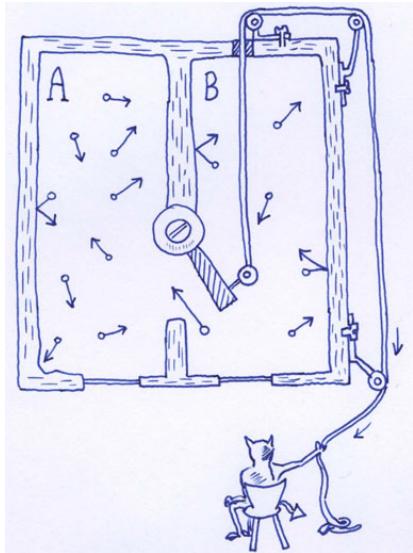


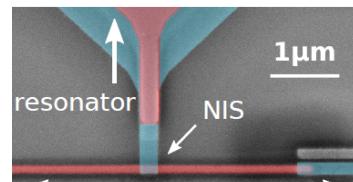
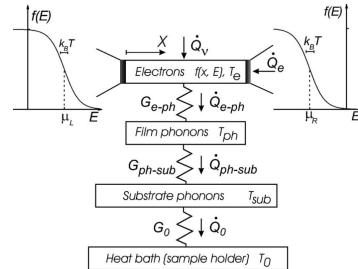
# LECTURE 2, Jukka Pekola

