

Topologically protected states at domain walls in bilayer graphene

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MINISTERIO
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What are the domain walls in bilayer graphene?

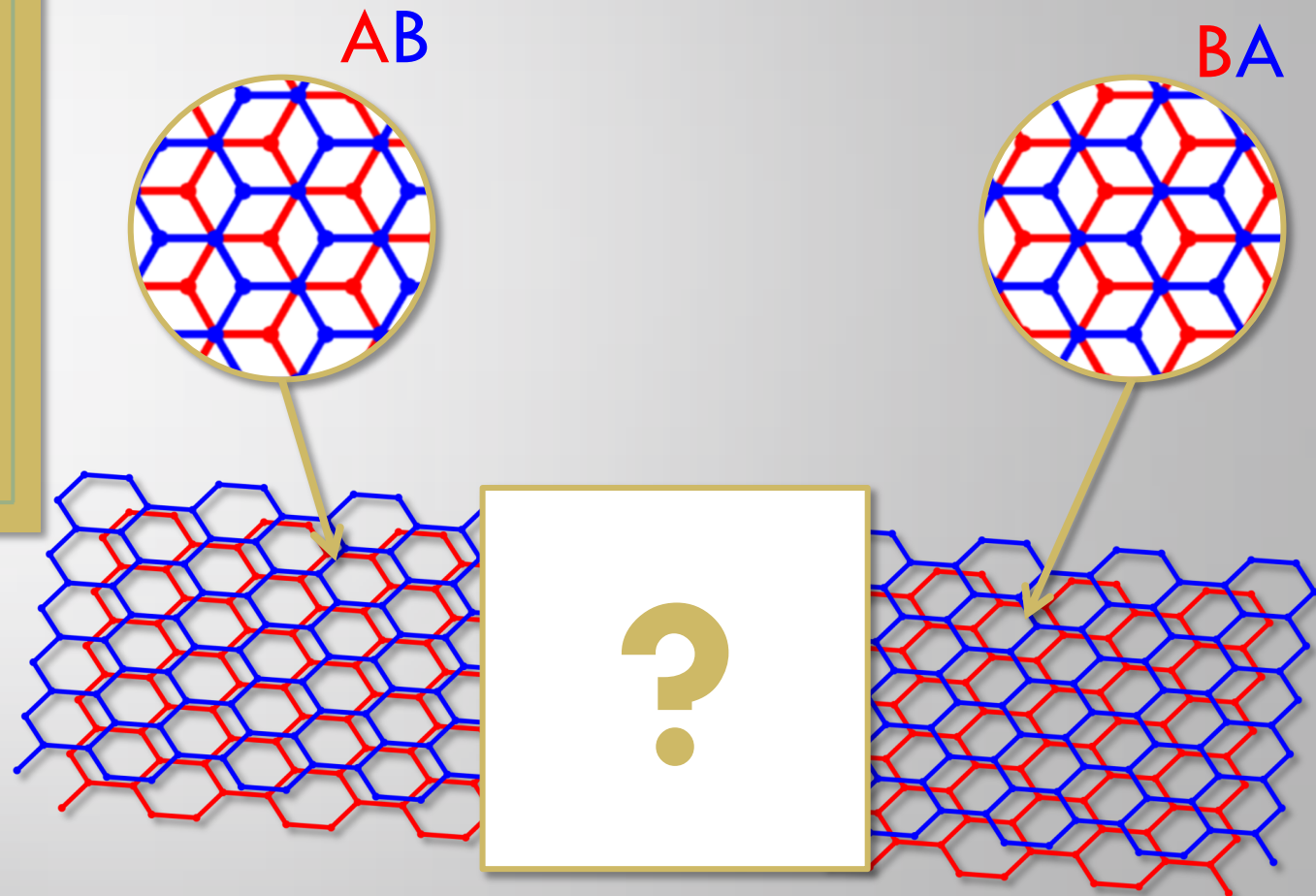
Boundaries
between regions
with different
properties

Magnetic moments

Gate voltage sign

★ Stacking

etc.



Why do we investigate domain walls in graphene?

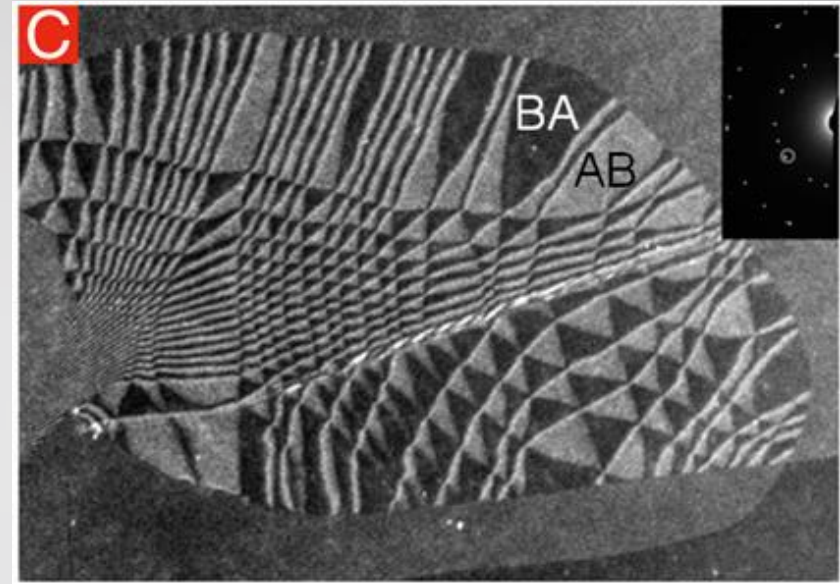
- **occur**

spontaneously
intentionally

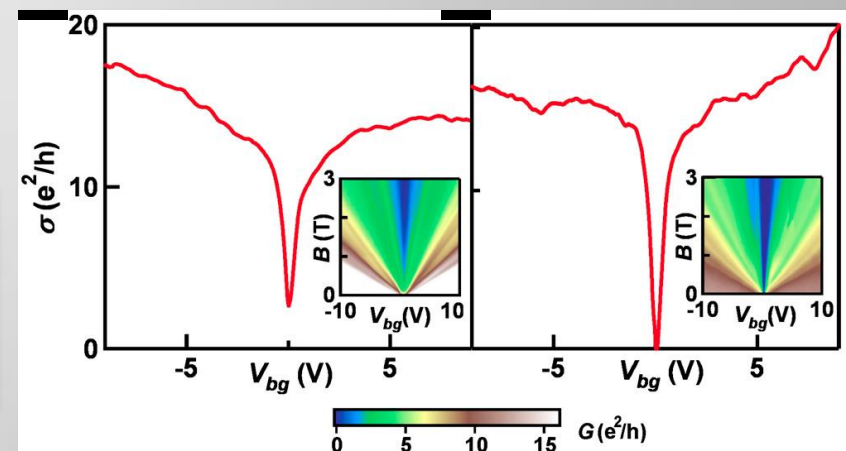
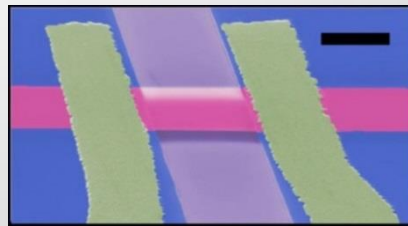
- **affect transport**

no conductance between
the domains
domain wall – conducting
channel

*Aberration-corrected
annular dark-field
STEM*



*Suspended double-
gated BL graphene*



Alden – PNAS (2013)

Bao – PNAS (2012)

Two terminal differential conductivity vs. back-gate voltage

Why do we investigate domain walls in graphene?

- occur

spontaneously
intentionally

- affect transport

no conductance between
the domains
domain wall – conducting
channel

*Dual-gated field effect
transistor devices on BLG with
AB-BA domain walls (green line)*

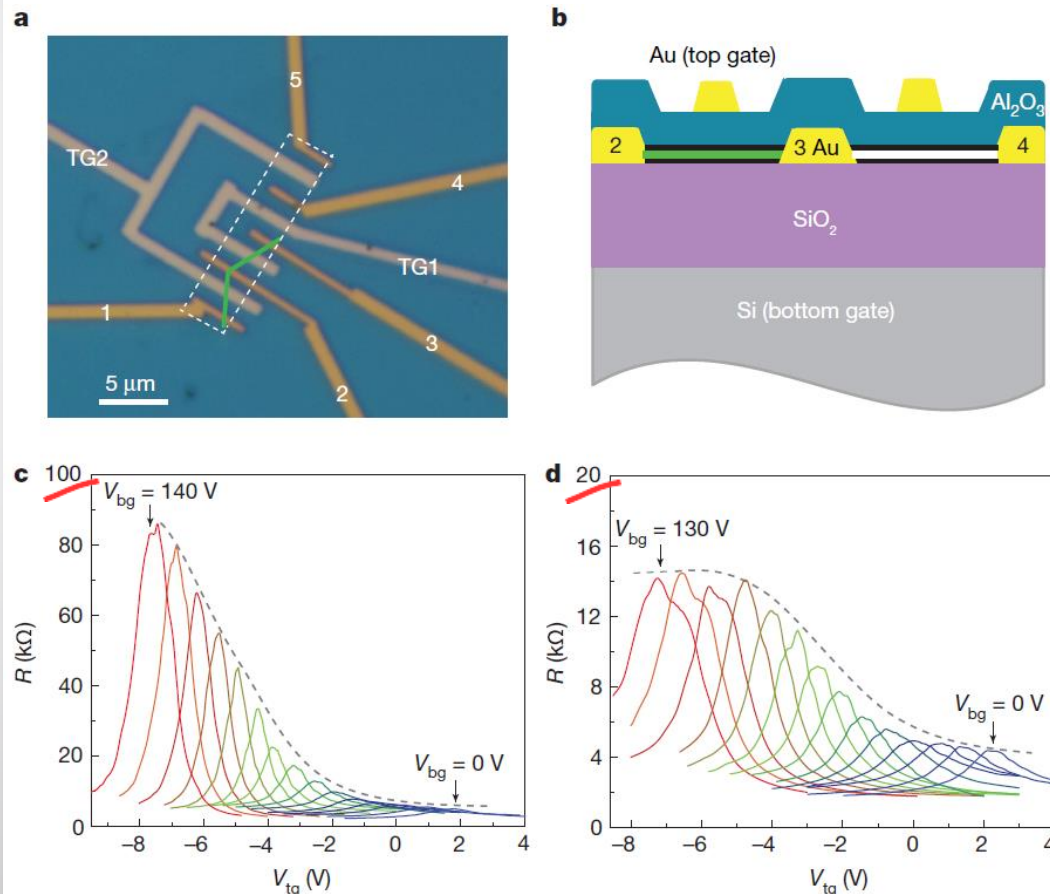
Ju – Nature (2015)

