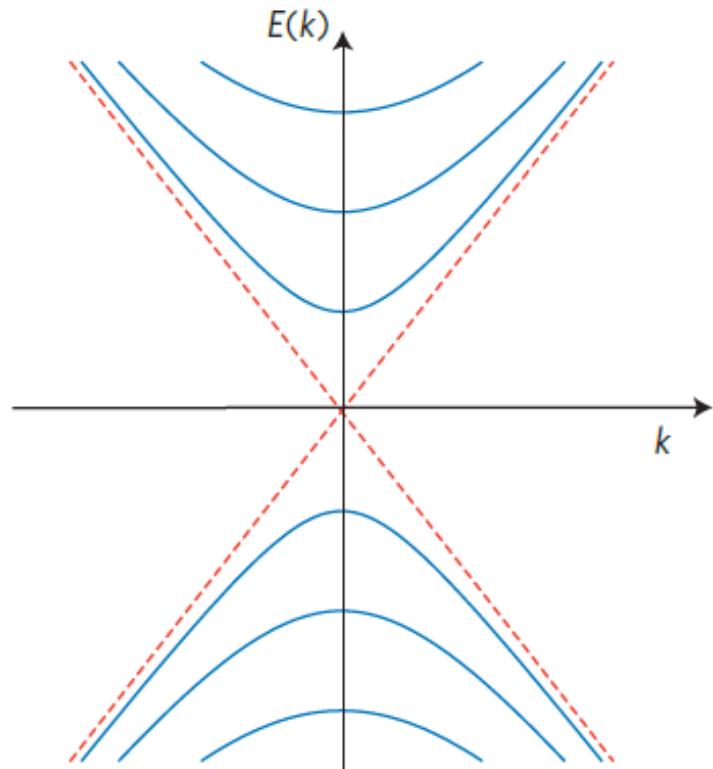
S. Cho et al., Nat. Commun. **6**, 7634 (2015)

L.A. Jauregui et al., Nat. Nanotech. **11**, 345 (2016)

Bardarson & Moore, PRL **105**, 156803 (2010)

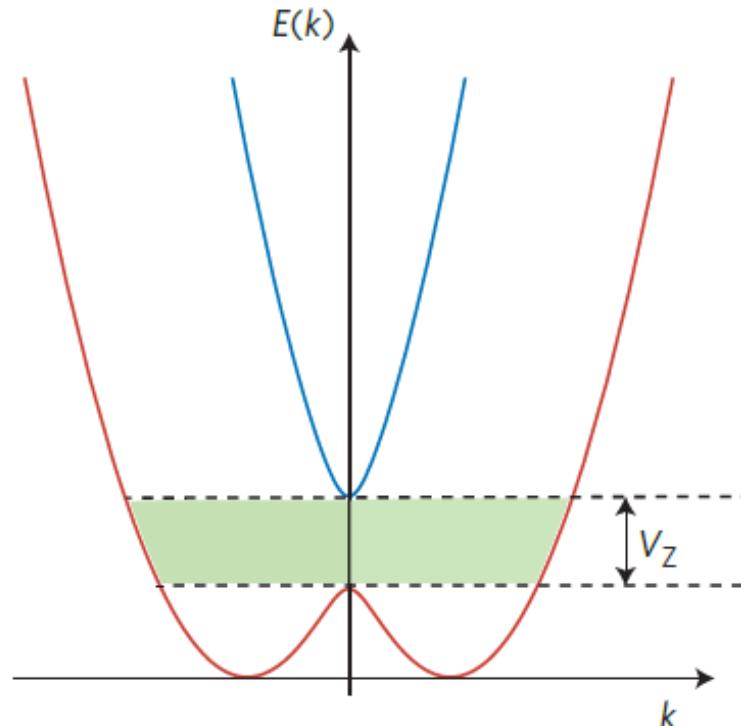
# Advantage of TI wires

TI wire:  $\phi / \phi_0 = 0.5$



Odd number of Fermi points in the right half of the Brillouin zone everywhere in the bulk gap

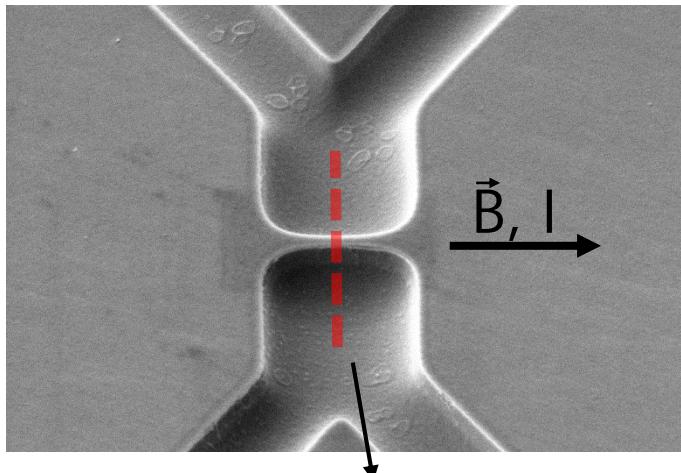
Wire with SO interaction:  $V_z$  tuned by **B**-field



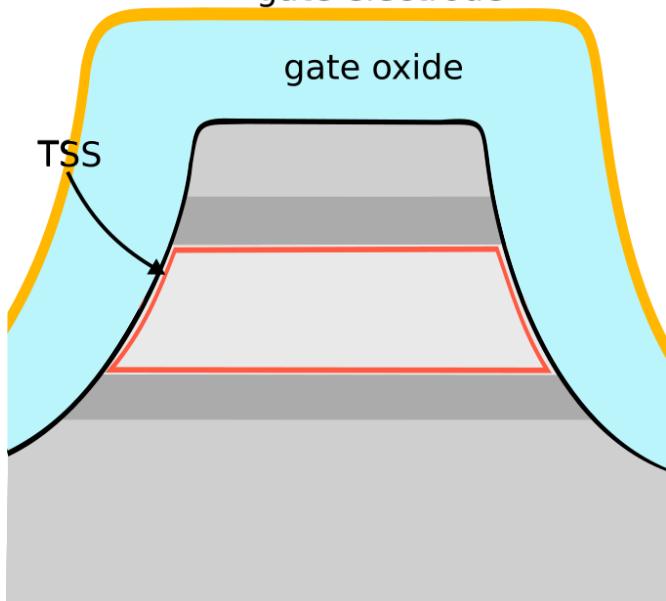
Condition for topological phase only fulfilled in gap (green)