## Outline

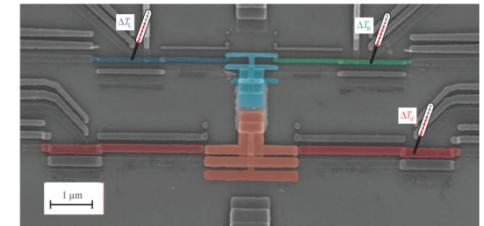
### Maxwell's demon



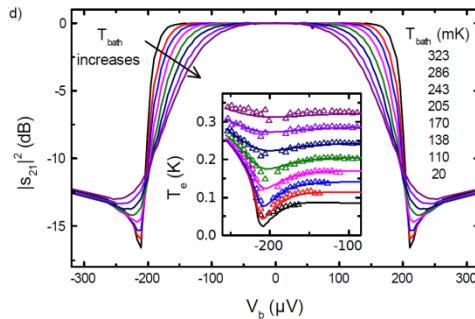
### Energy relaxation and thermometry



### Autonomous Maxwell's Demon

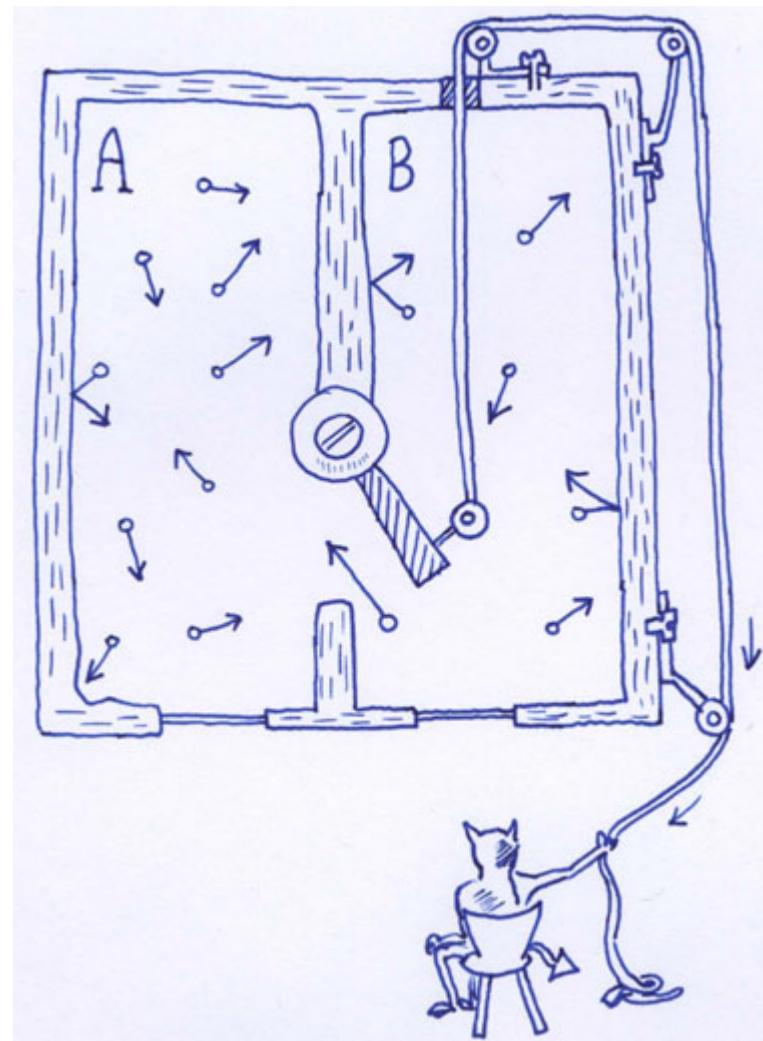


### ... role of information



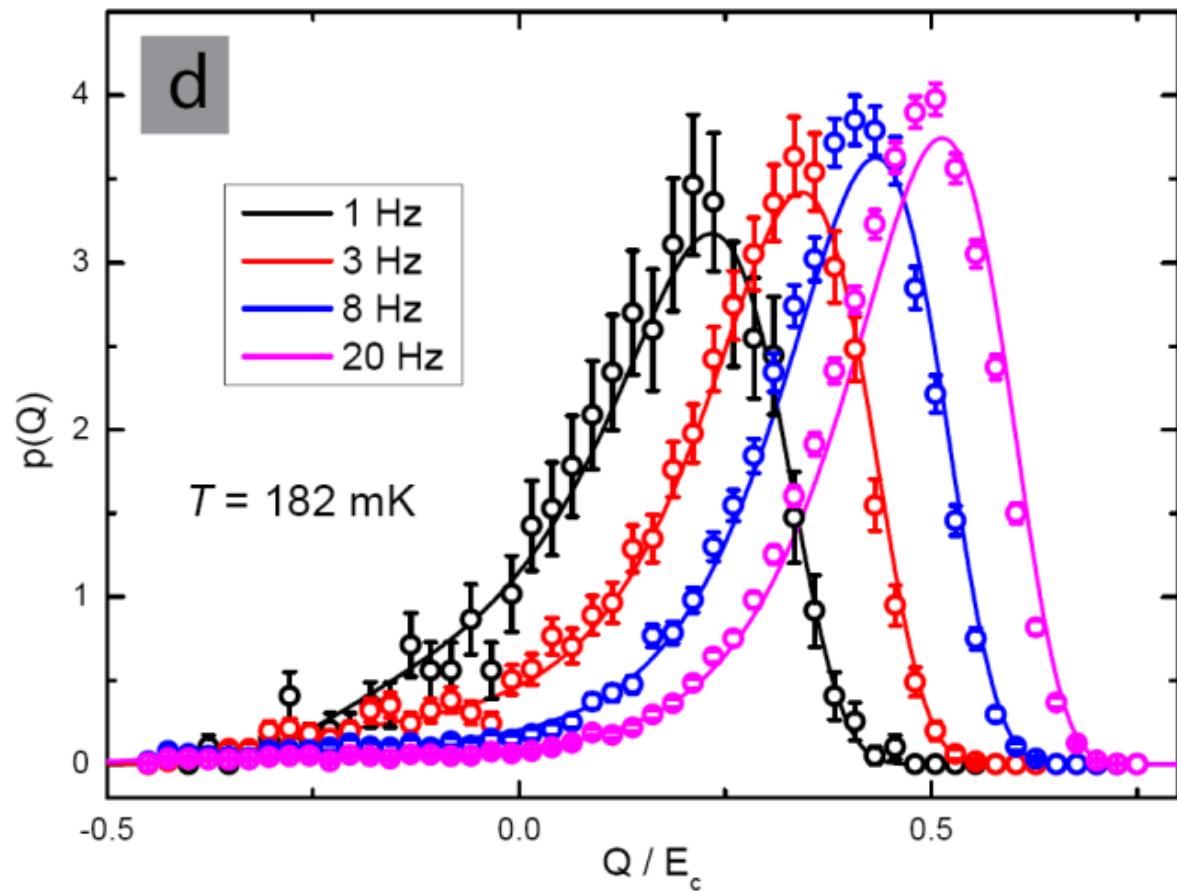
# Maxwell's Demon

J. C. Maxwell 1867



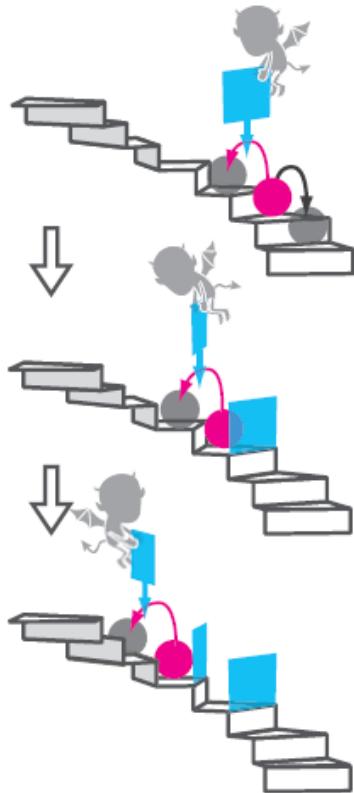
# Negative heat

Possible to extract heat from the environment

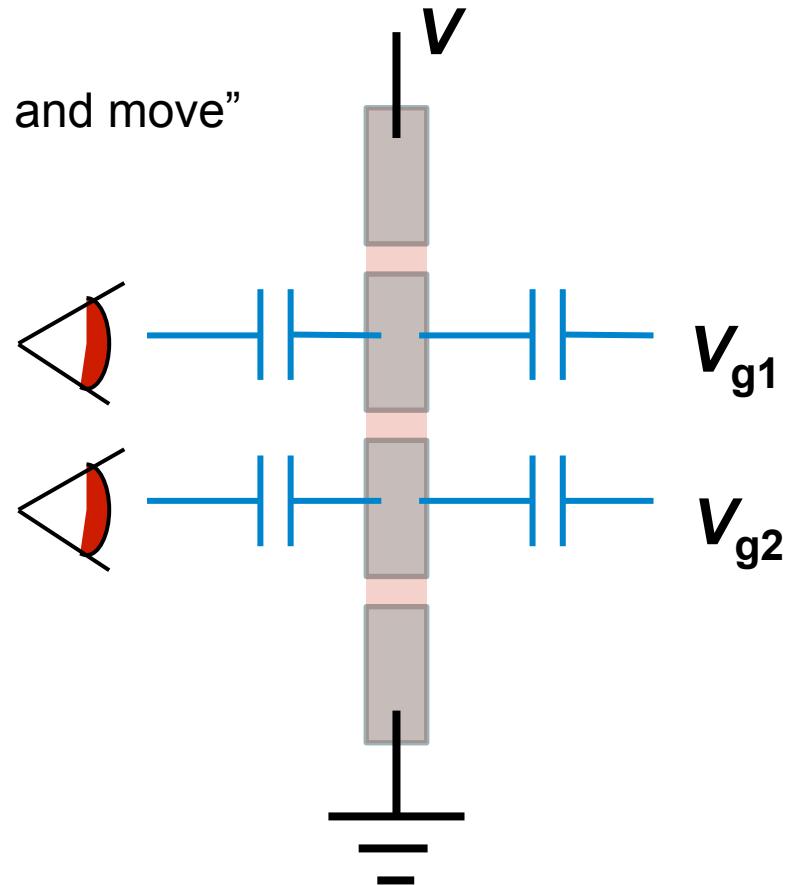


Provides means to realize Maxwell's demon using SETs

# Electronic Maxwell's demon



"watch and move"



S. Toyabe et al., Nature Physics 2010

- D. Averin et al., PRB 84, 245448 (2011).  
G. Schaller et al., PRB 84, 085418 (2011).  
P. Strassberg et al., PRL 110, 040601 (2013).  
J. Bergli et al., Phys. Rev. E 88, 062139 (2013).

# Szilard's engine (L. Szilard 1929)

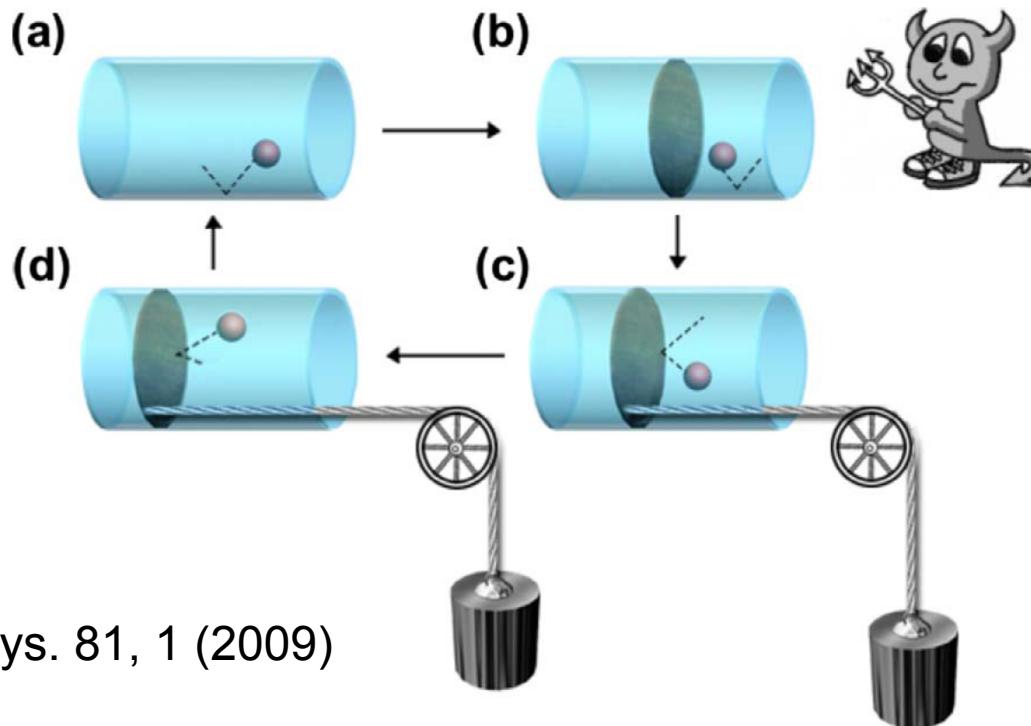


Figure from  
Rev. Mod. Phys. 81, 1 (2009)

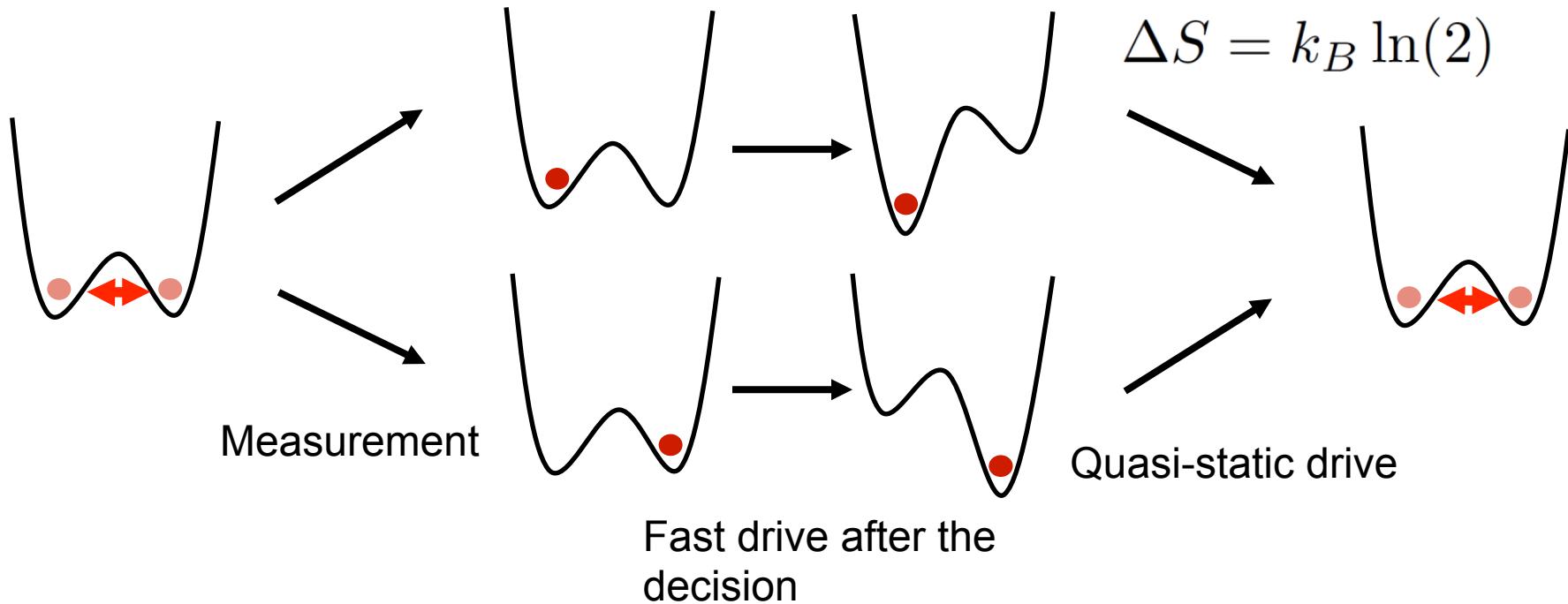
**Isothermal expansion of the "single-molecule gas" does work against the load**

$$W = Q = \int_{V/2}^V pdV = \int_{V/2}^V \frac{k_B T}{V} dV = k_B T \ln 2$$

# Szilard's engine for single electrons

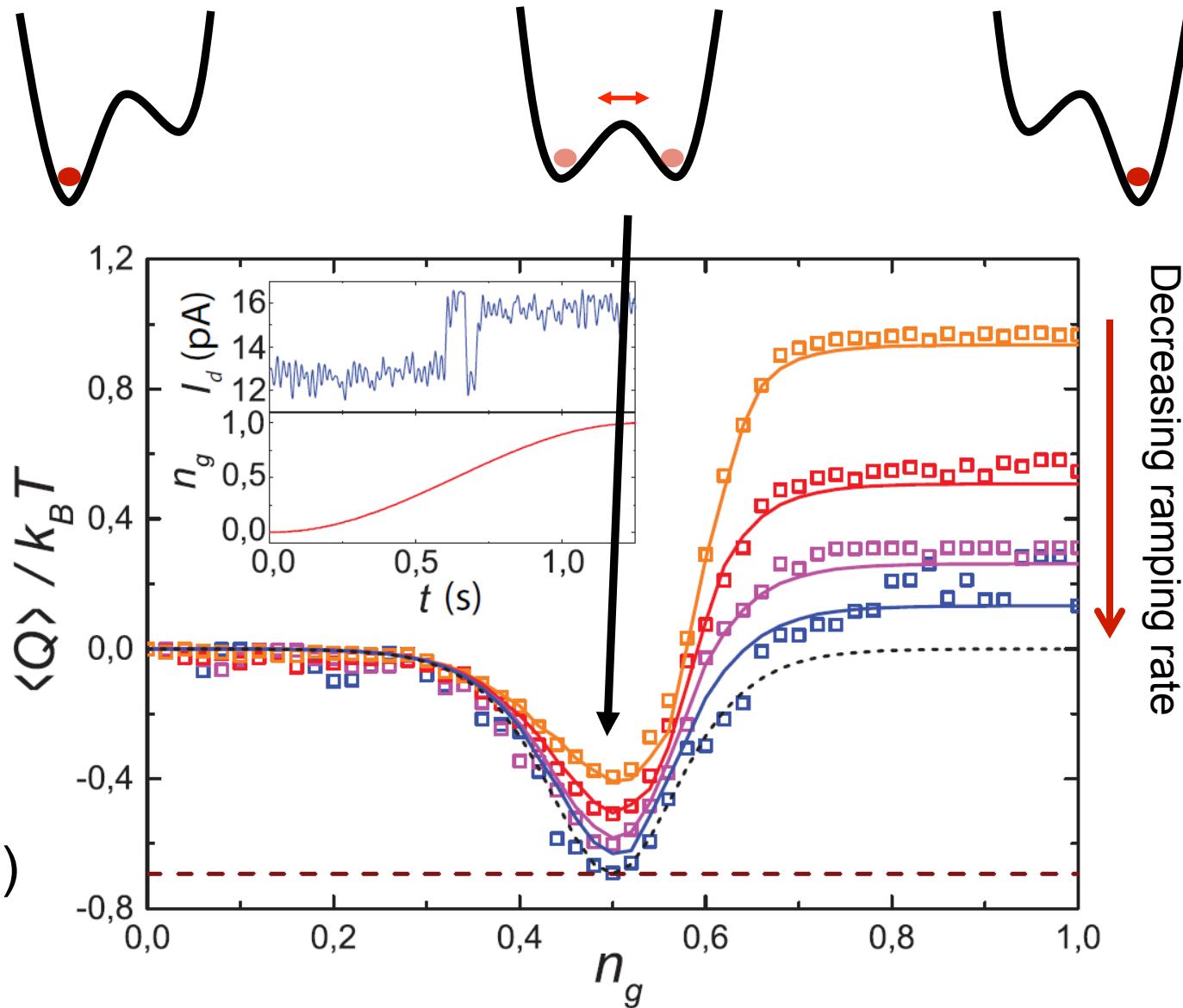
J. V. Koski et al., PNAS 111, 13786 (2014); PRL 113, 030601 (2014).