LETTER

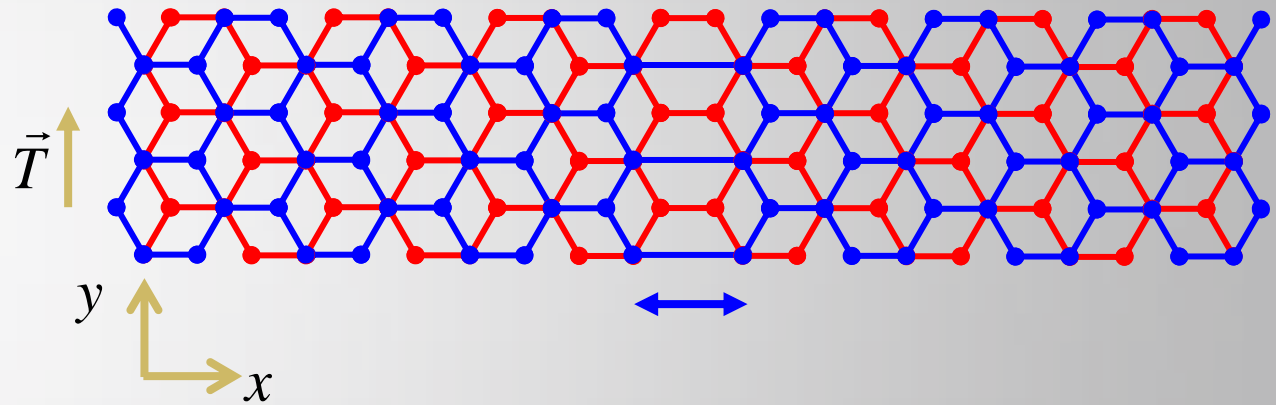
doi:10.1038/nature14364

Topological valley transport at bilayer graphene domain walls

Long Ju^{1*}, Zhiwen Shi^{1*}, Nityan Nair¹, Yinchuan Lv¹, Chenhao Jin¹, Jairo Velasco Jr¹, Claudia Ojeda-Aristizabal¹, Hans A. Bechtel², Michael C. Martin², Alex Zettl^{1,3,4}, James Analytis^{1,3,4} & Feng Wang^{1,3,4}



Abrupt
connection

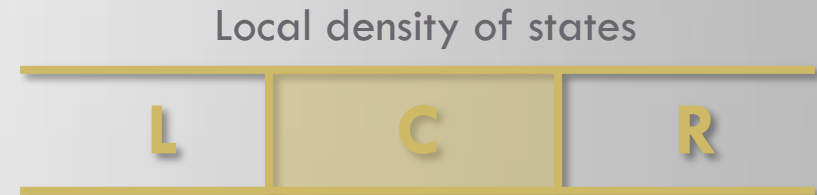
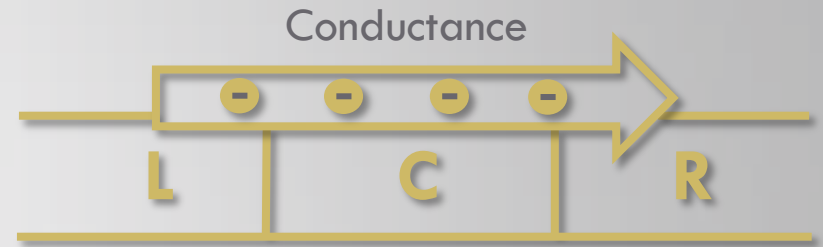
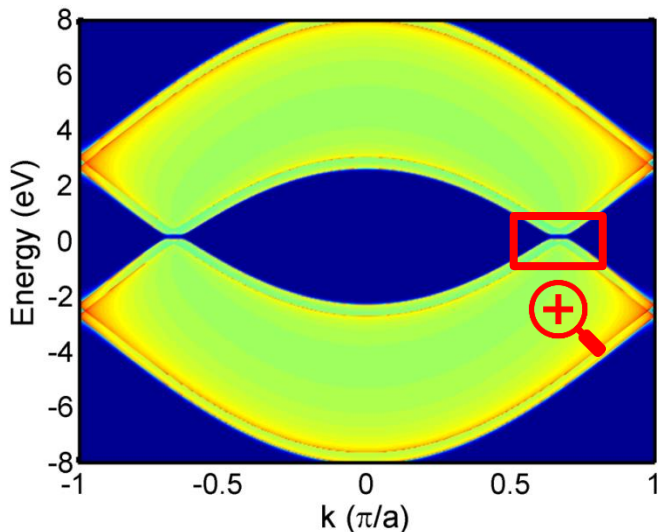


π -electron TB + Green functions

in-plane: nearest neighbor approx.

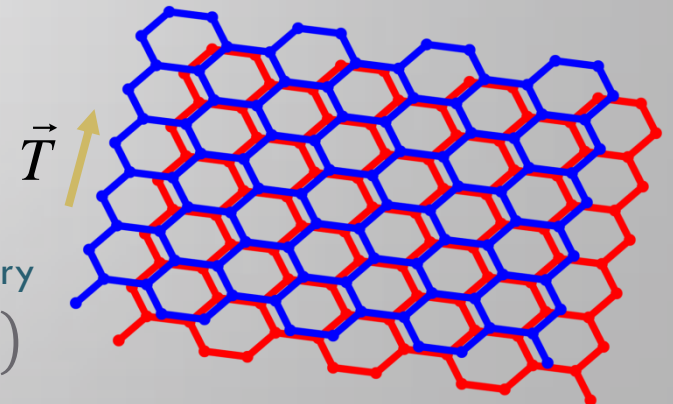
interplane: hopping for overlapping atoms

GFMT: Landauer-Büttiker formalism



Time-reversal symmetry

$$\Psi(\vec{k}) = \Psi(-\vec{k})$$

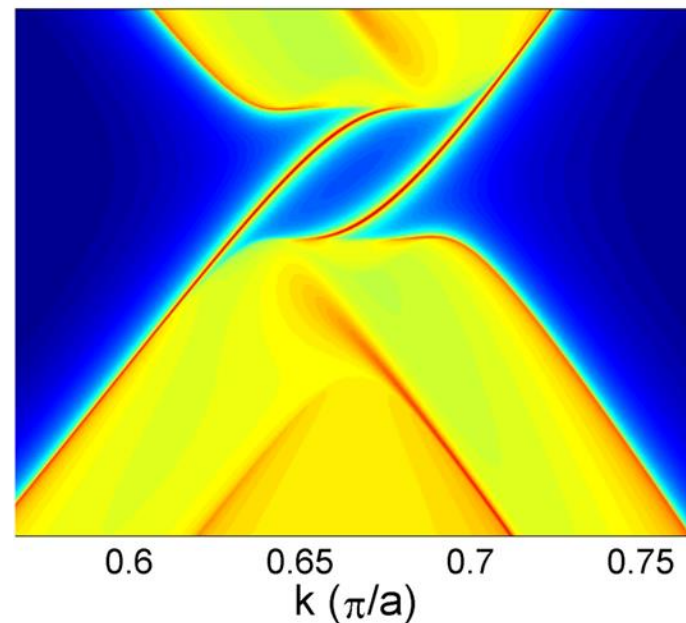
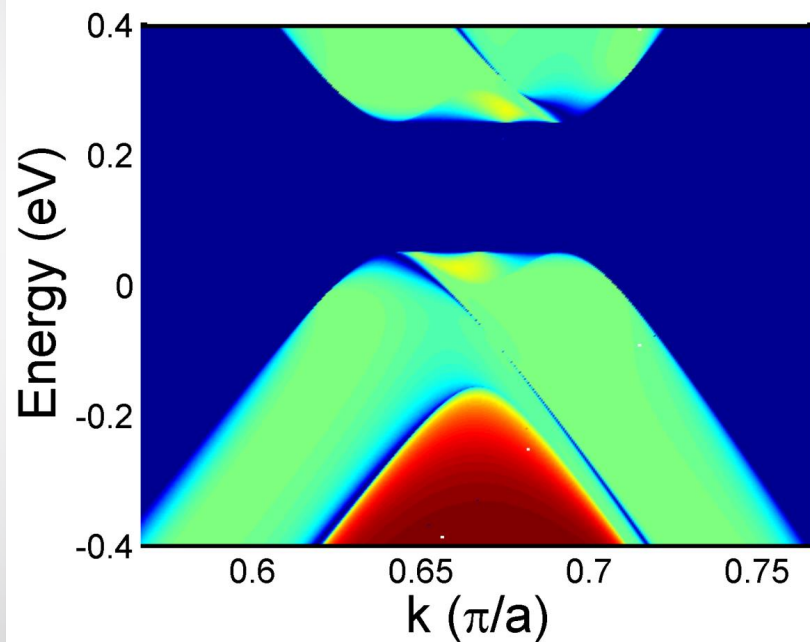


Abrupt connection

$$V = 0.3 \text{ eV}$$

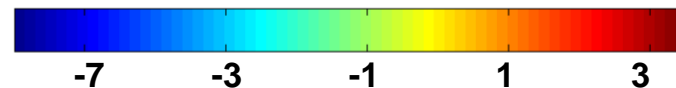
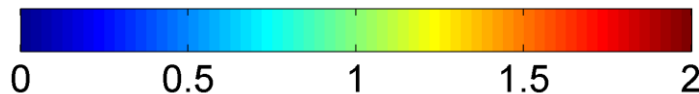
Conductance
between domains

Local Density of States
at the boundary



G ($2e^2/h$)