# Nanowire devices

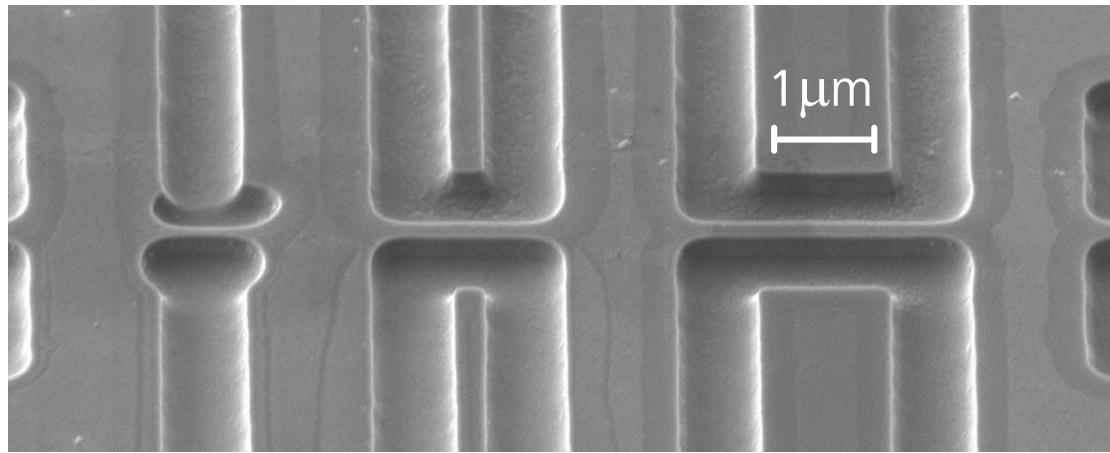
quasi 2-point



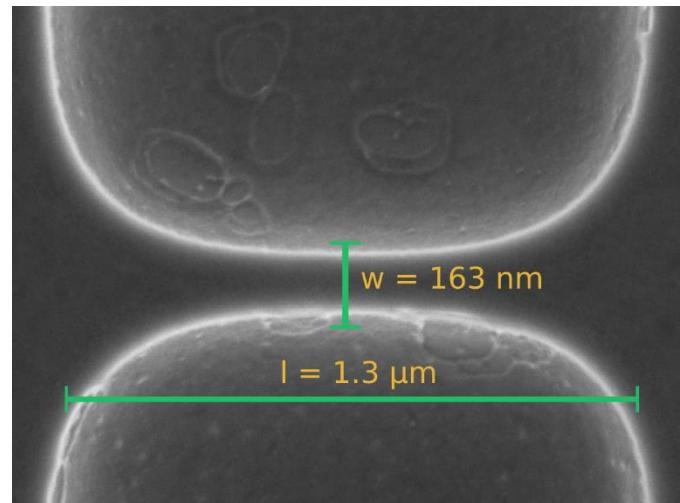
gate electrode



4-point

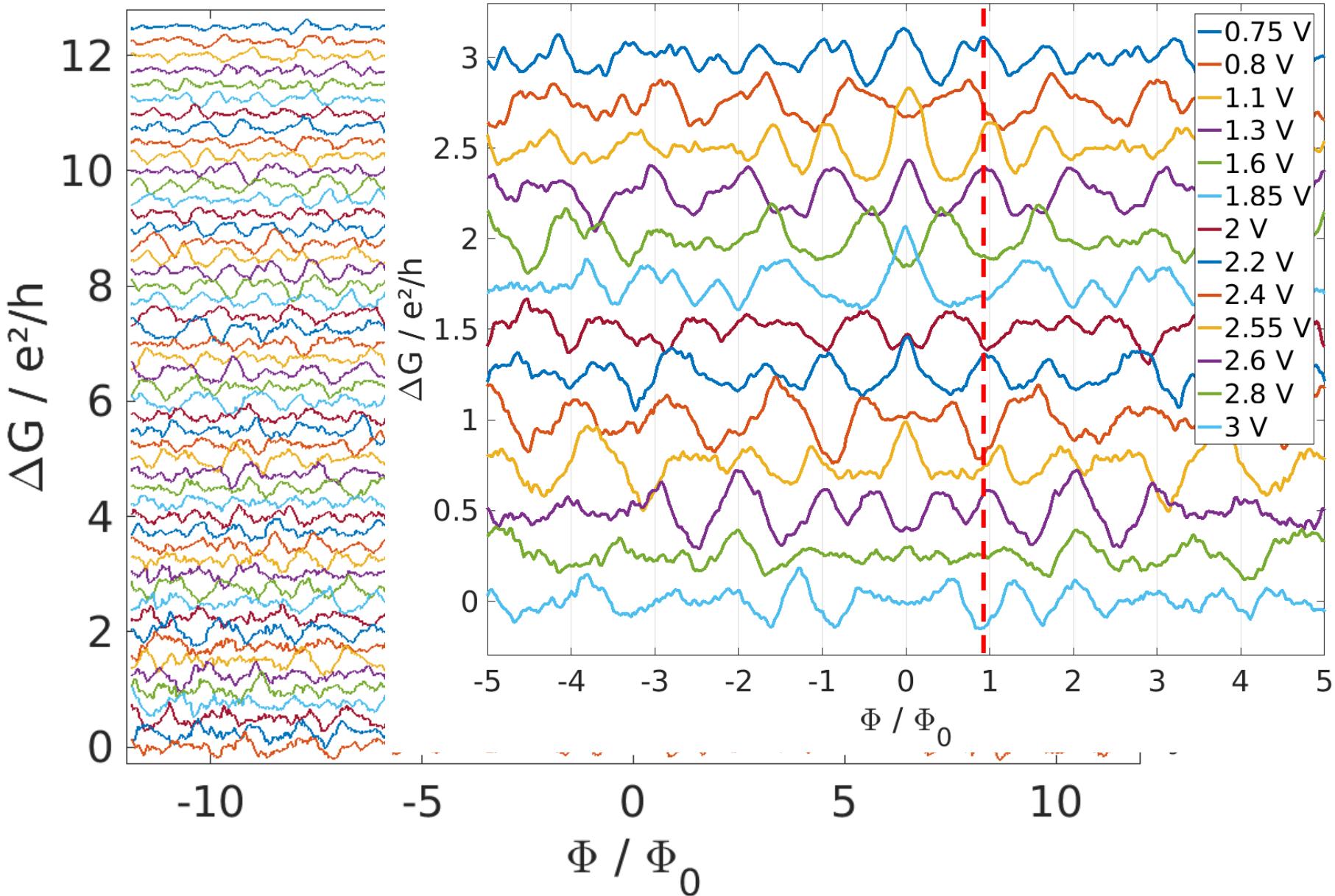


tilted view (50°)