Entropy of the charge states:  $S = -k_B \sum_{i=0,1} p(i) \ln[p(i)]$



In the full cycle (ideally):  $Q = W = -k_B T \ln(2)$

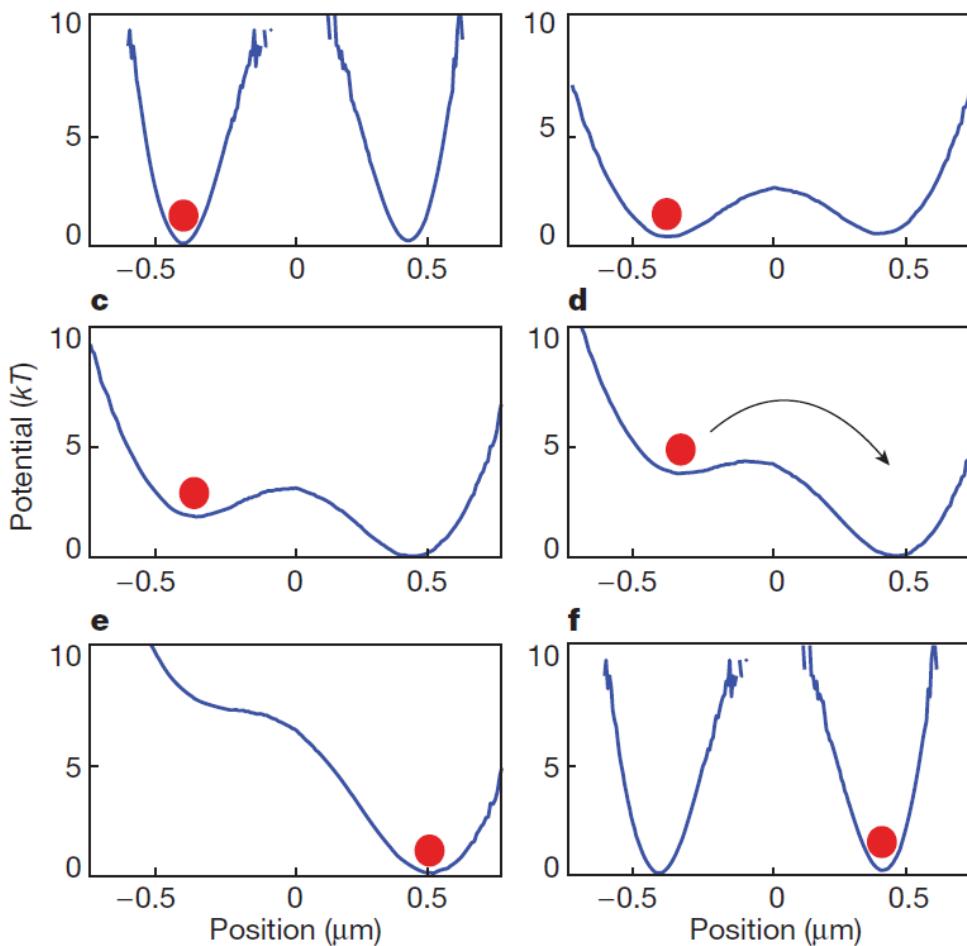
# Extracting heat from the bath



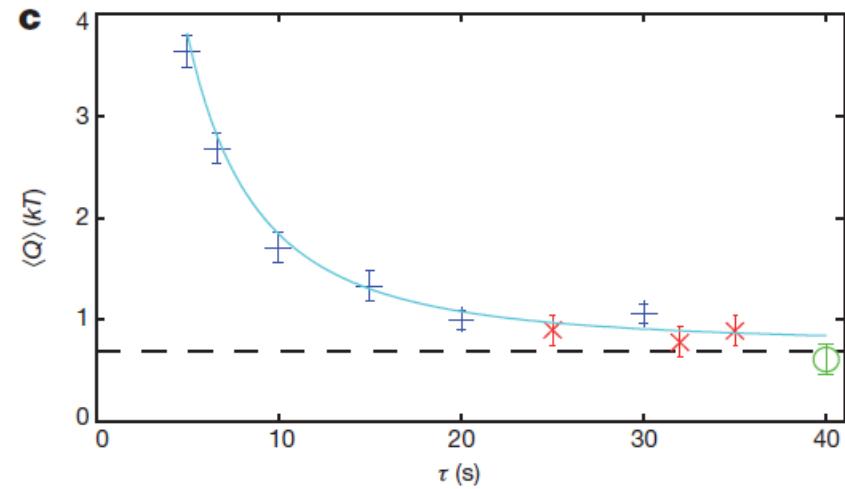
# Erasures of information

**Landauer principle: erasure of a single bit costs energy of at least  $k_B T \ln(2)$**

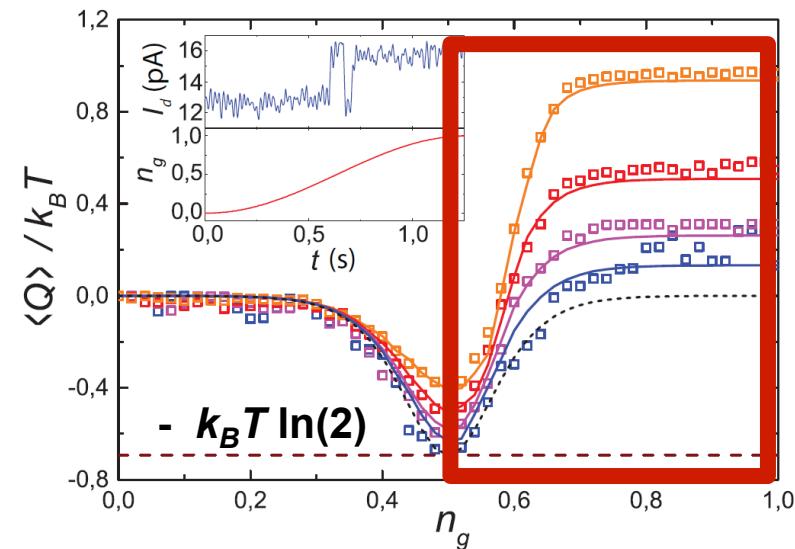
Experiment on a colloidal particle:



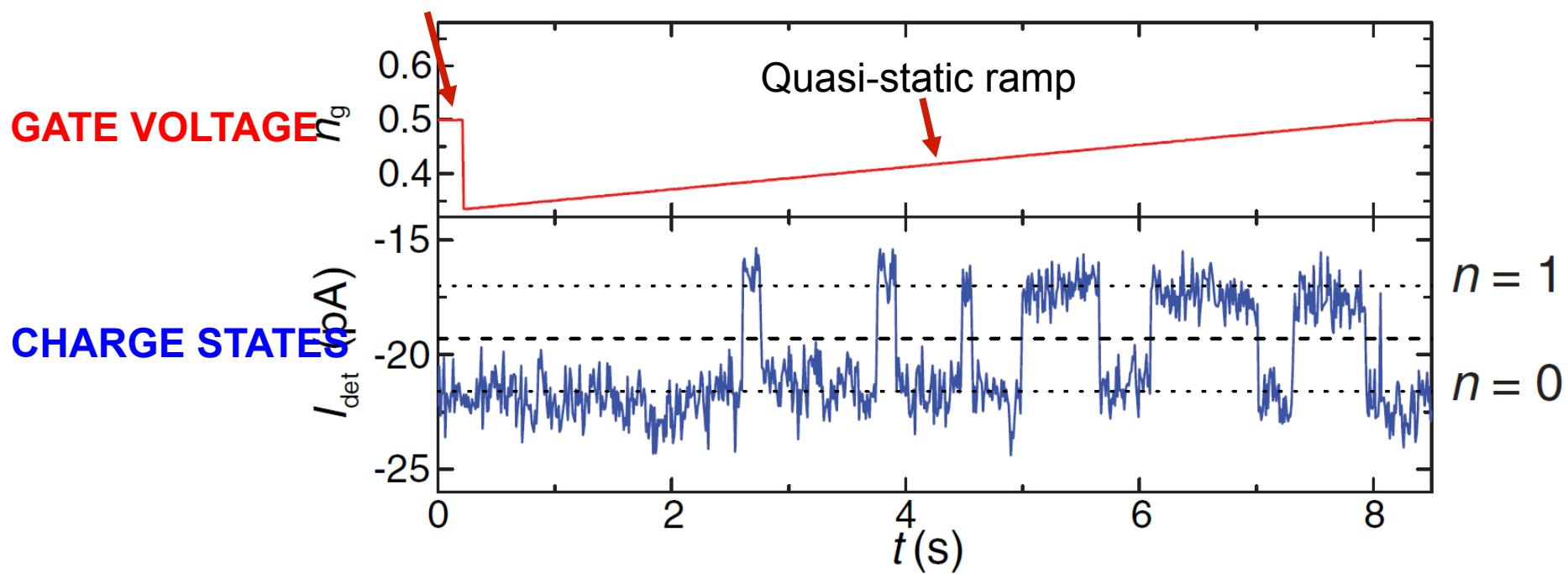
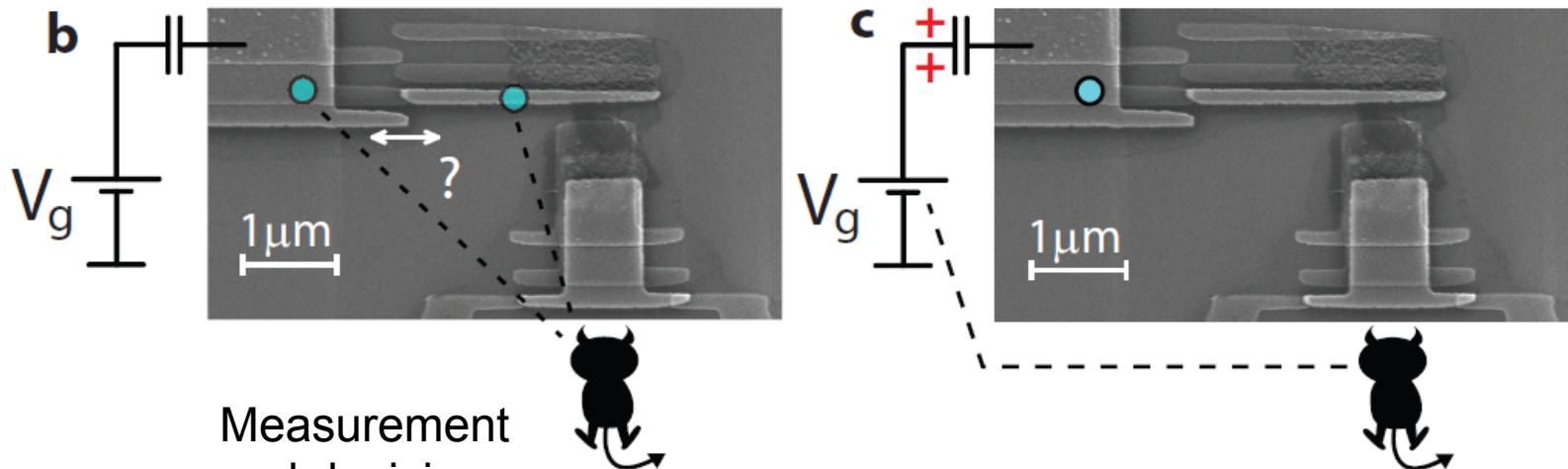
A. Berut, ... , S. Ciliberto et al., Nature 2012



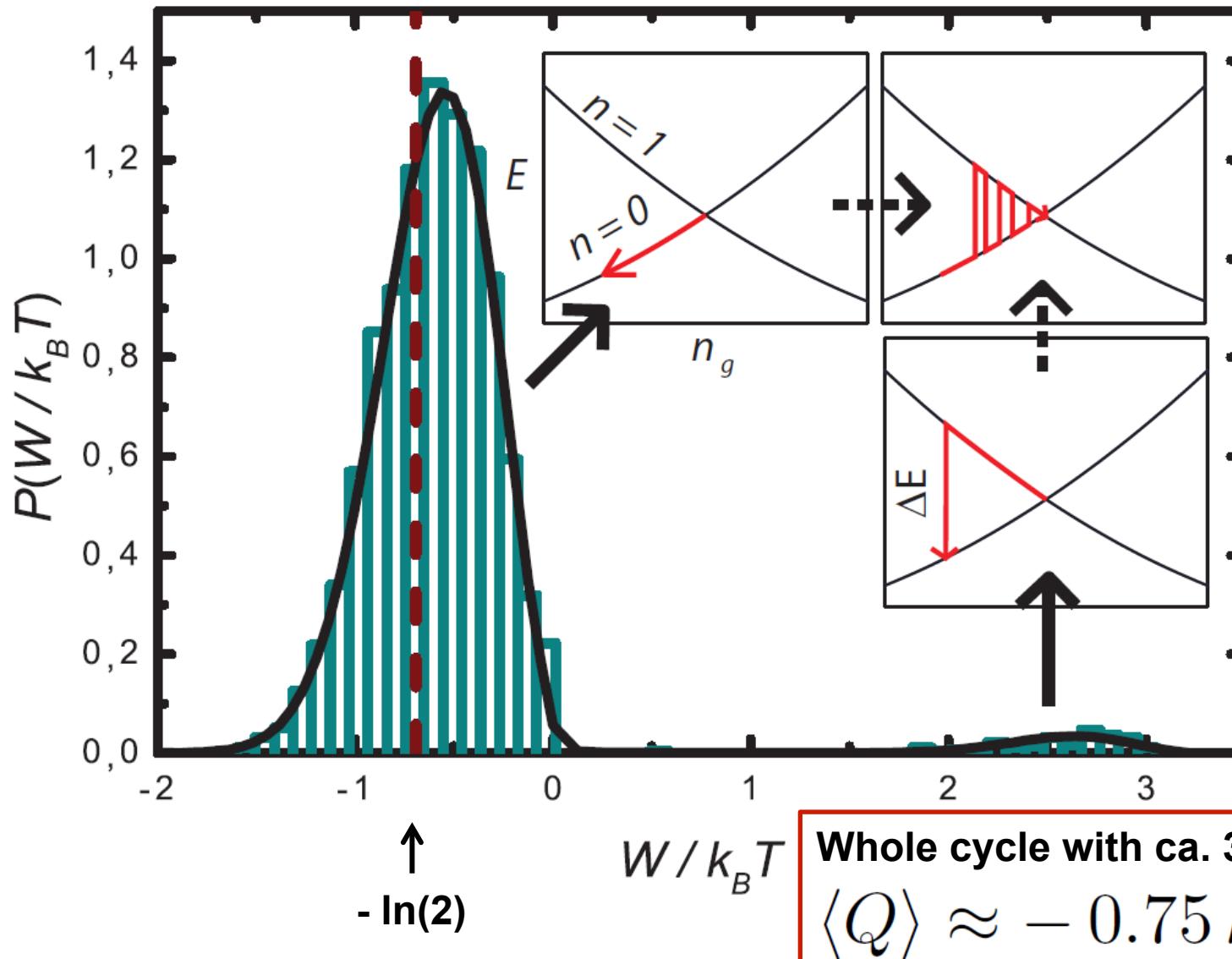
Corresponds to our experiment:



# Realization of the Maxwell's demon with an electron



# Measured distributions in the Szilard's engine



# Sagawa-Ueda relation

$$\langle e^{-(W - \Delta F)/k_B T - I} \rangle = 1$$

$$I(m, n) = \ln \left( \frac{P(n|m)}{P(n)} \right)$$

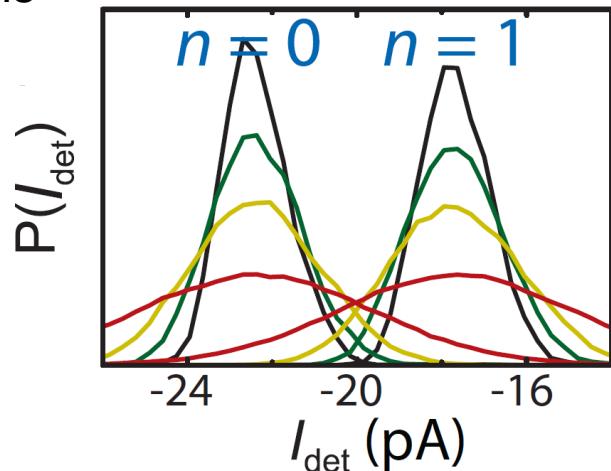
T. Sagawa and M. Ueda, PRL 104, 090602 (2010)

For a symmetric two-state system:

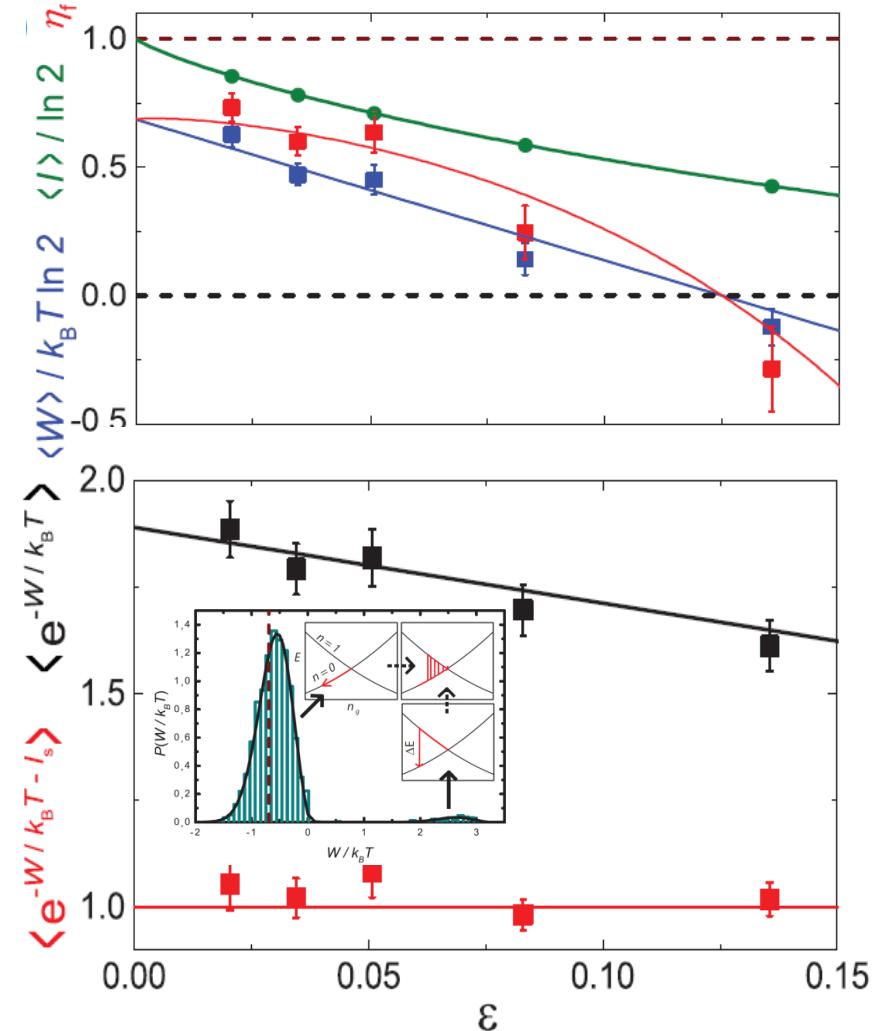
$$I(n = m) = \ln(2(1 - \epsilon))$$

$$I(n \neq m) = \ln(2\epsilon)$$

Measurements of  $n$  at different detector bandwidths

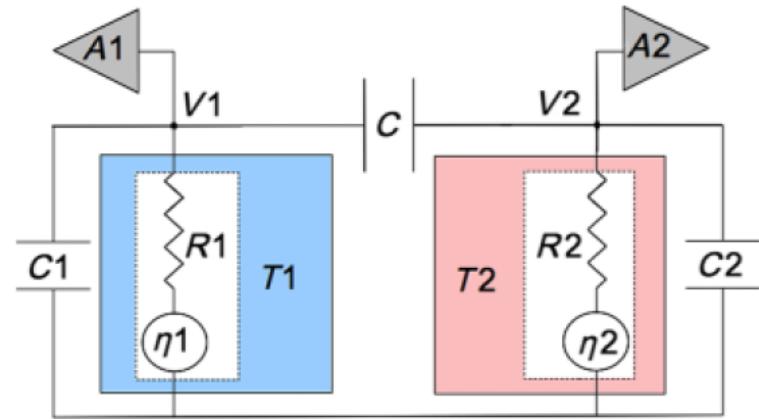
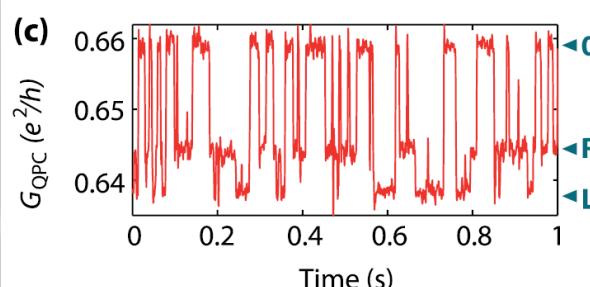
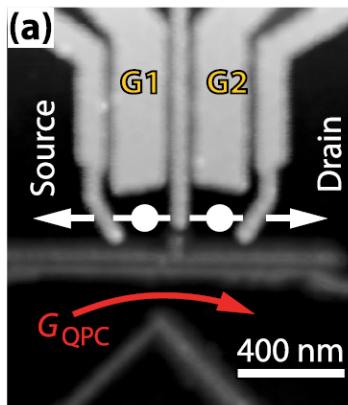


J. V. Koski et al., PRL 113, 030601 (2014)



# Work and heat in small systems: experimental situation

Typically an indirect measurement, hinging on understanding the system sufficiently well



$$Q = neV_{DS}$$

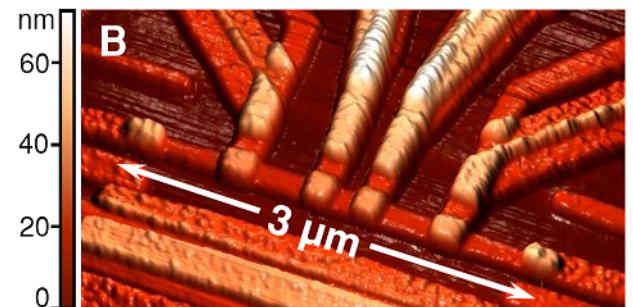
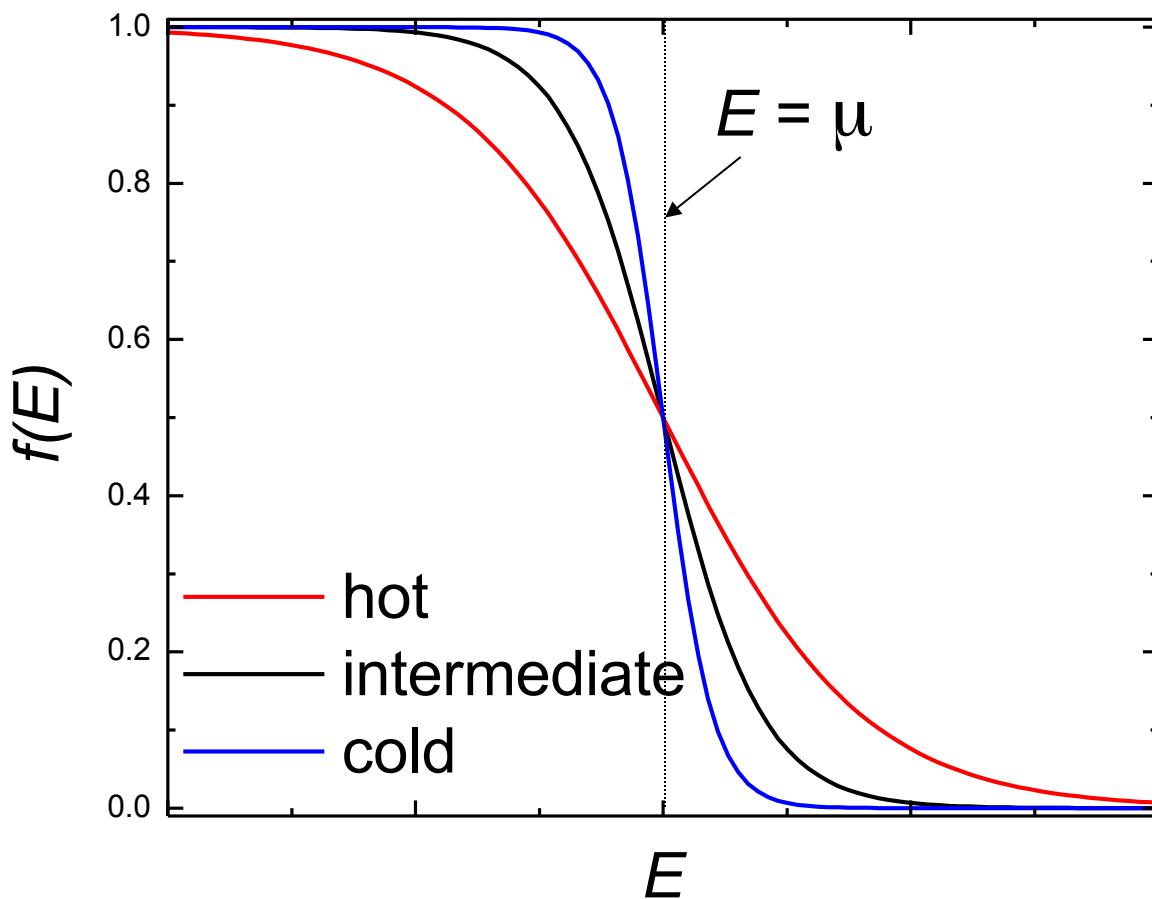
$$Q_{m,\tau} = \int_t^{t+\tau} i_m V_m dt$$