$\ln(\text{LDOS})$

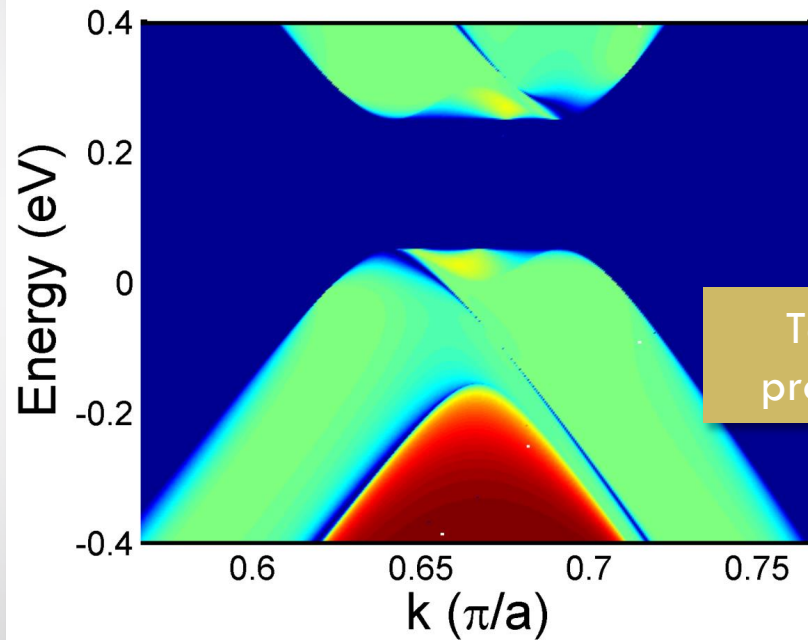


Abrupt connection

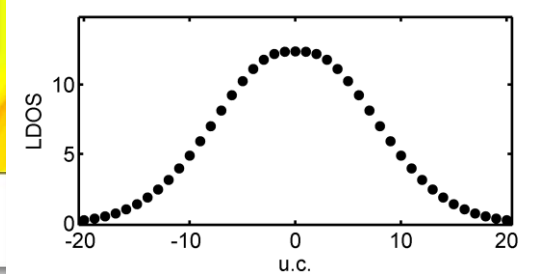
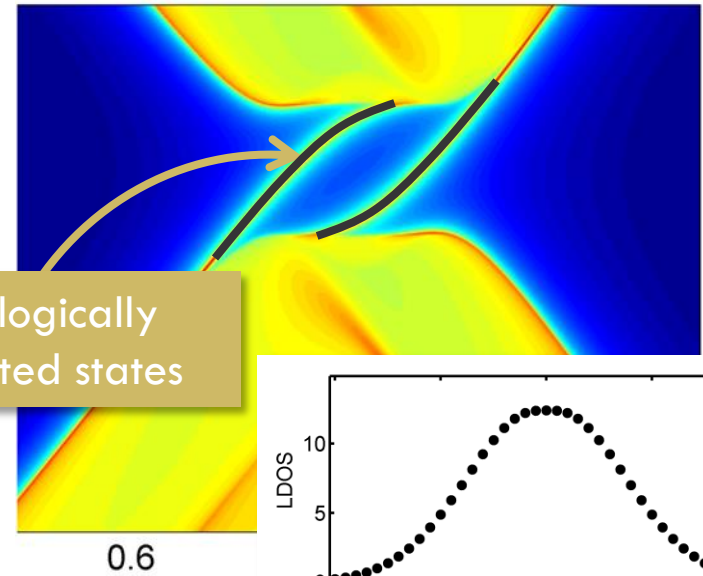
$$V = 0.3 \text{ eV}$$

Conductance
between domains

Local Density of States
at the boundary

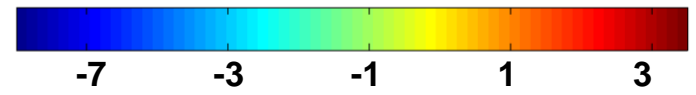
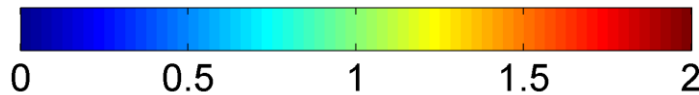


Topologically
protected states

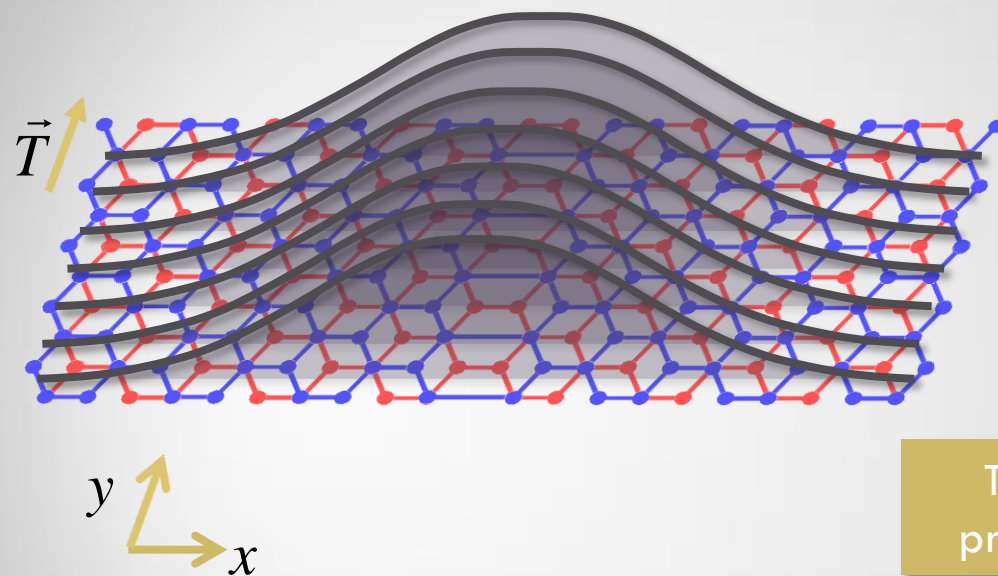


G ($2e^2/h$)

$\ln(\text{LDOS})$



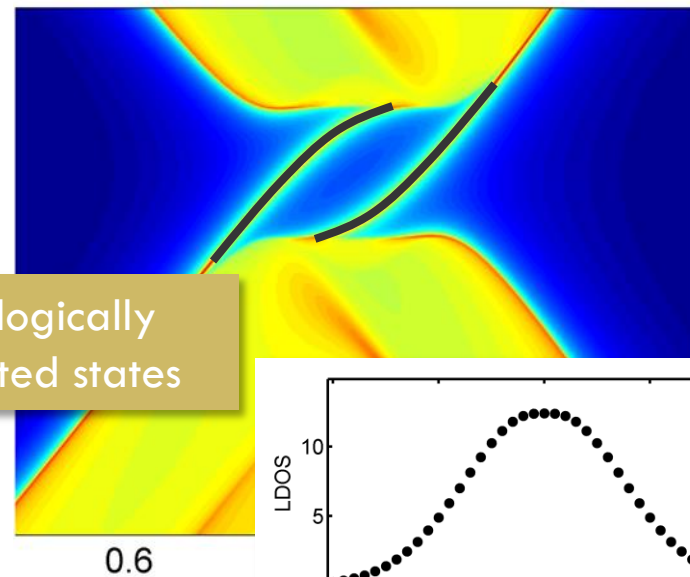
Abrupt connection



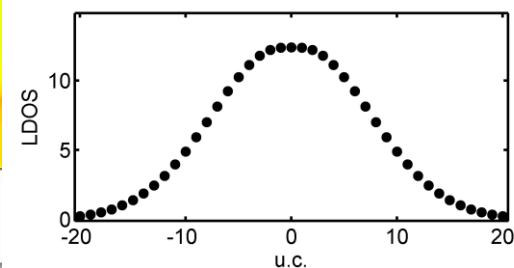
$$G_x(E_F) = 0$$

$$G_y(E_F) \neq 0$$

Local Density of States
at the boundary



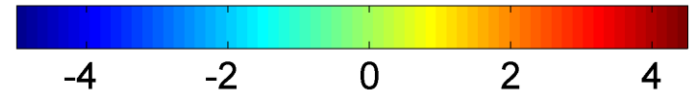
Topologically
protected states



Topology

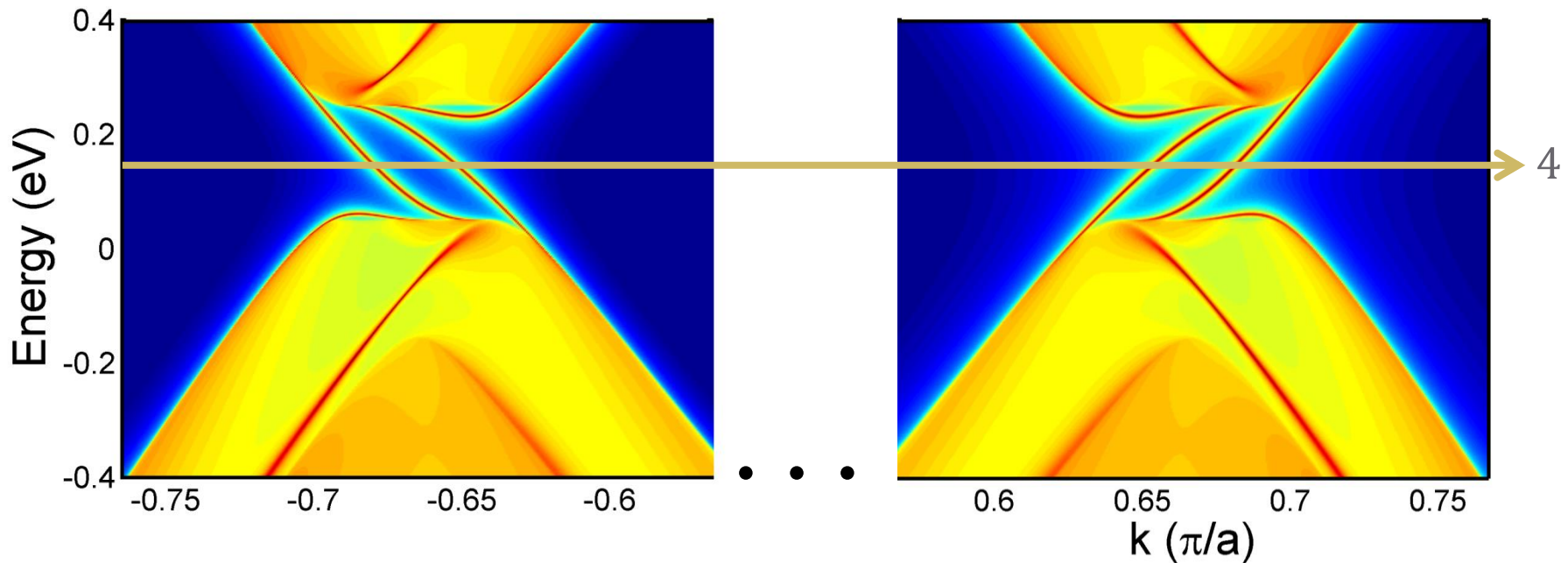
symmetry-protected topological state
 difference of „valley” Chern numbers = 2
 robust (insensitive to local impurities)