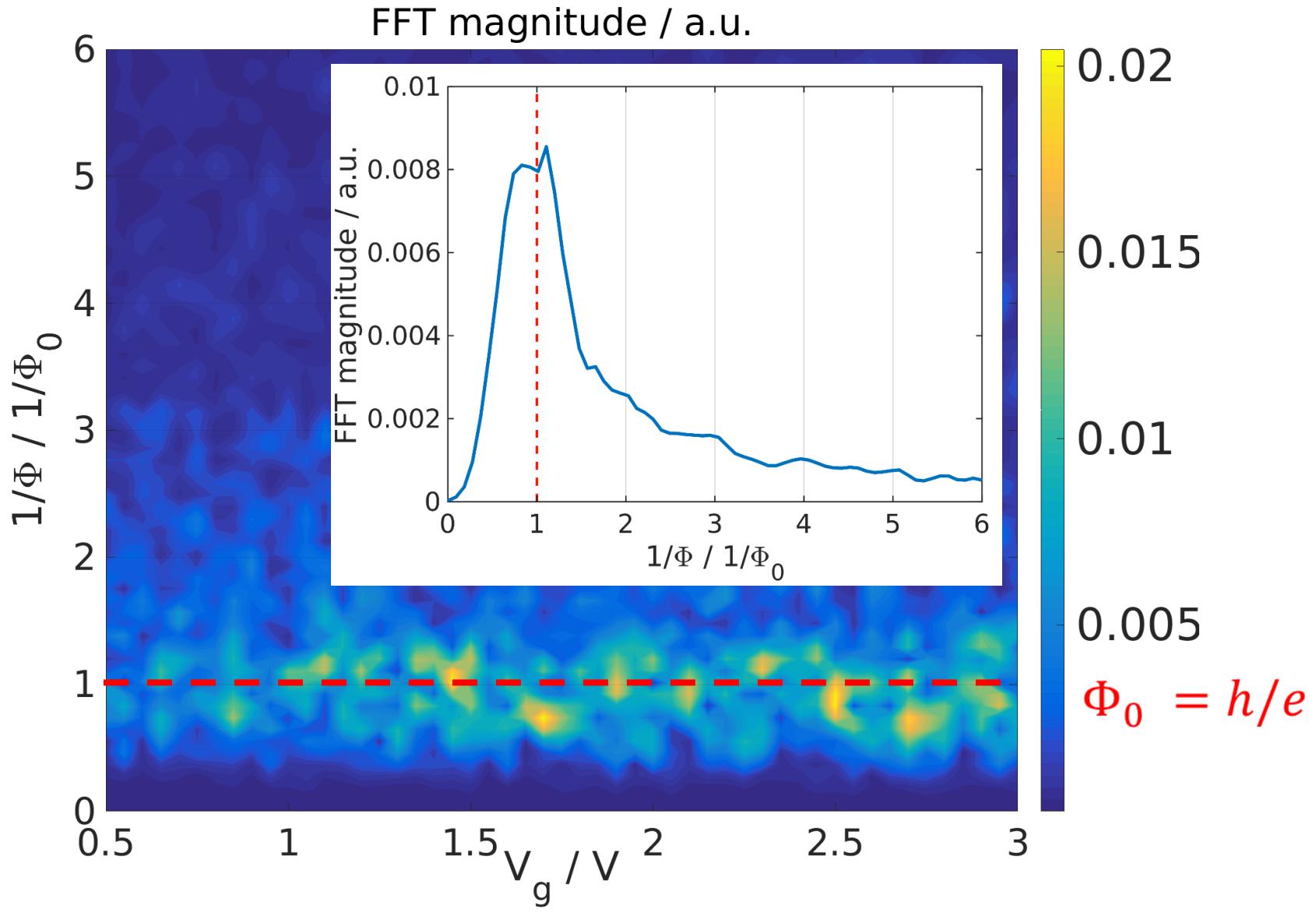


top view

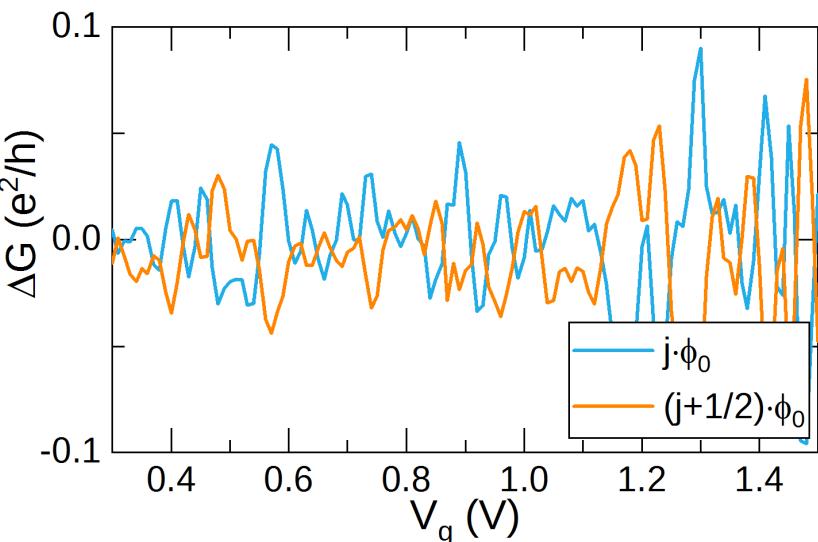
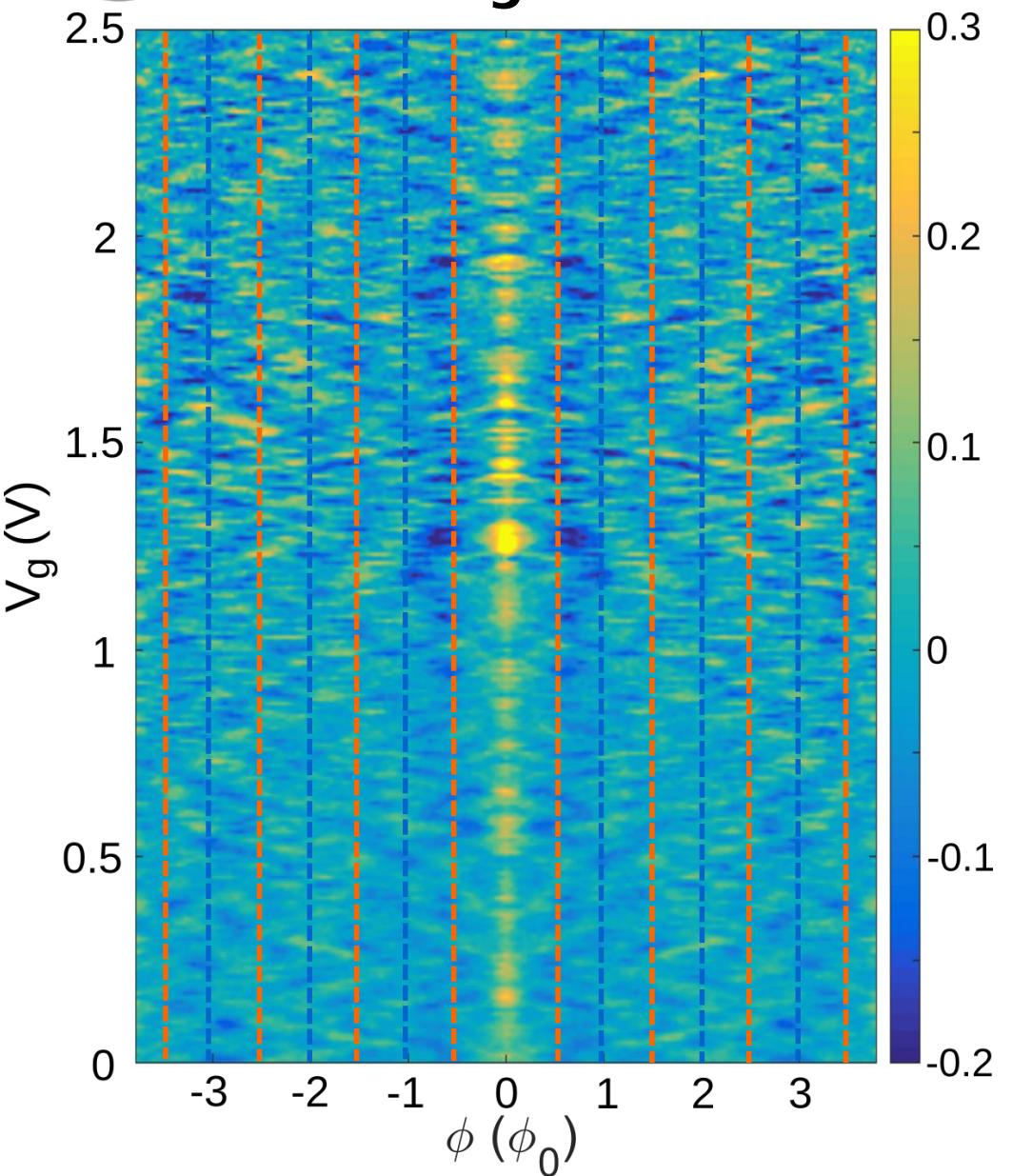
# Aharonov Bohm-type oscillations