Y. Utsumi et al. PRB 81, 125331 (2010),  
B. Kung et al. PRX 2, 011001 (2012)

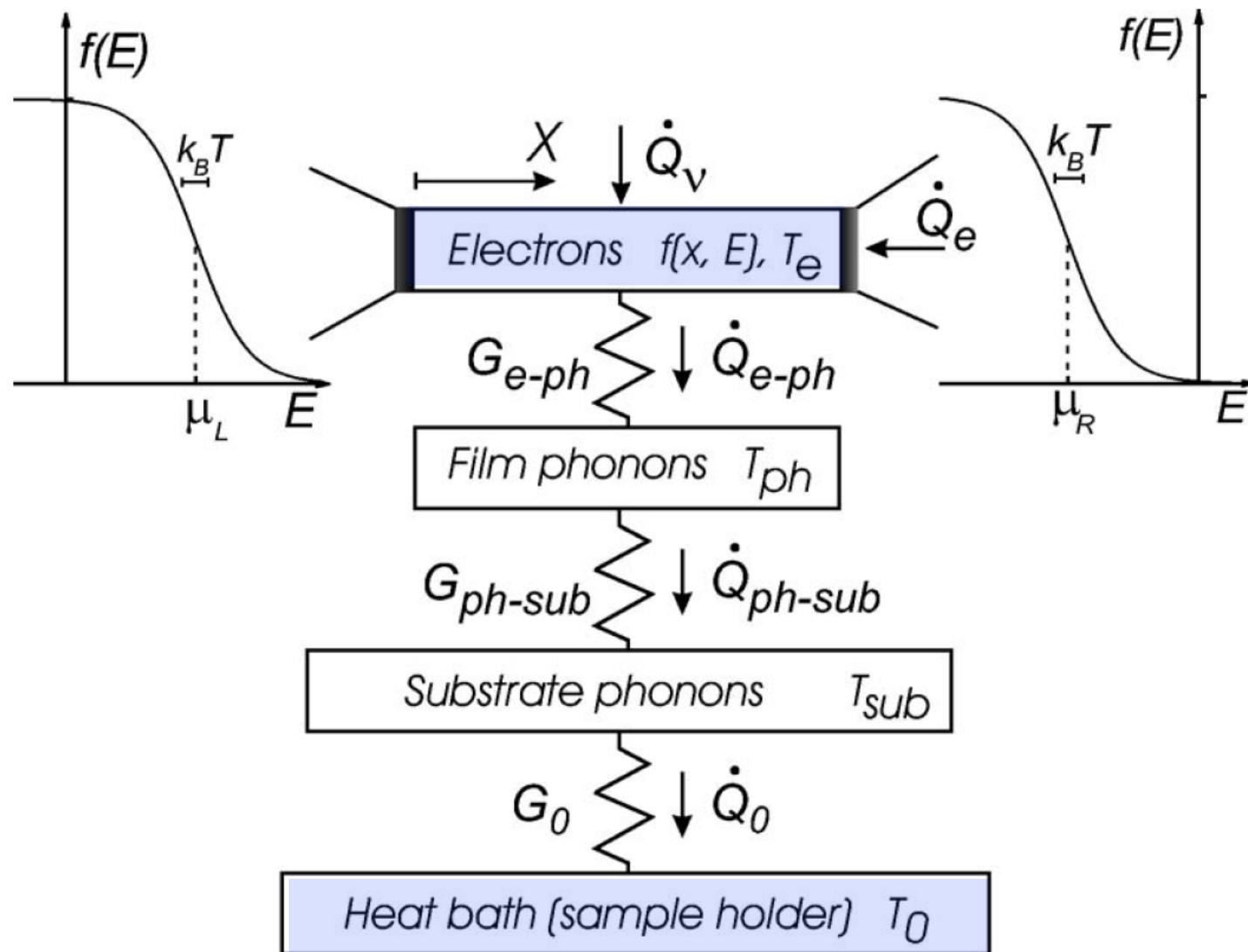
S. Ciliberto et al., PRL 110, 180601 (2013)

# Temperature in an electronic device

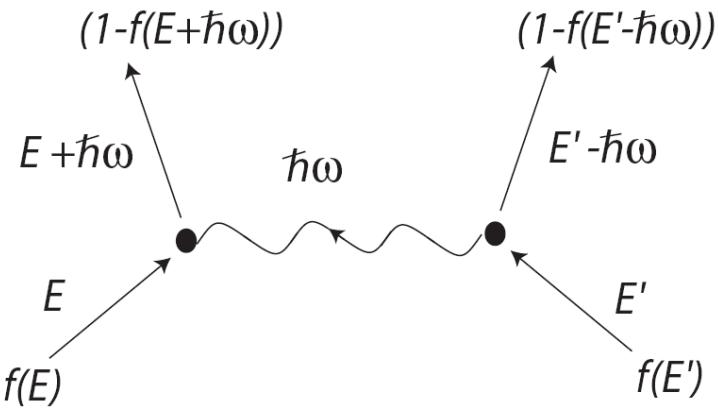
$$f(E) = \frac{1}{1 + e^{(E-\mu)/k_B T}}$$



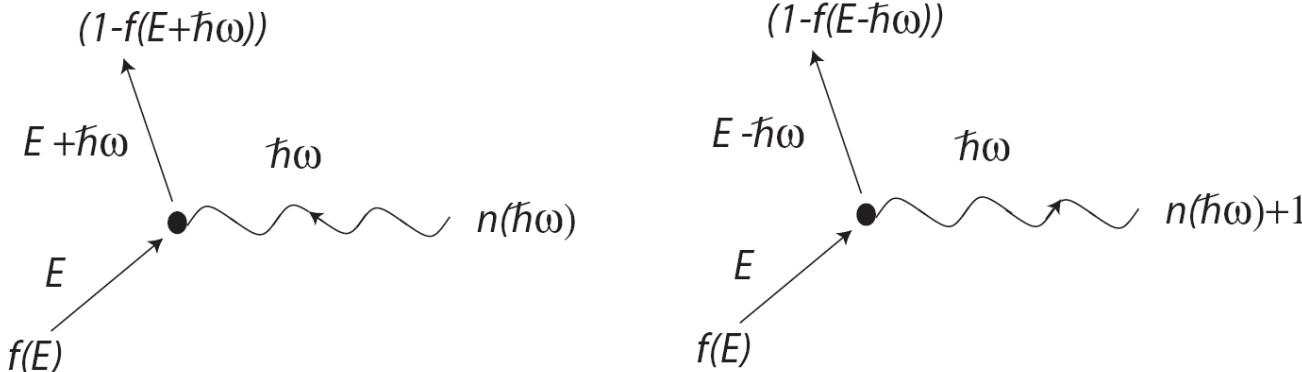
# Generic thermal model for an electronic conductor



# Electron-electron and electron-phonon relaxation



e-e relaxation drives  
the system towards  
*quasi-equilibrium*



e-p relaxation drives  
the system towards  
**equilibrium**

# The energy distribution of electrons in a small metal conductor

The distribution is determined by energy relaxation:

Equilibrium – Thermometer measures the temperature of the "bath"

Quasi-equilibrium – Thermometer measures the temperature of the electron system which can be different from that of the "bath"

Non-equilibrium – There is no well defined temperature measured by the "thermometer"

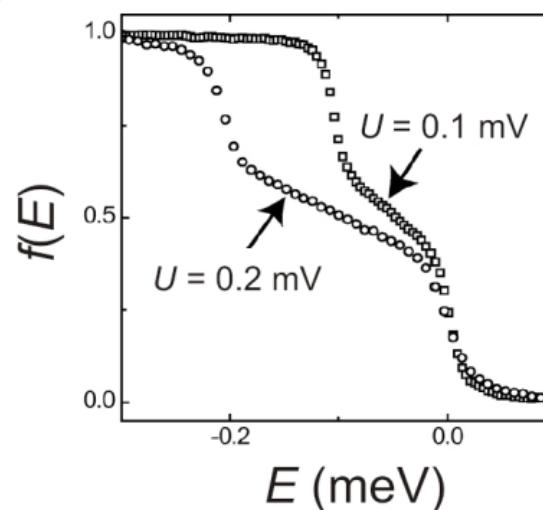
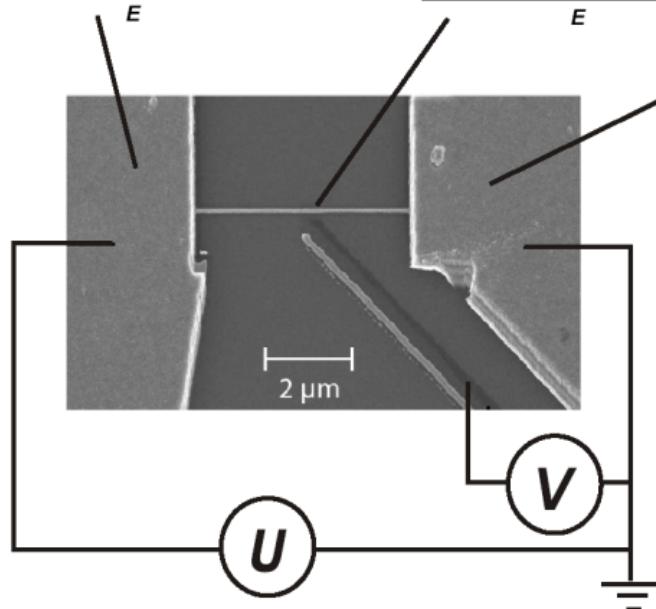
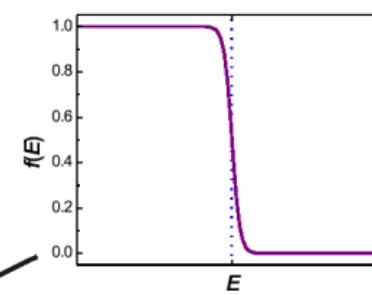
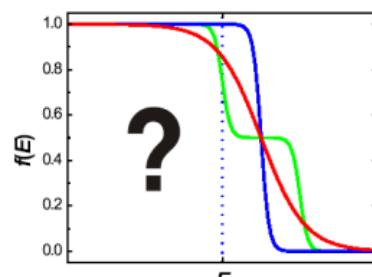
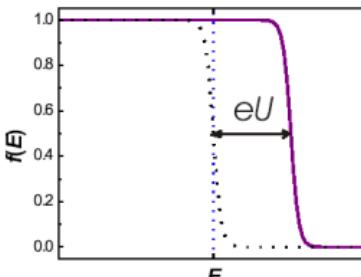


Illustration: diffusive normal metal wire  
H. Pothier et al. 1997

$$\begin{aligned}\tau_{ee} &= 1 \text{ ns} \\ \tau_{ep} &= 10 \mu\text{s}\end{aligned}$$

# Electron-phonon relaxation in metals at low $T$

PHYSICAL REVIEW B

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1 MARCH 1994-I

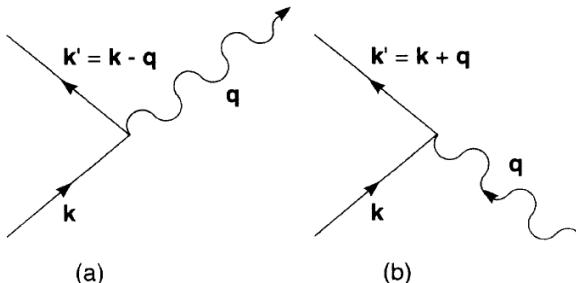
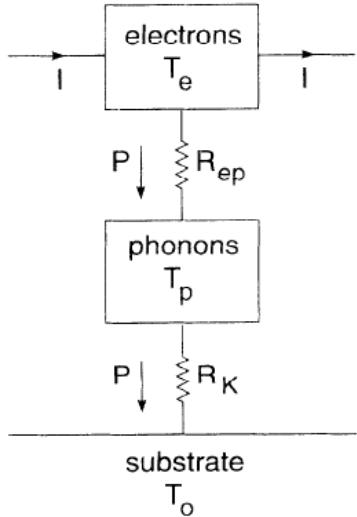
## Hot-electron effects in metals