$\ln(\text{LDOS})$

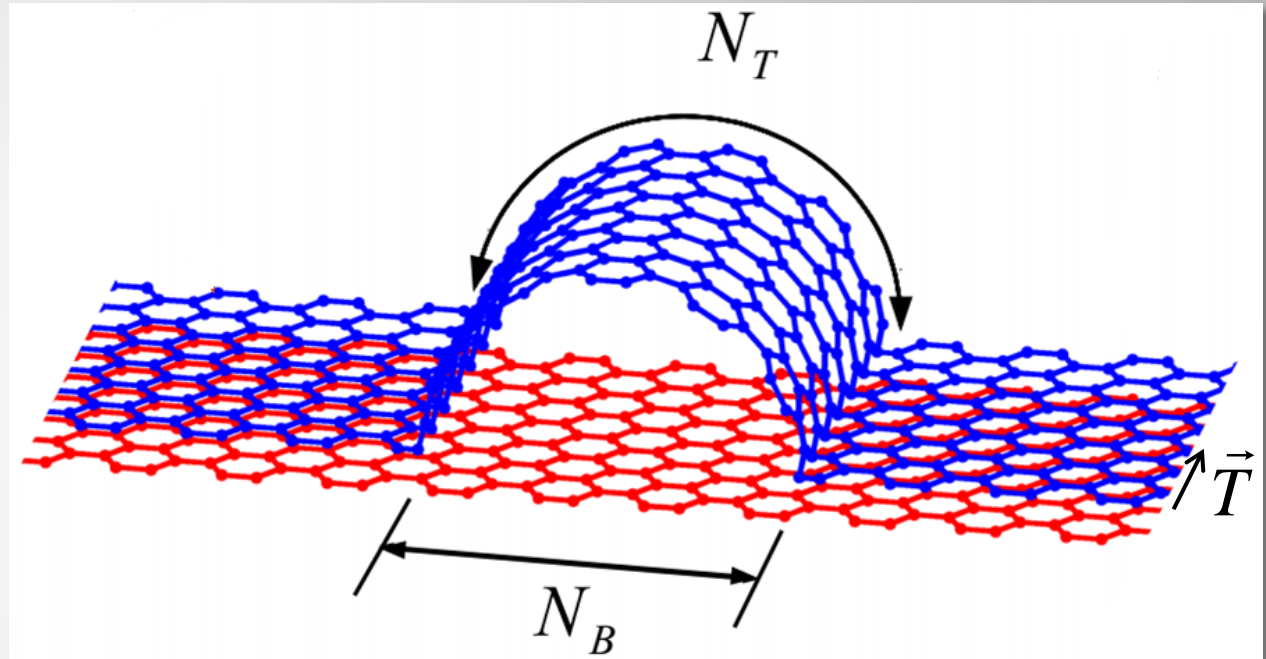


$$\begin{aligned} \curvearrowright K' \quad n_{AB} &= -1 \\ n_{BA} &= +1 \end{aligned}$$

$$\begin{aligned} \curvearrowright K \quad n_{AB} &= +1 \\ n_{BA} &= -1 \end{aligned}$$



Corrugation



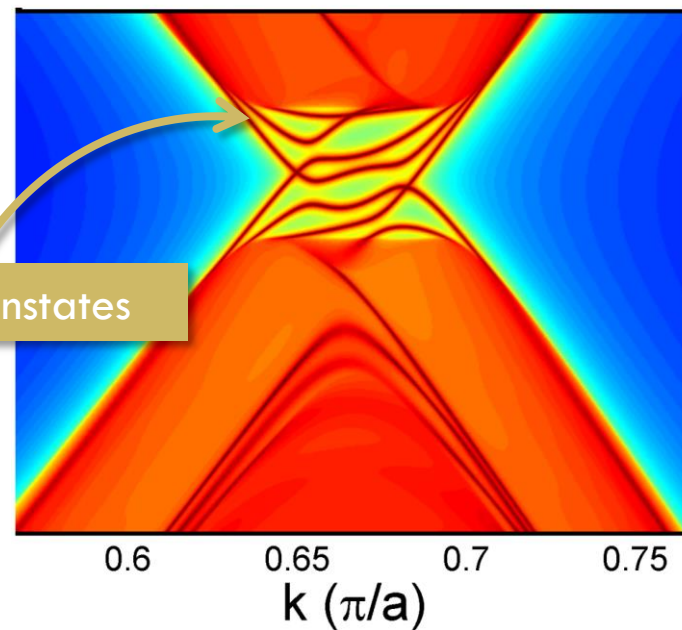
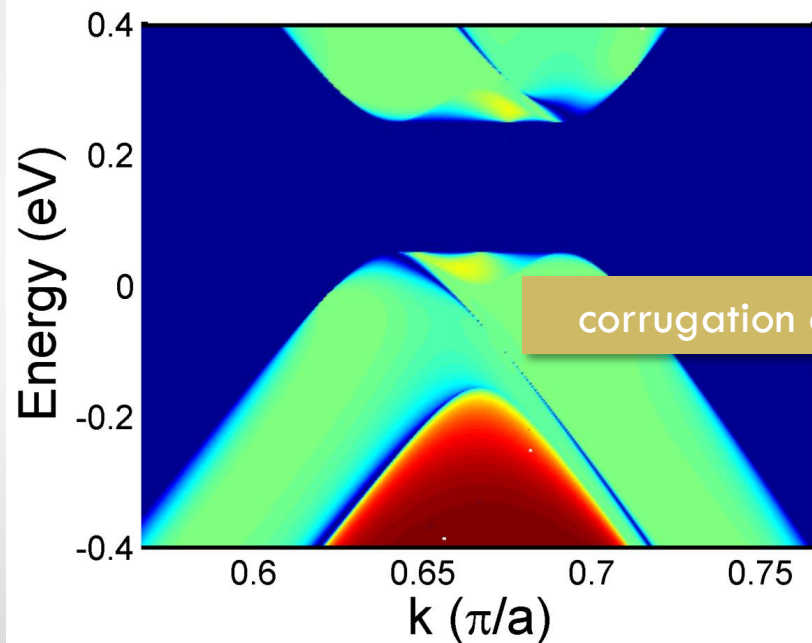
$$N_T \approx \pi \cdot N_B$$

Corrugation

$$N_B = 30 \quad V = 0.3 \text{ eV}$$
$$N_T = 48$$

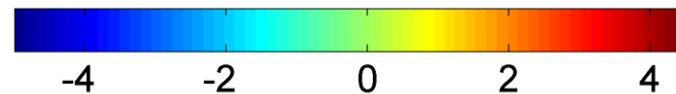
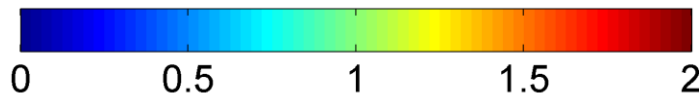
Conductance
between domains

Local Density of States
at the boundary



G ($2e^2/h$)

$\ln(\text{LDOS})$

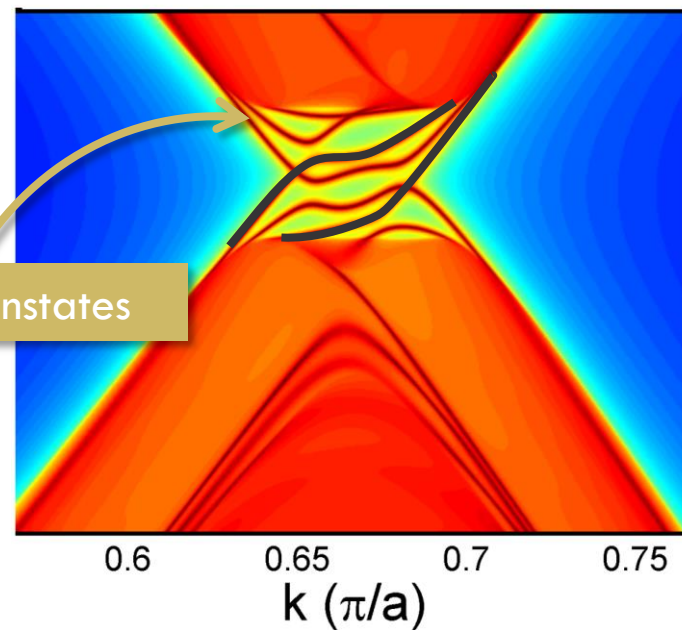
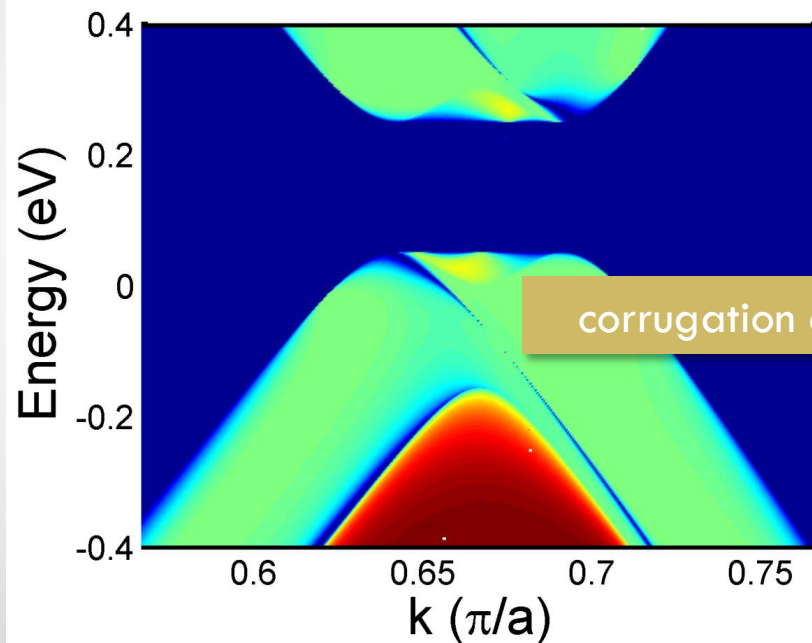