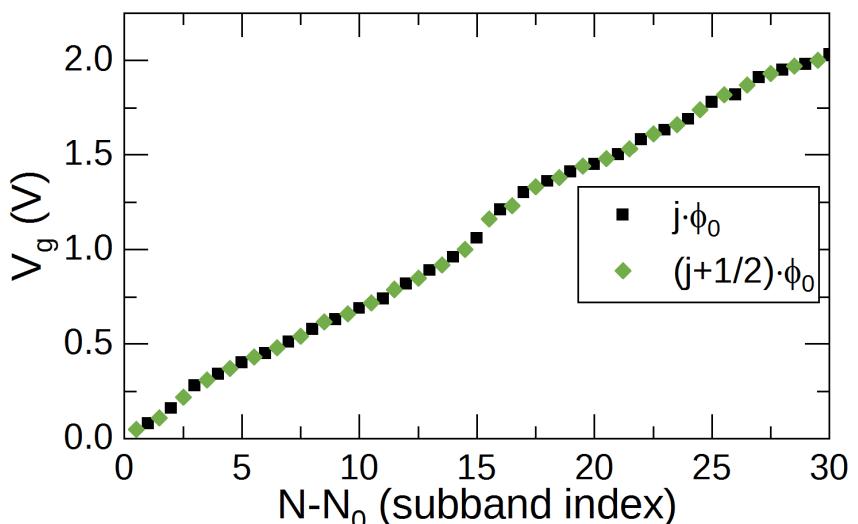
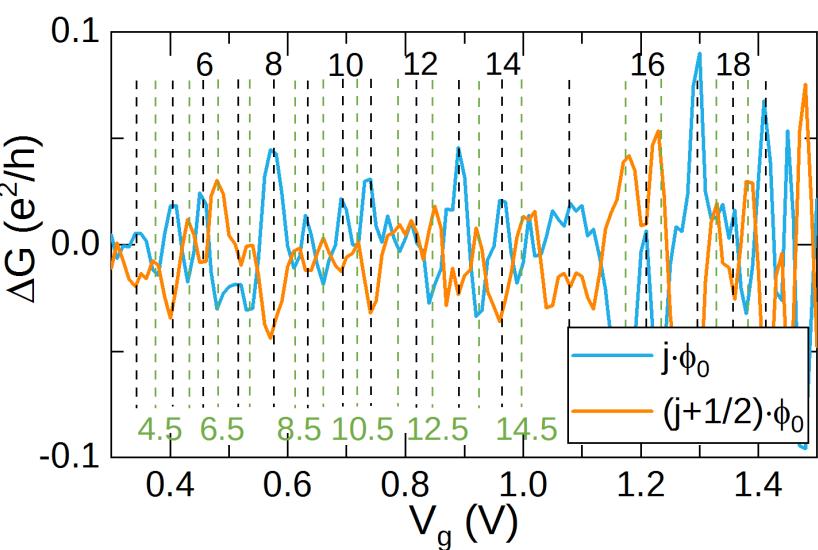
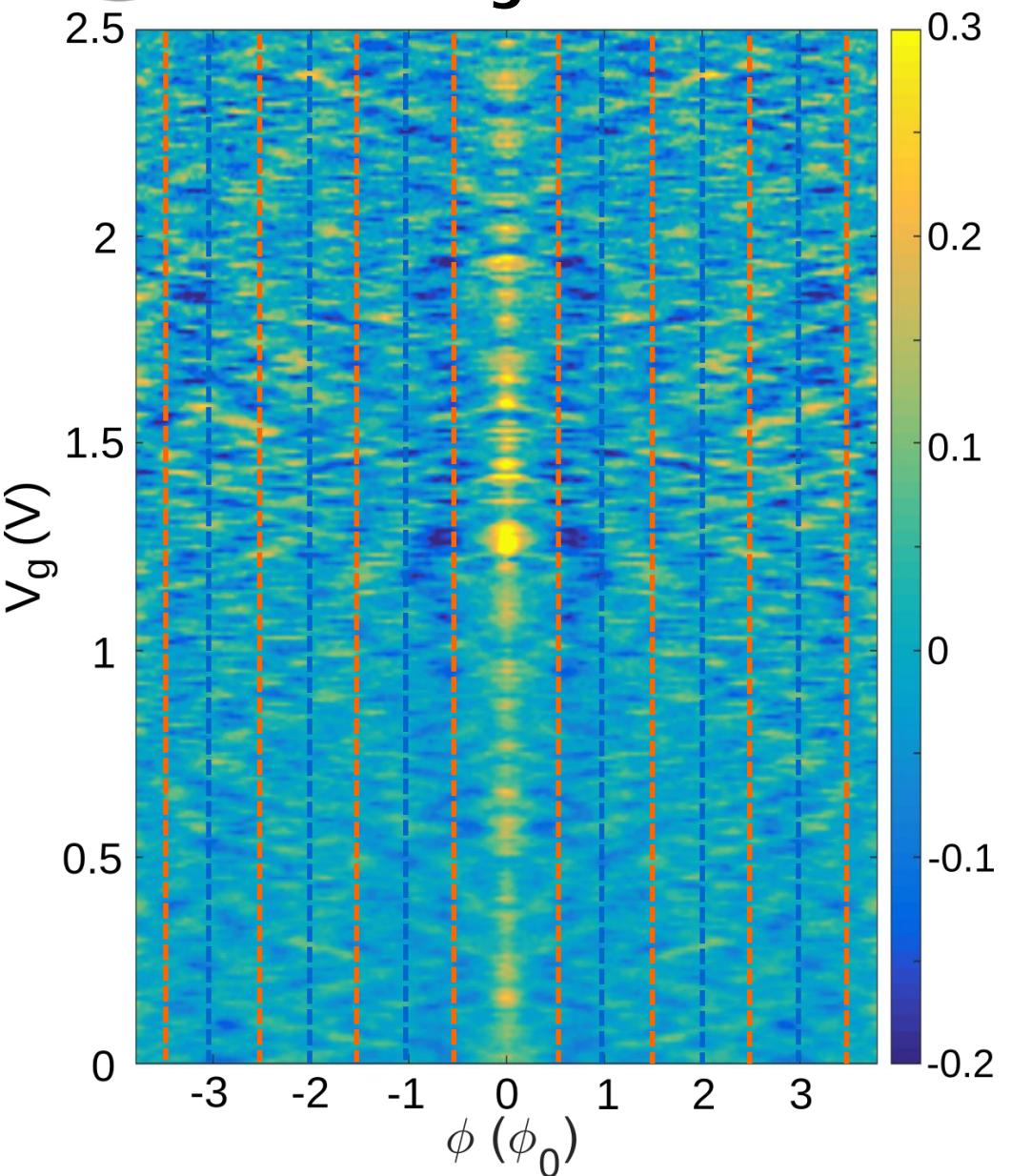
# Aharonov Bohm-type oscillations