F. C. Wellstood,\* C. Urbina,<sup>†</sup> and John Clarke

*Department of Physics, University of California, Berkeley, California 94720*

*and Materials Sciences Division, Lawrence Berkeley Laboratory, Berkeley, California 94720*

(Received 21 July 1993)

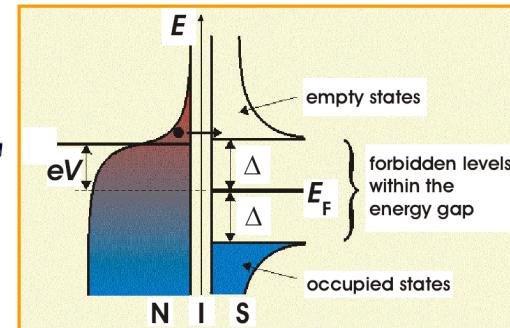


$$\dot{Q}_{ep} = \Sigma \Omega (T_e^5 - T_p^5)$$

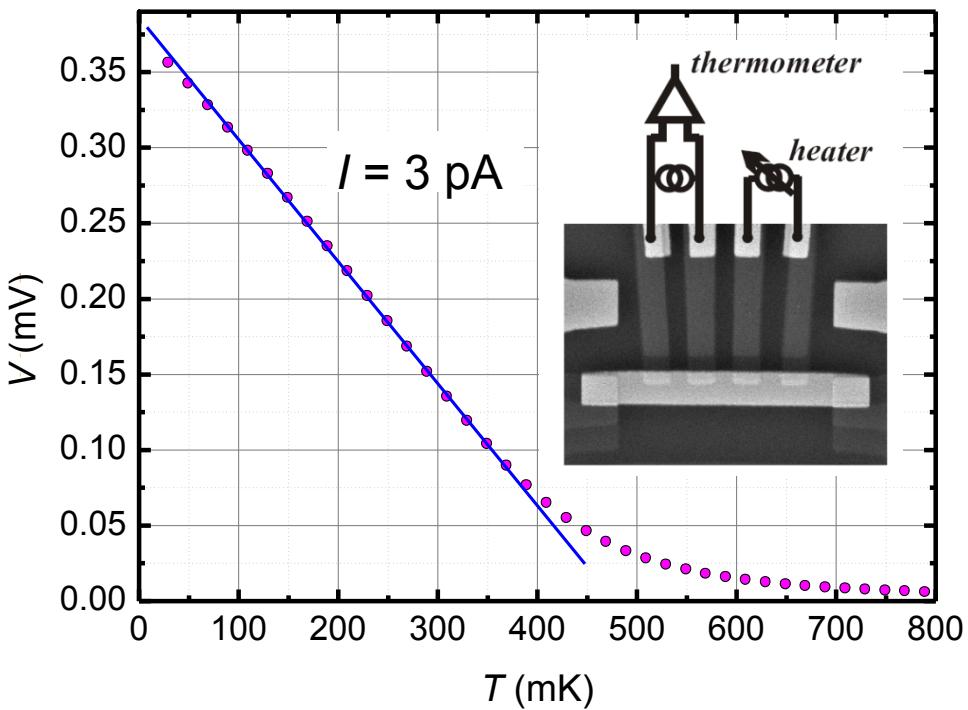
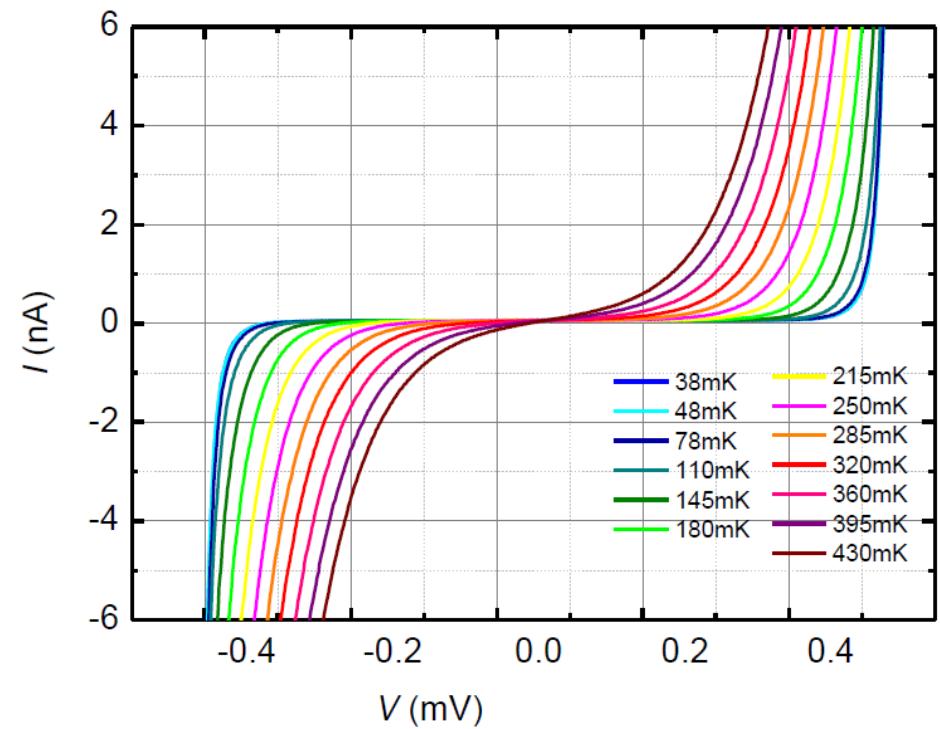
FIG. 2. Emission and absorption of phonons of wave vector  $q$  by an electron of wave vector  $k$ .

# NIS-thermometry

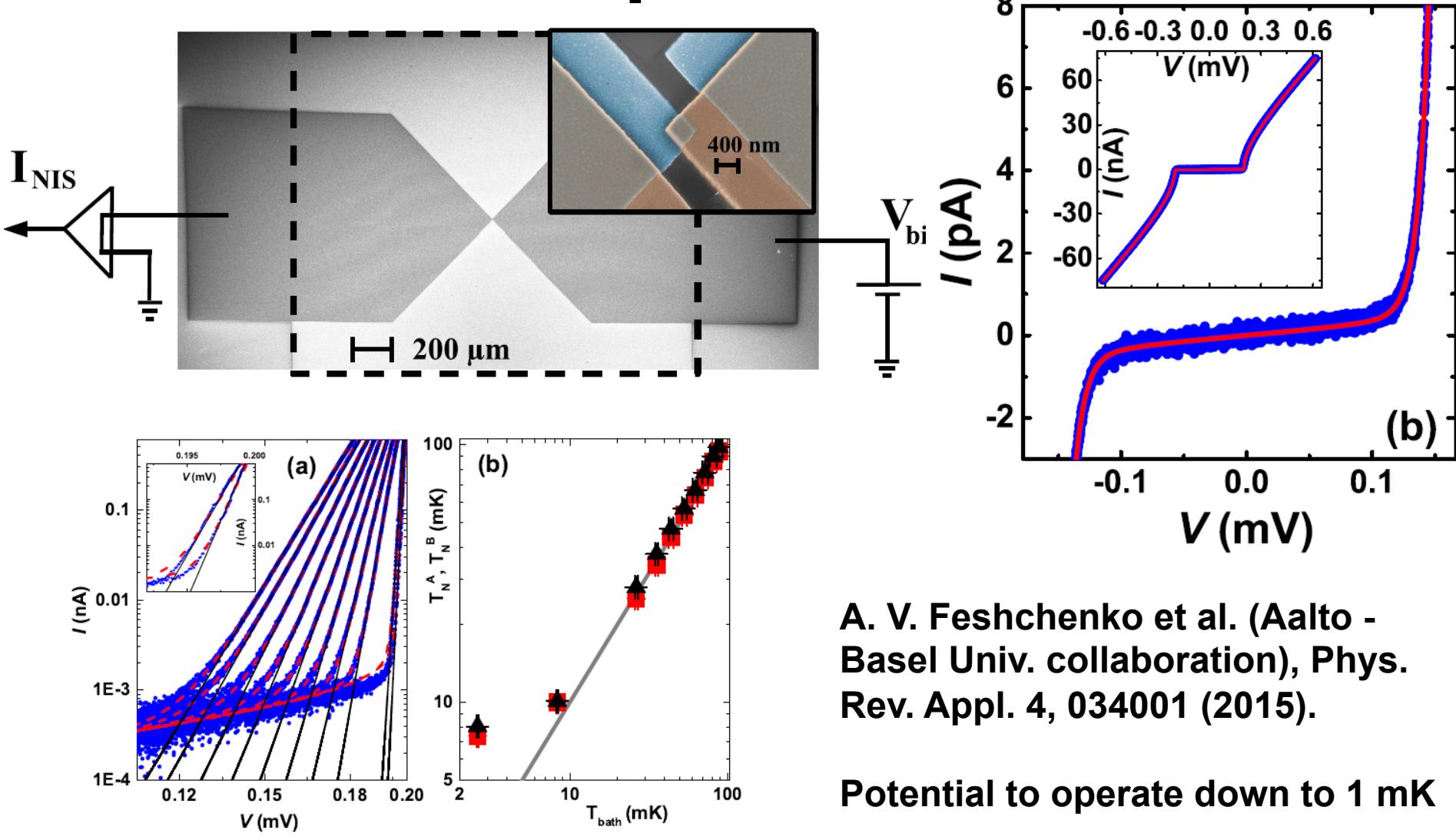
$$I = \frac{1}{2eR_T} \int n_S(E) [f_N(E - eV) - f_N(E + eV)] dE$$