Corrugation

$$N_B = 30 \quad V = 0.3 \text{ eV}$$
$$N_T = 48$$

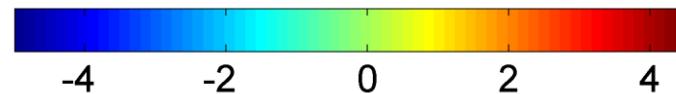
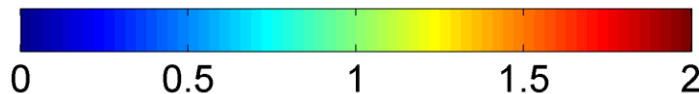
Conductance
between domains

Local Density of States
at the boundary



G ($2e^2/h$)

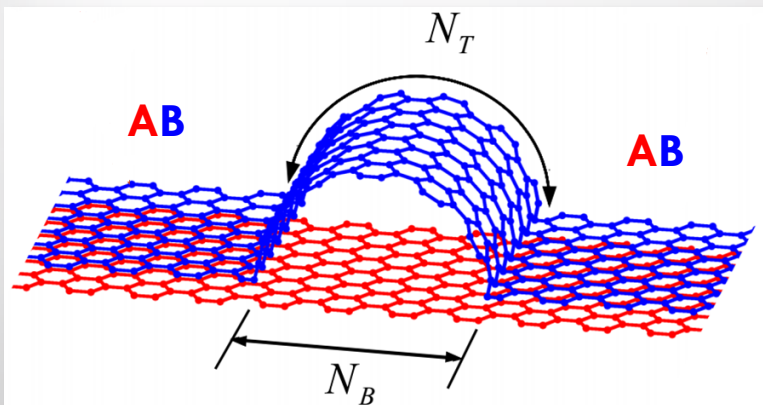
$\ln(\text{LDOS})$



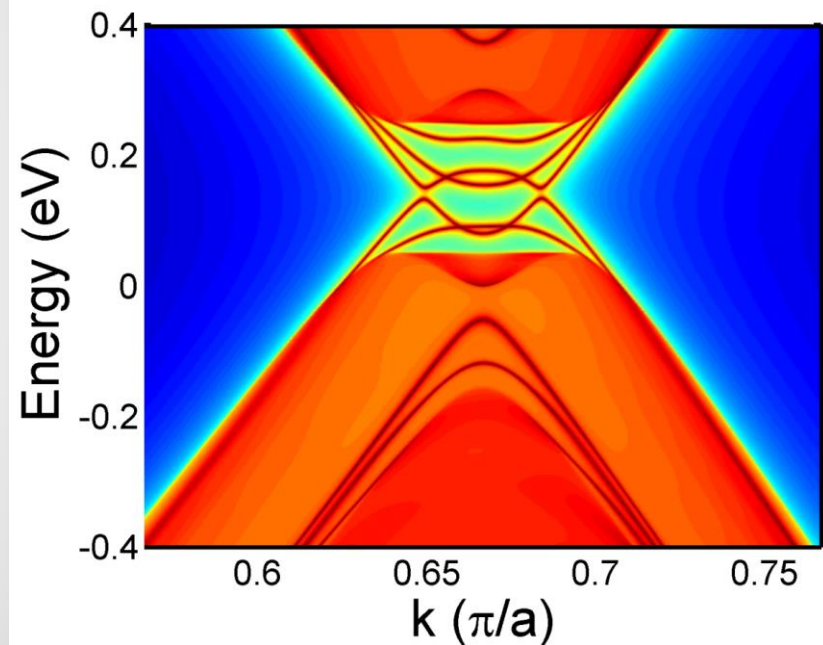
Corrugation

$$N_B = 30 \quad V = 0.3 \text{ eV}$$
$$N_T = 48$$

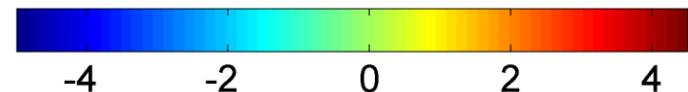
no stacking change



Local Density of States
at the boundary



$\ln(\text{LDOS})$



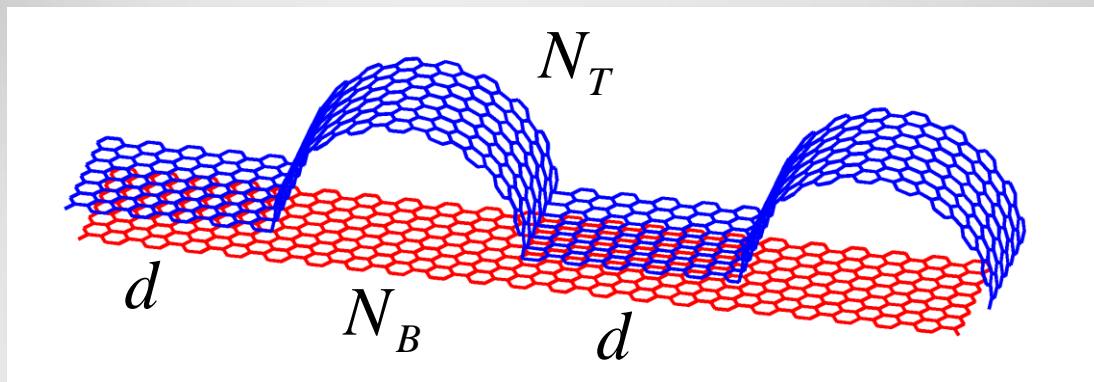
Conductance along the fold

$$N_B = 6$$

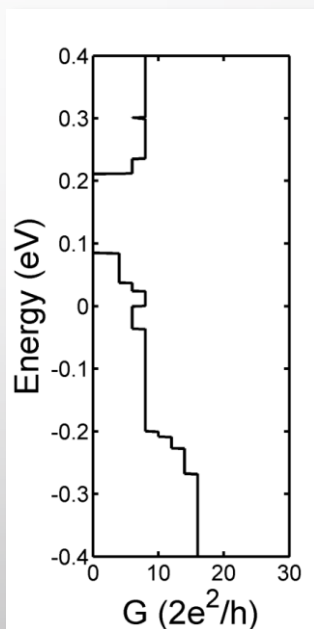
$$N_T = 10$$

$$d = 10$$

$$V = 0.3 \text{ eV}$$

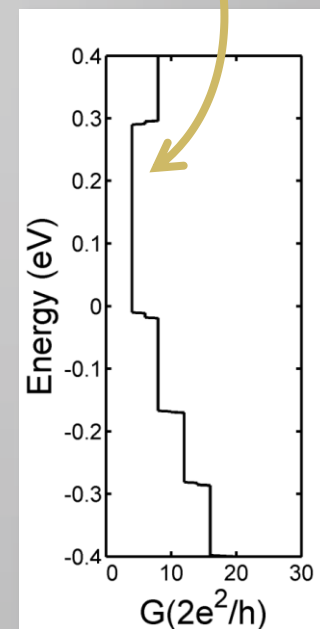
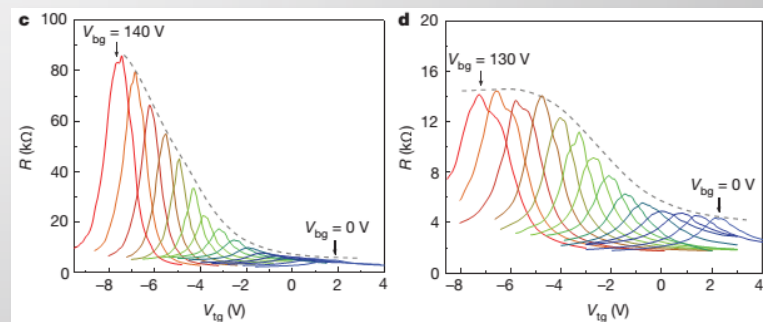