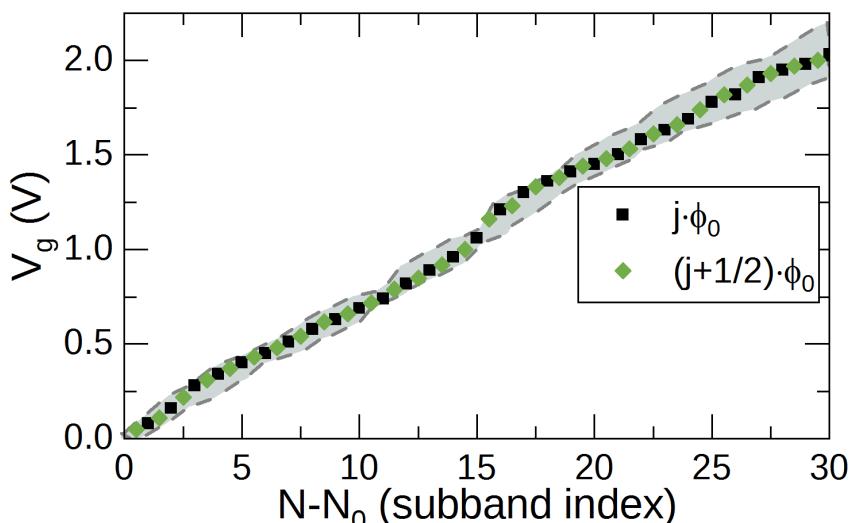
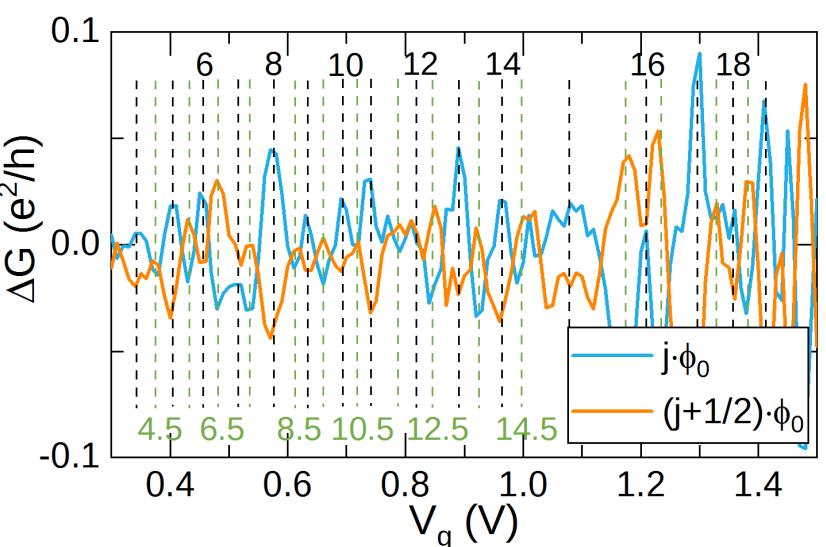
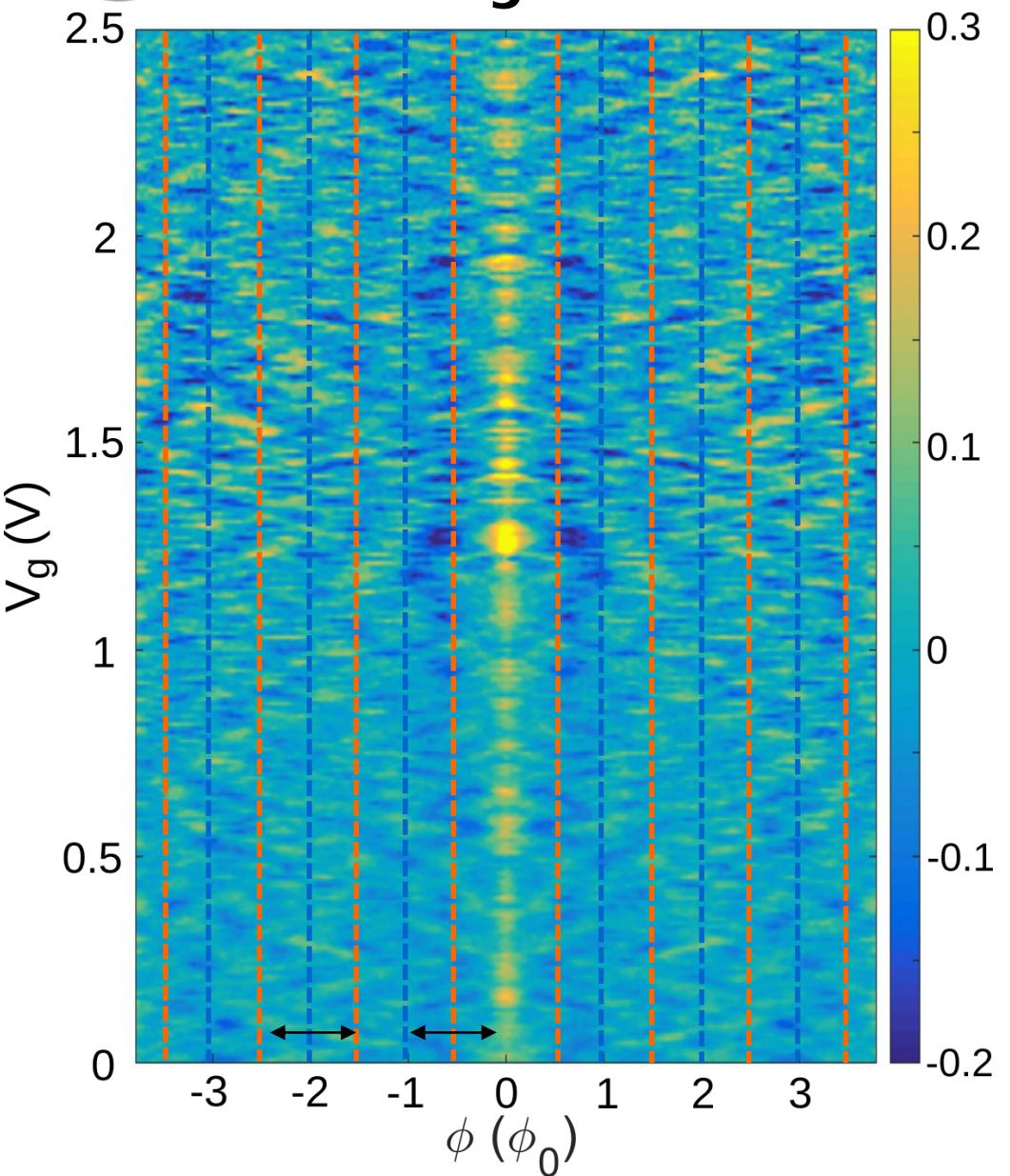
## Counting subbands