$$G(E_F) = 4$$



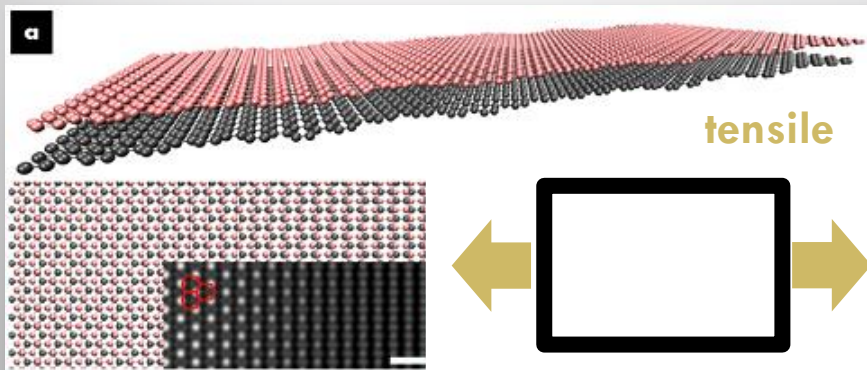
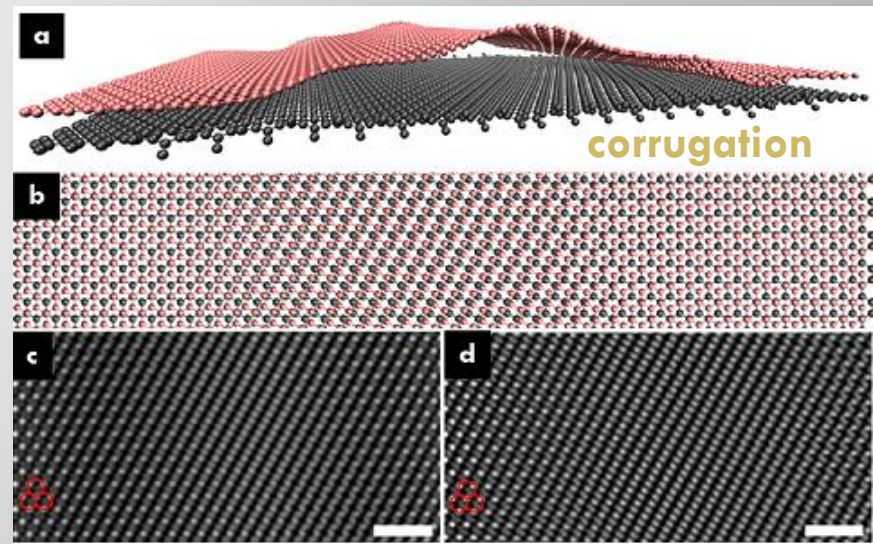
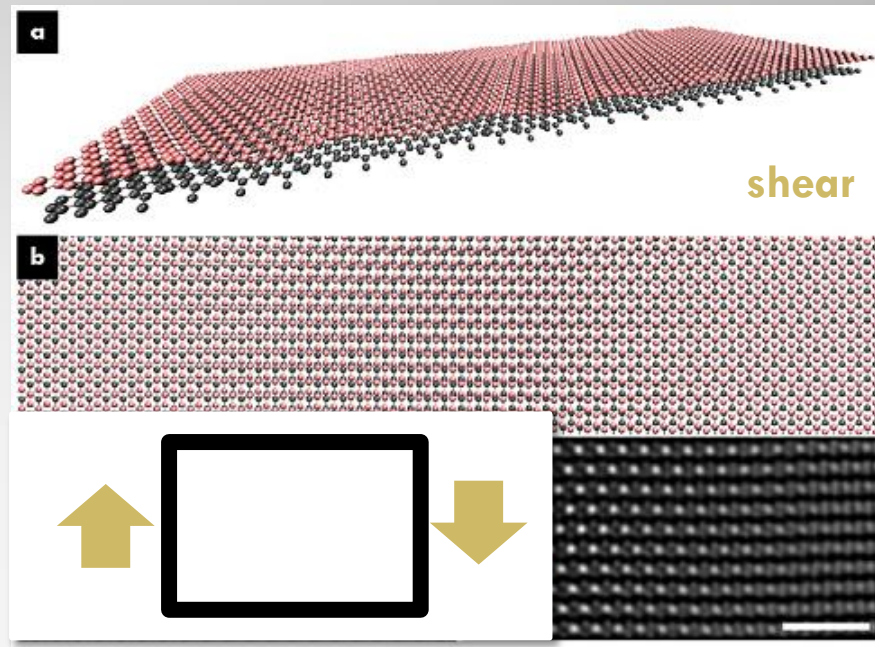
with stacking change

no stacking change



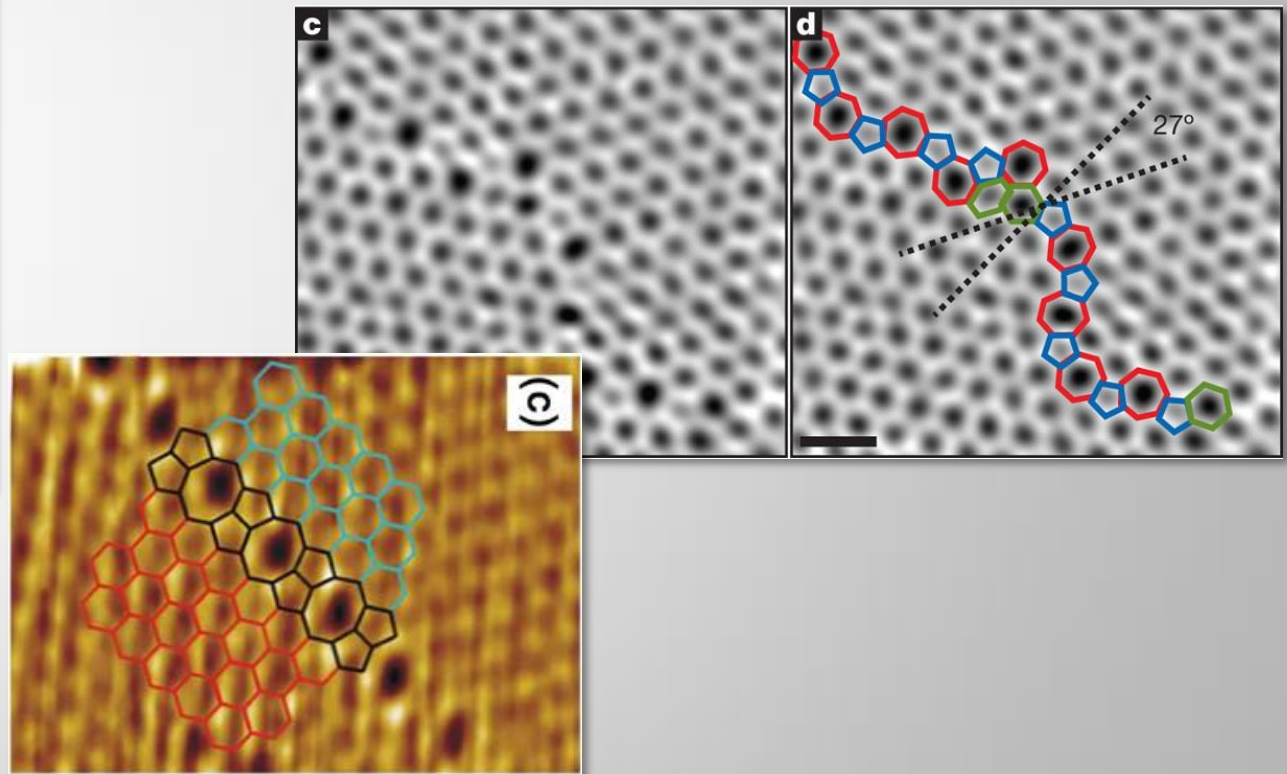
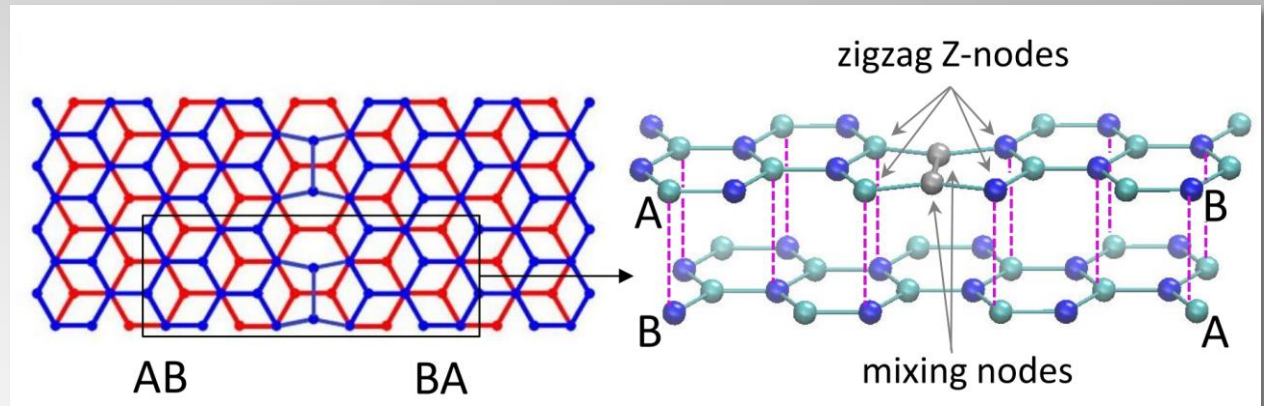
Defectless boundaries

„as long as we do
not mix the
sublattices”



San-Jose – PNAS (2014), Vaezi – PRX (2013)
Katsnelson – PRB (2008)

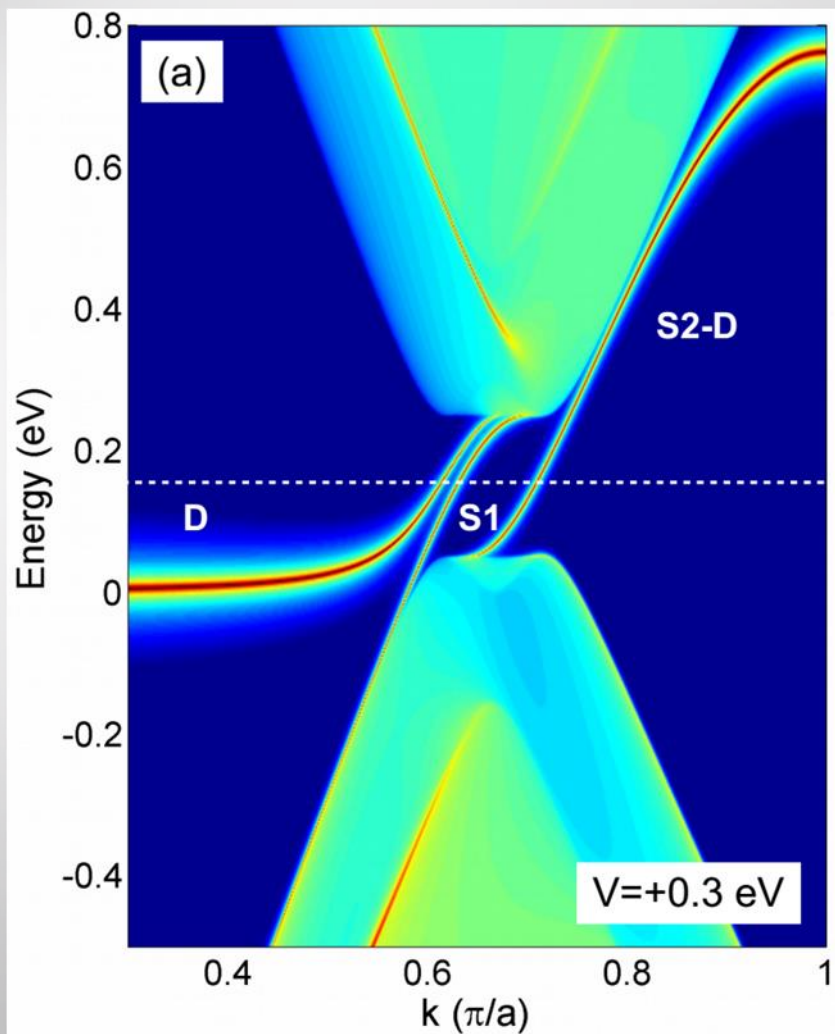
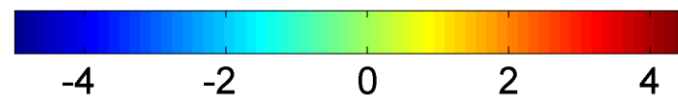
Grain boundaries