# Counting subbands

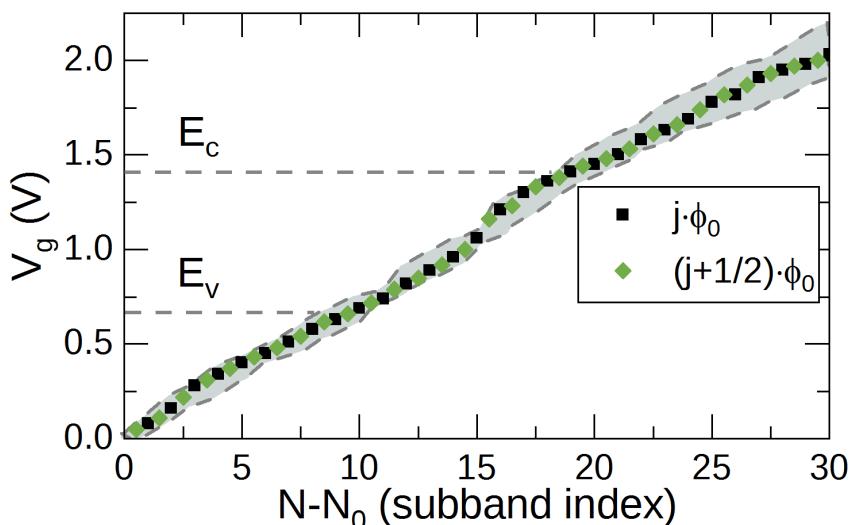
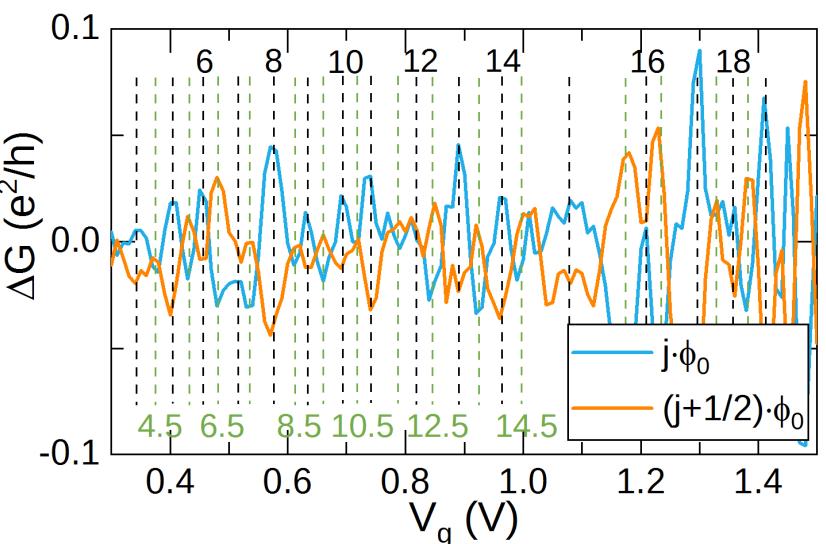
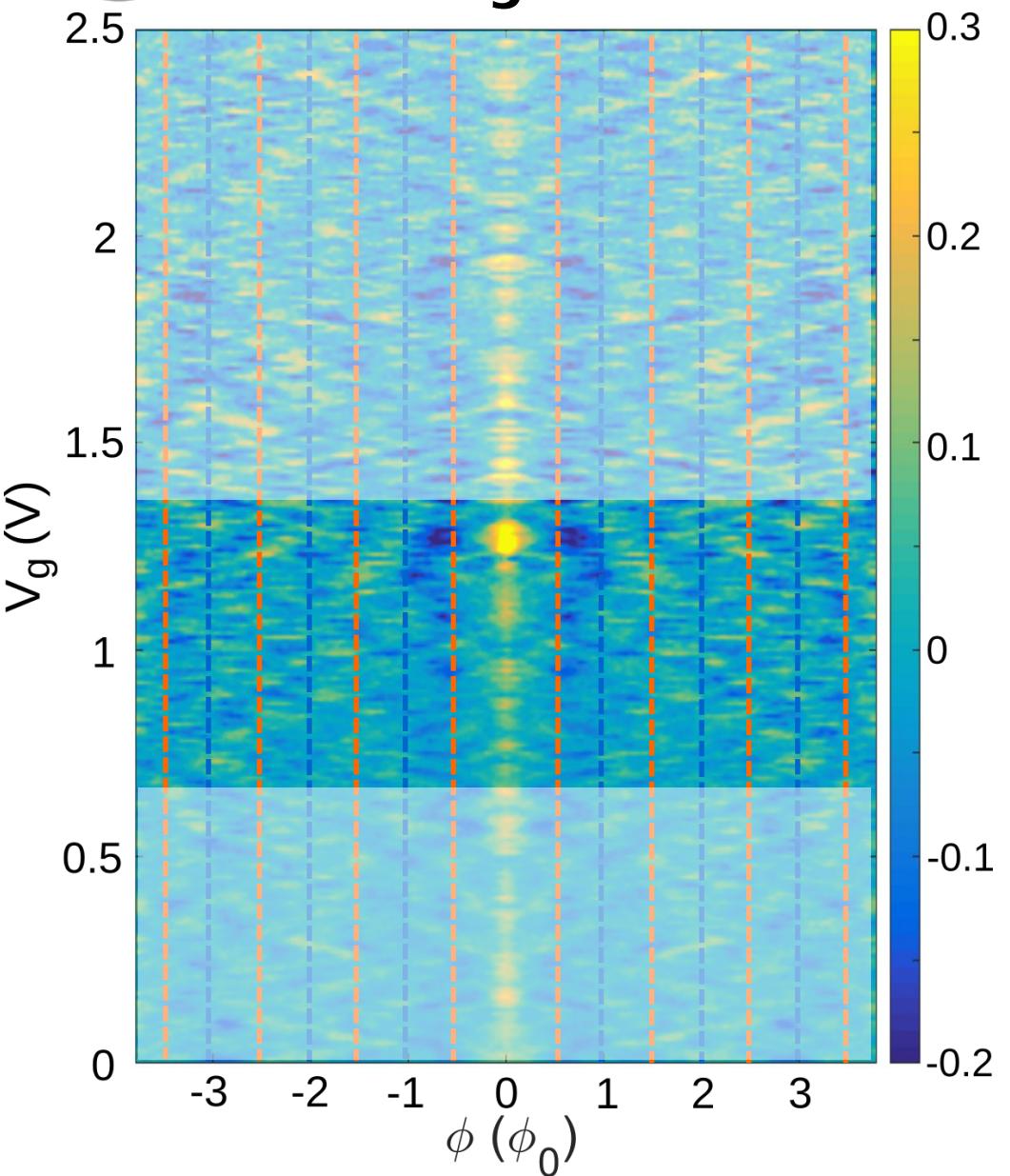


# Counting subbands



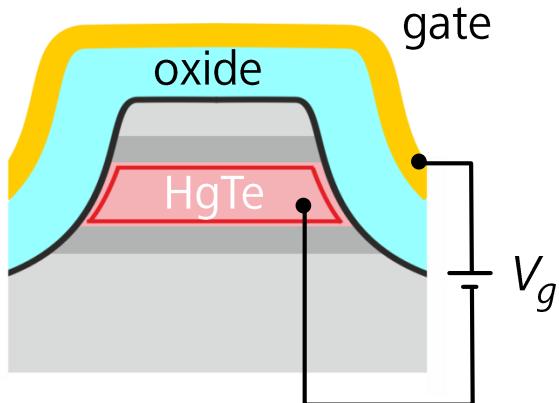


# Counting subbands



# UR Subband spacing: simple model

...relation between  $\Delta k$  and  $\Delta V$



$$n_s = \frac{k^2}{4\pi} ; \quad n_s = \frac{C}{e}(V_g - V_0) + n_0 ;$$

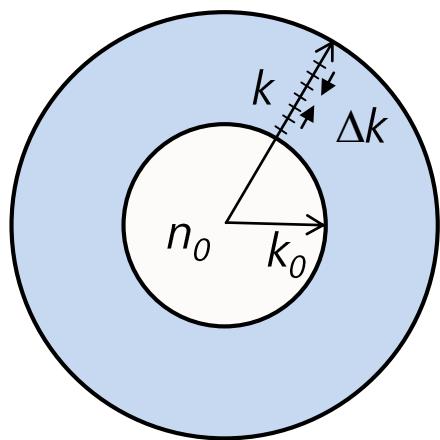
$$n_0 = \frac{k_0^2}{4\pi} = \text{electron density at } V_g = V_0$$

↑ helical Dirac electrons

Fermi wave vector at conductance minimum (= subband opening):