Grain stacking boundary

$$V = +0.3 \text{ eV}$$

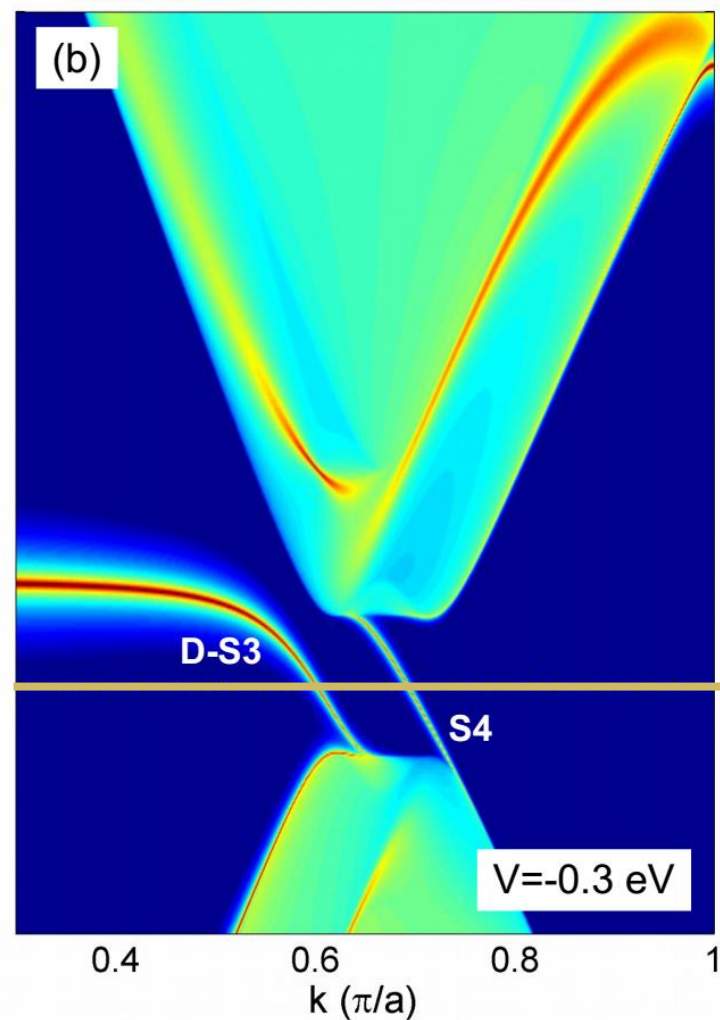
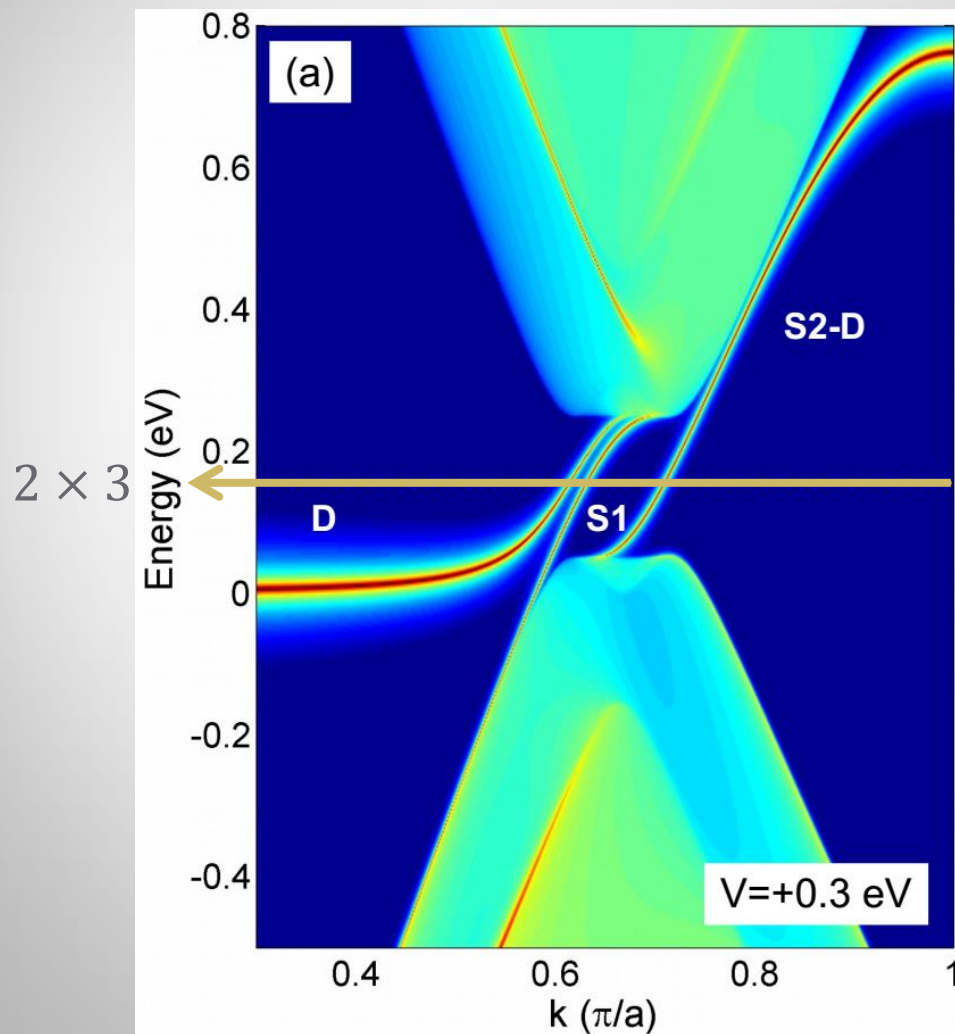
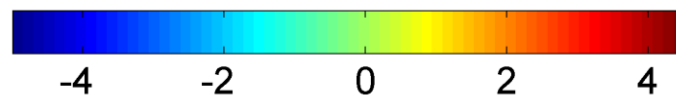
$\ln(\text{LDOS})$



Grain stacking boundary

$$V = \pm 0.3 \text{ eV}$$

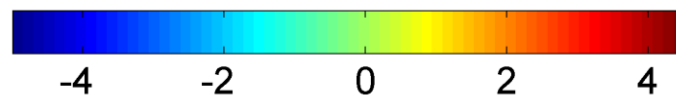
$\ln(\text{LDOS})$



Ingredients

$$V = \pm 0.3 \text{ eV}$$

$\ln(\text{LDOS})$



SL with grain
boundary 8/55

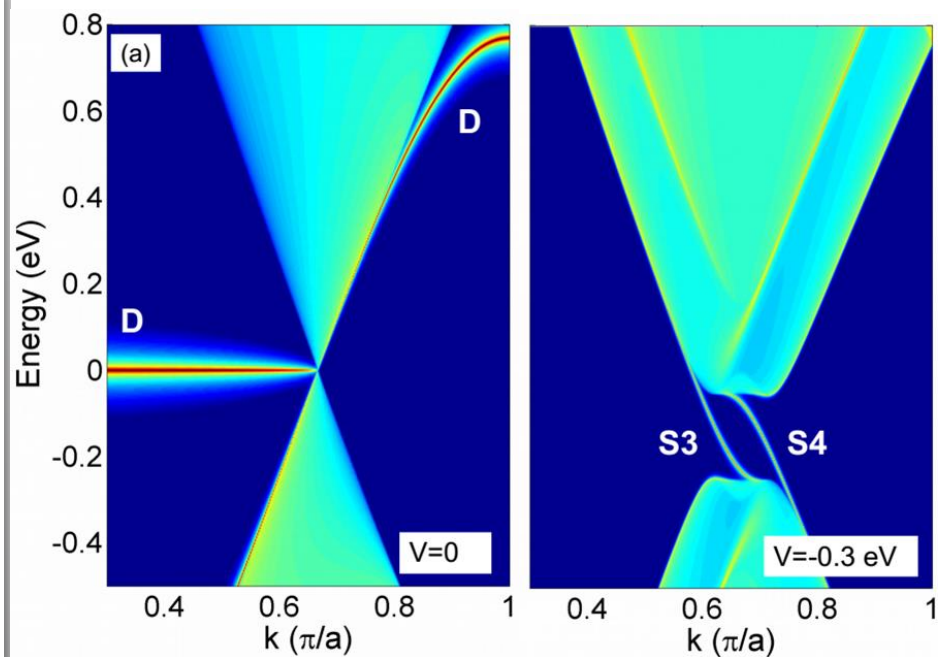
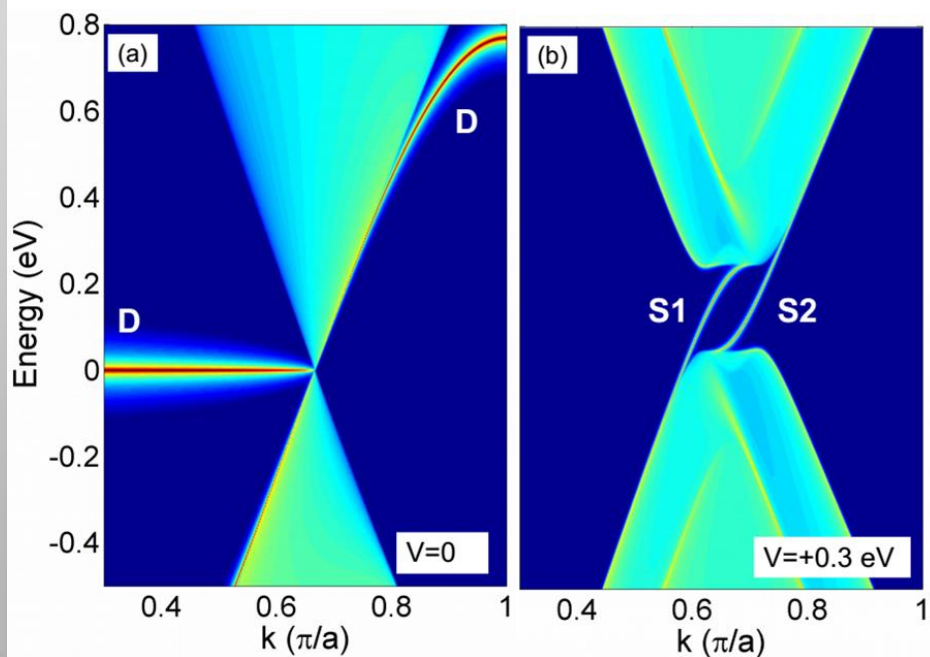