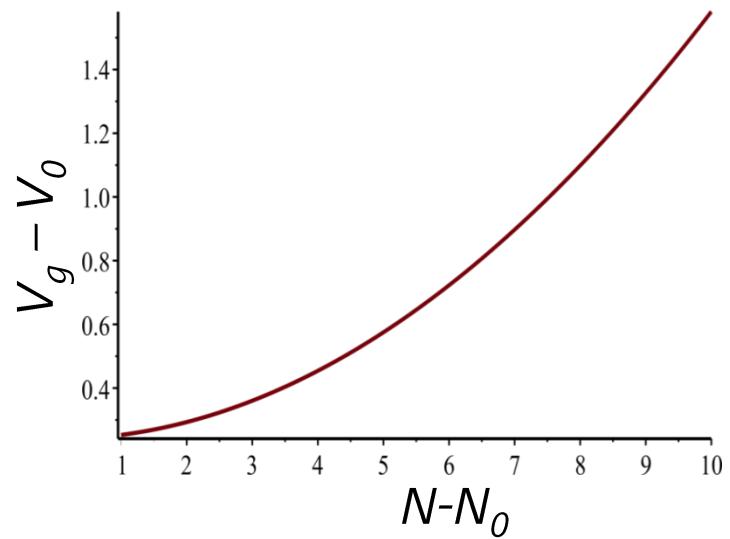
$$k_F = k_0 + (N - N_0)\Delta k$$

$$N - N_0 = 1, 2, 3, \dots$$



$$V_g - V_0 = \frac{e}{4\pi C} (2k_0(N - N_0)\Delta k_\ell + (N - N_0)^2 \Delta k_\ell^2)$$

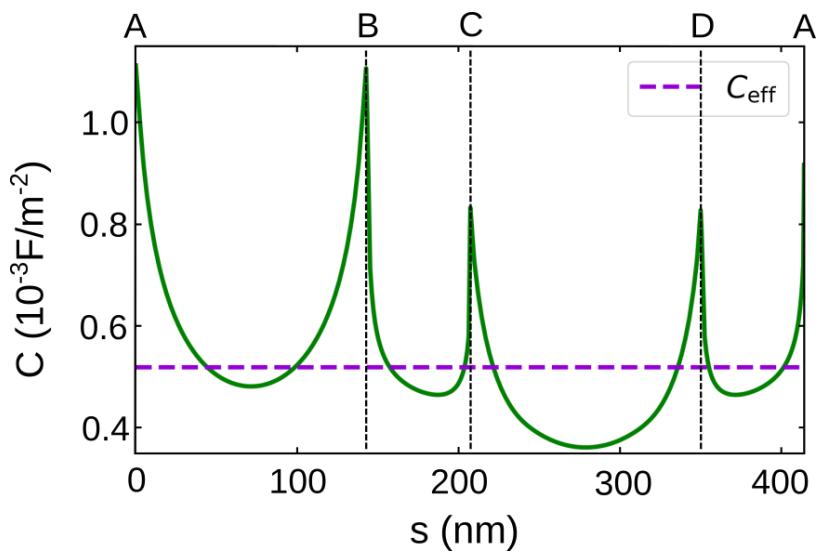
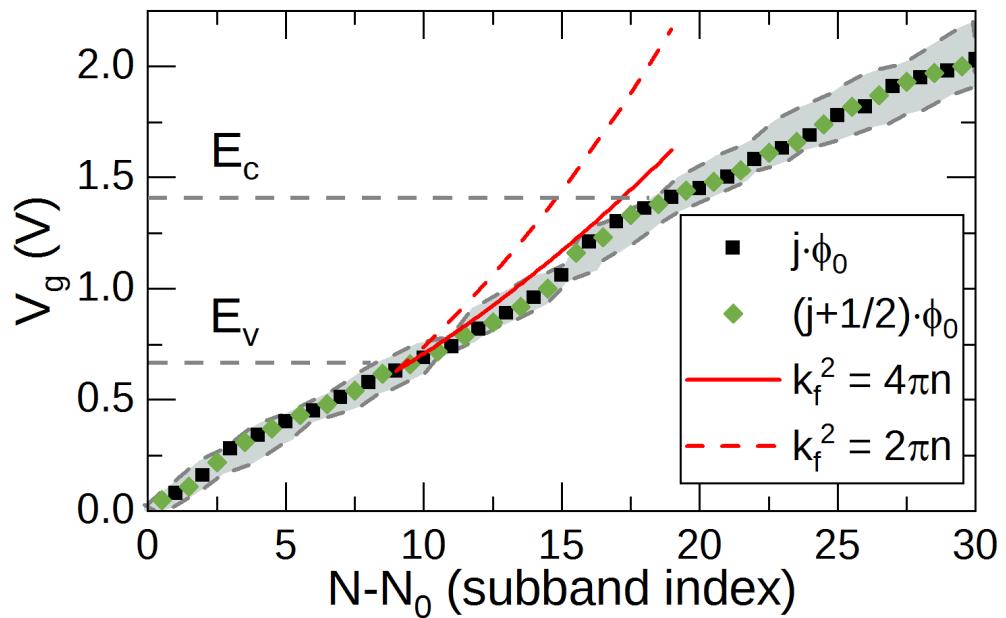
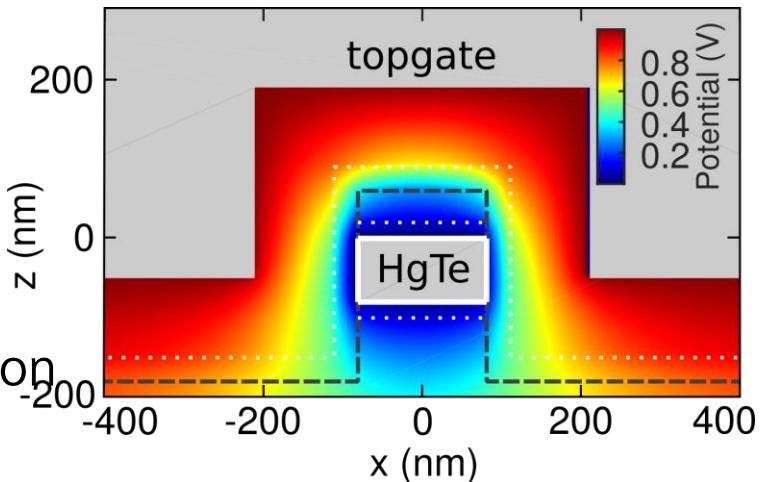
determined by  $C$  and  $\Delta k_\ell = 2\pi / P$



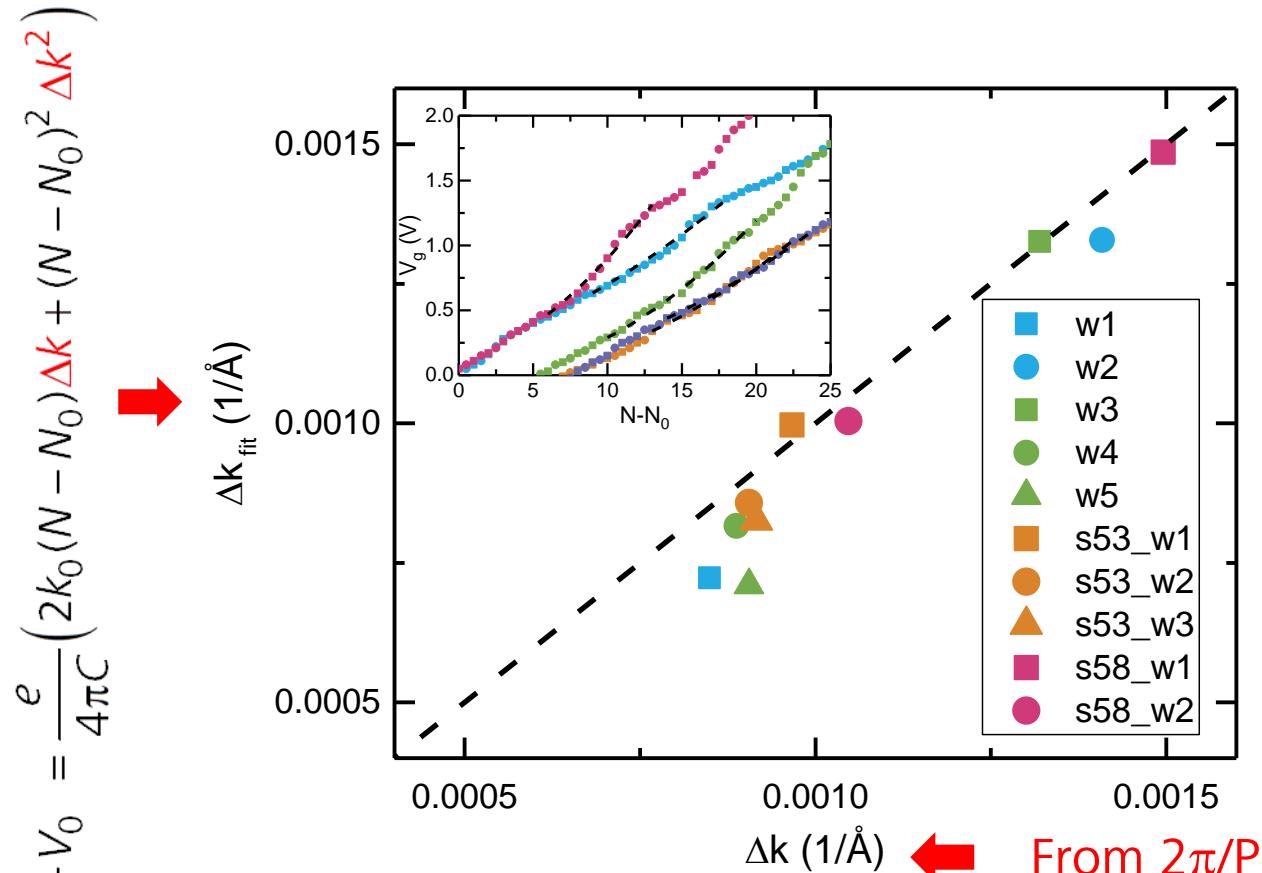
# Electrostatic model

$$V_g - V_0 = \frac{e}{4\pi C} \left( 2k_0(N - N_0) \Delta k + (N - N_0)^2 \Delta k^2 \right)$$

Numeric solution of Laplace equation



# Validity check (with 10 nanowires)



Subband structure: experimentally confirmed



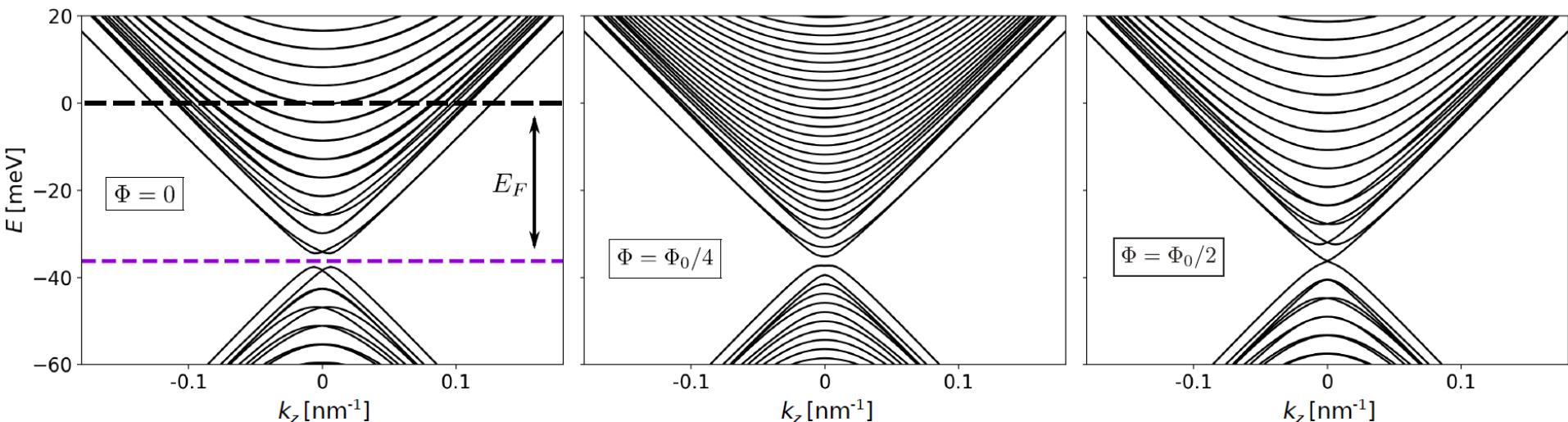
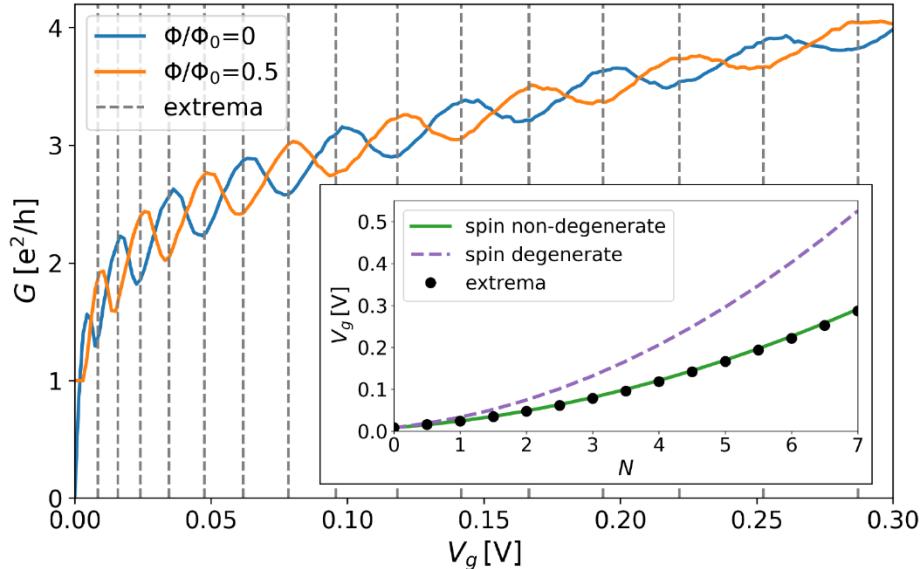
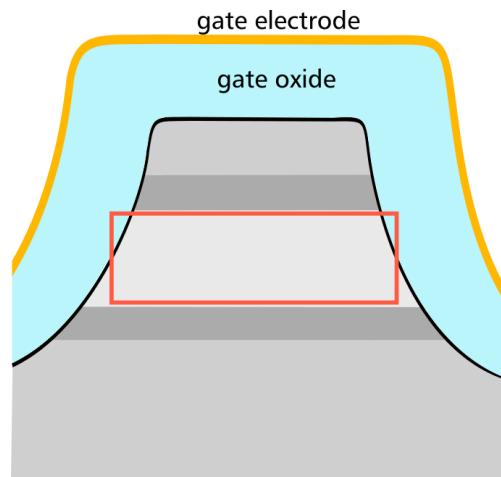
Topological nature of surface states confirmed



Existence of perfectly transmitted mode



# Full capacitance model (transport calculation using Kwant)





## Summary

- Antidot peak position probes  $k_F$  of top surface and confirms topological nature of surface states
- HgTe nanowires show  $h/e$  periodic quantum oscillations
- Anti-phase oscillations observed as function of  $V_g$  – but only quantitative correct description of  $V_g$ - $N$  relation confirms topological origin
- Indirect proof that perfectly transmitted mode can be switched on and off by half flux quantum



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