BL with stacking
boundary, $V > 0$

SL with grain
boundary 8/55



BL with stacking
boundary, $V < 0$



Localization

$$V = \pm 0.3 \text{ eV}$$

different
layers

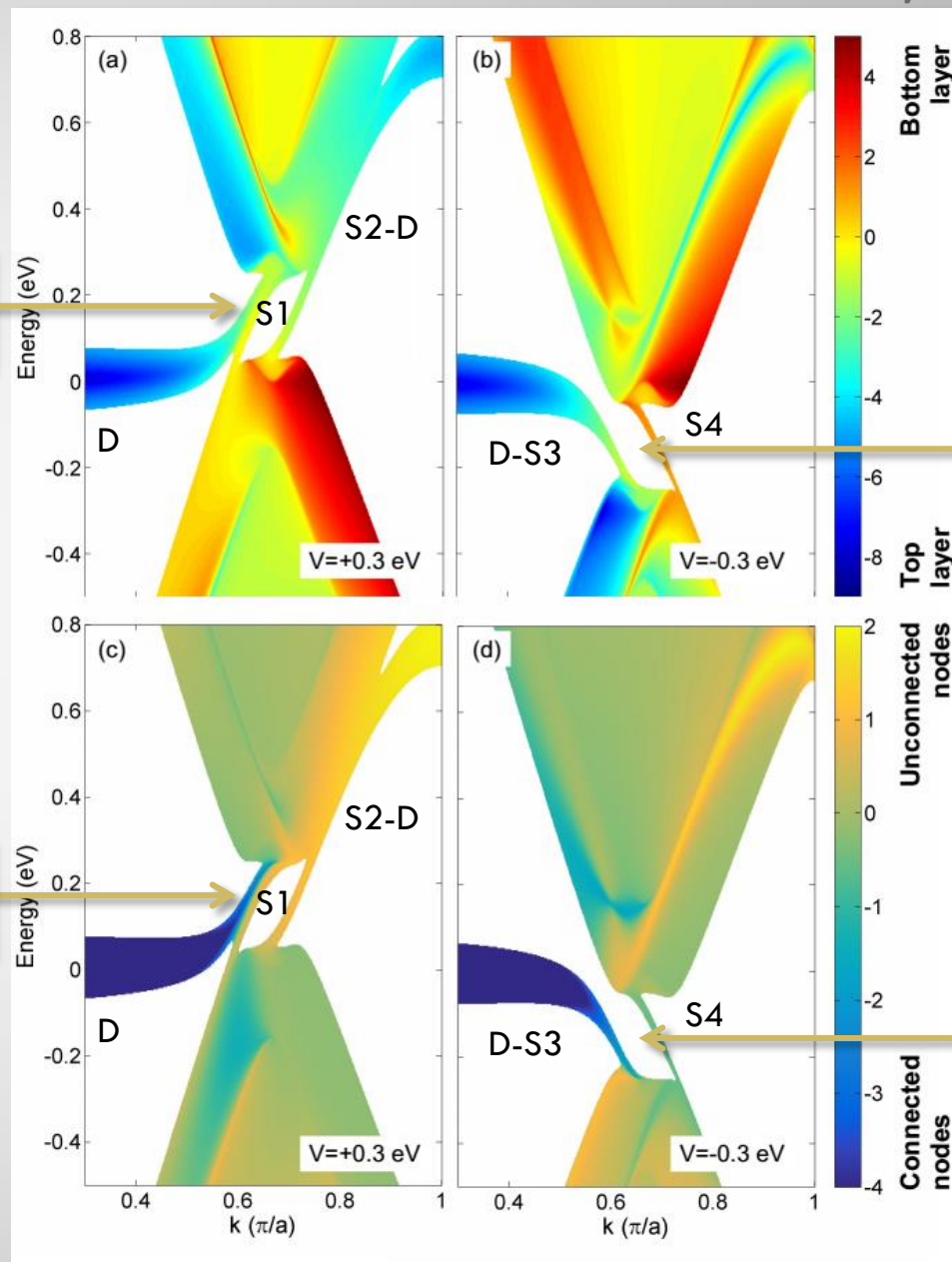
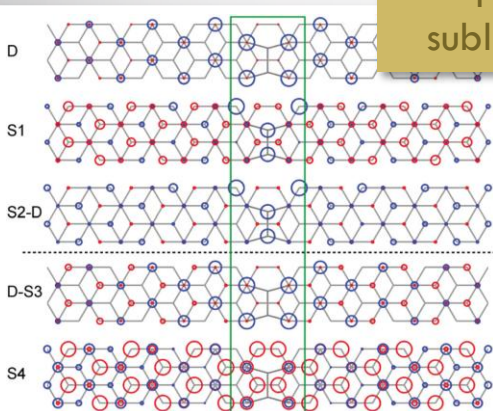
Defect (D) and TPS (S1)
coexist when they are
localized on different nodes

Defect (D) and TPS (S3)
hybridize when they are
localized on same nodes

opposite
sublattices

same
layers

same
sublattices



Summary

Abrupt connection

The appearance of 2 TPS
(Chern numbers)

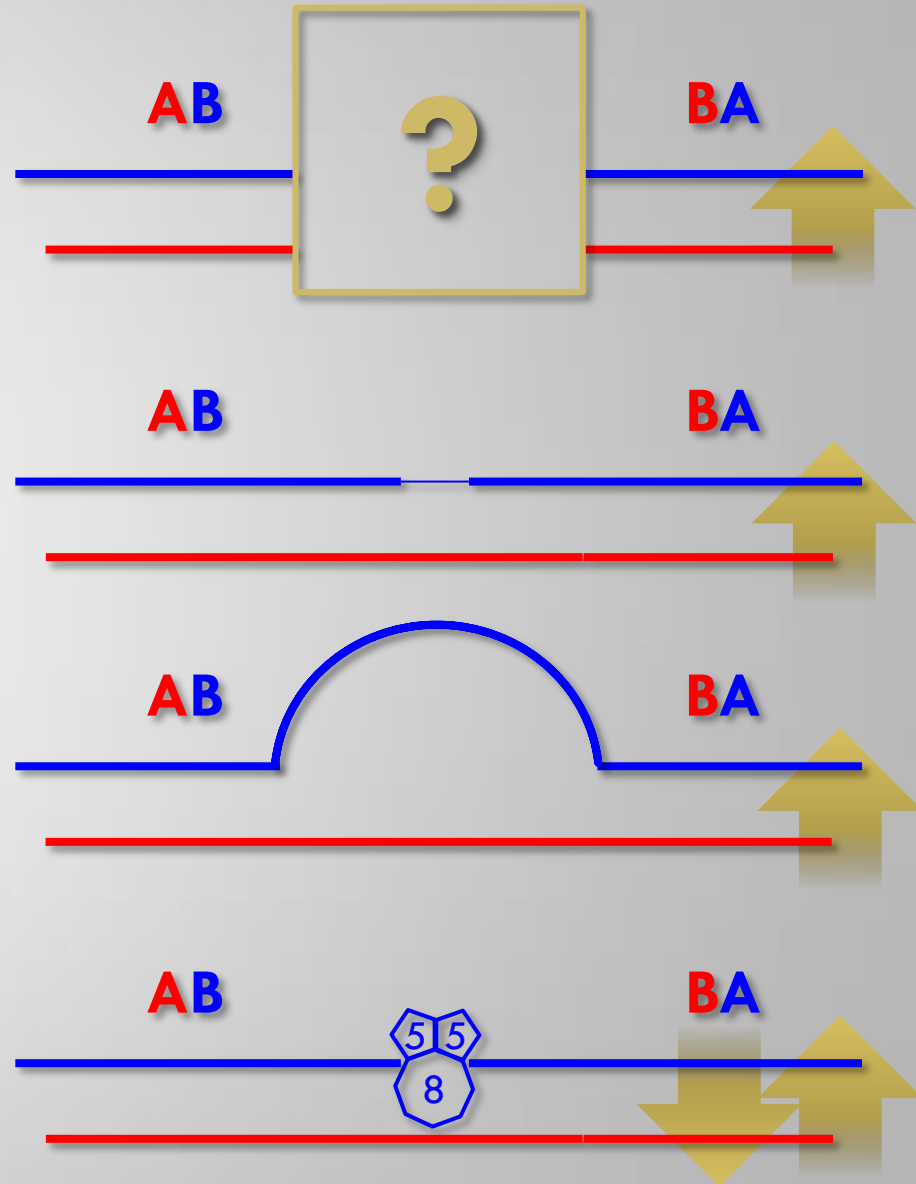
Defectless, smooth transitions

More gap states (anticrossings)
2 TPS not affected (Chern numbers)

Grain boundaries with defects

Interaction between TPS and defect state
Asymmetry in number gap states for different
polarization – potential electrical switches

Bilayer graphene with stacking boundary



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Nanoscale **8**, 6079 (2016)

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