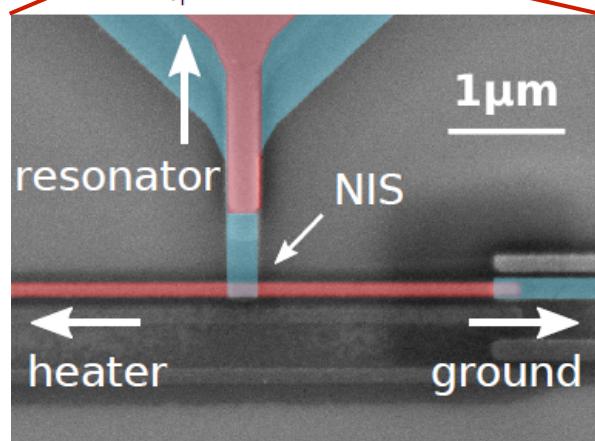
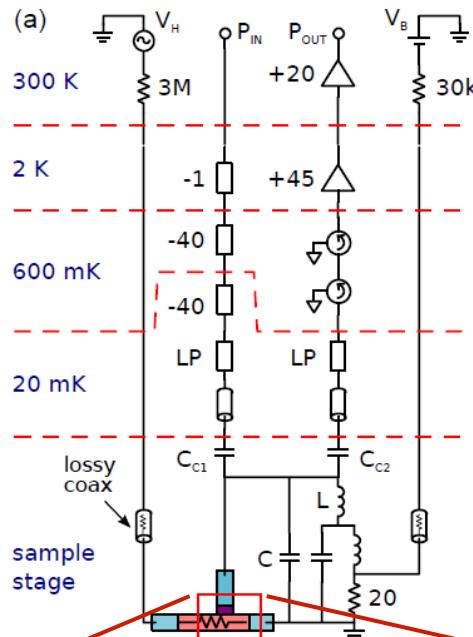
Probes electron temperature of N island (and not of S!)



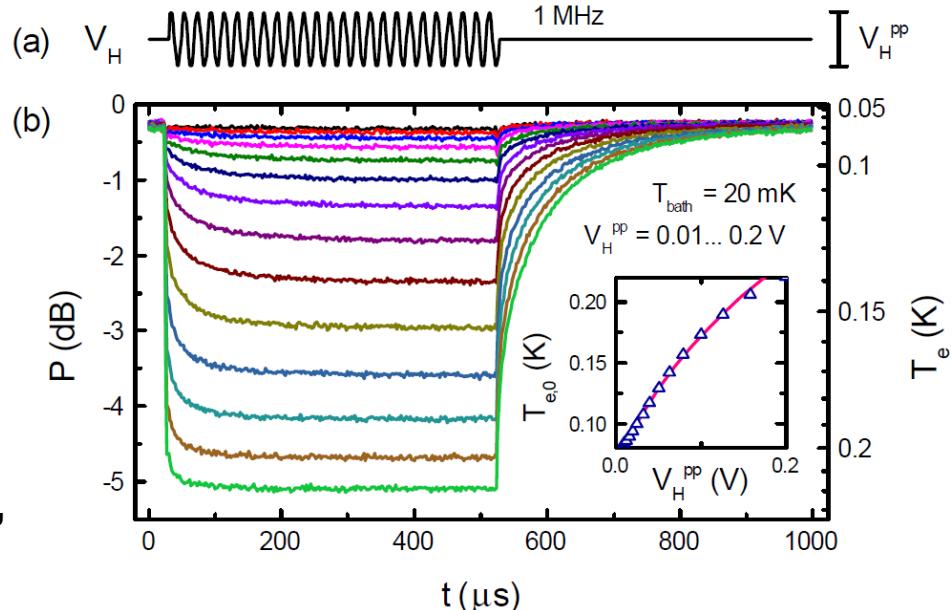
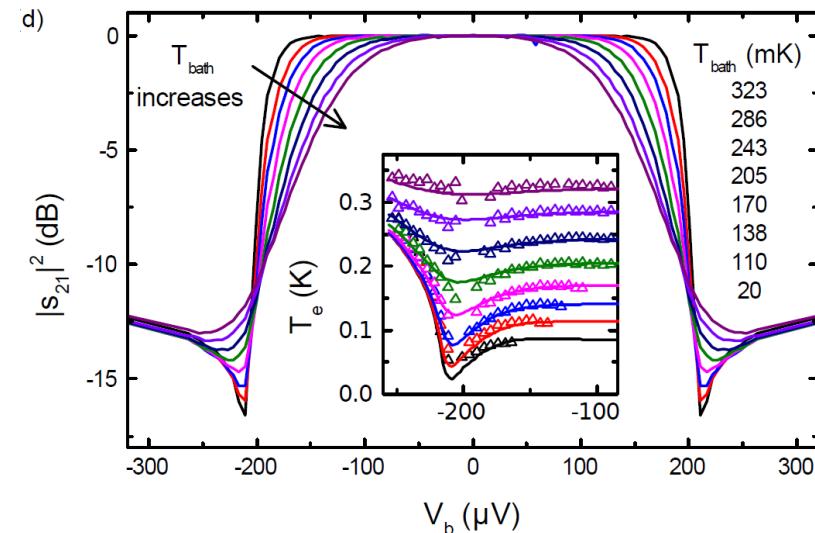
# NIS-thermometry at mK temperatures



# Fast thermometry



Transmission read-out at 600 MHz of a NIS junction

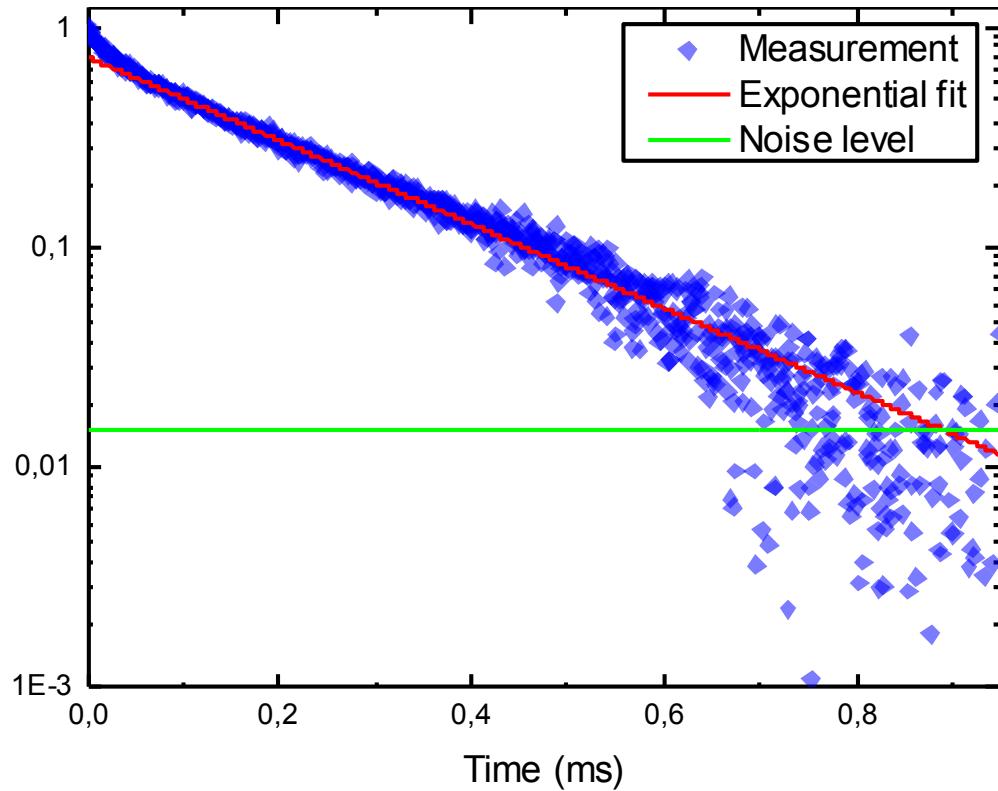


S. Gasparinetti et al., Phys. Rev. Applied 3, 014007 (2015); K. L. Viisanen et al., New J. Phys. 17, 055014 (2015).

# Fast thermometry

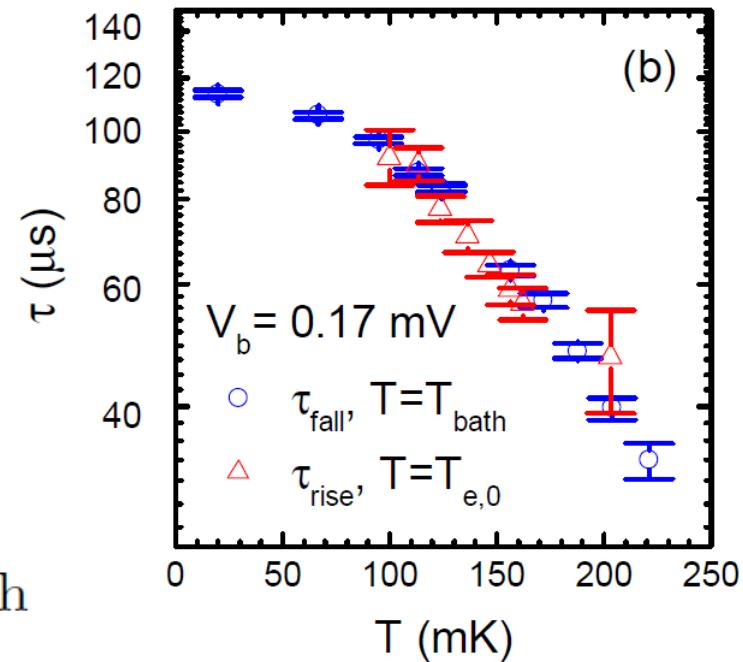
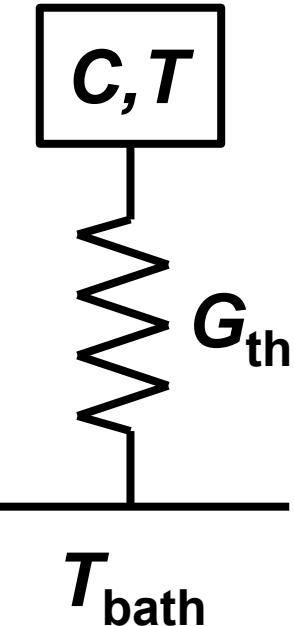
## Time-resolved measurements

Relaxation



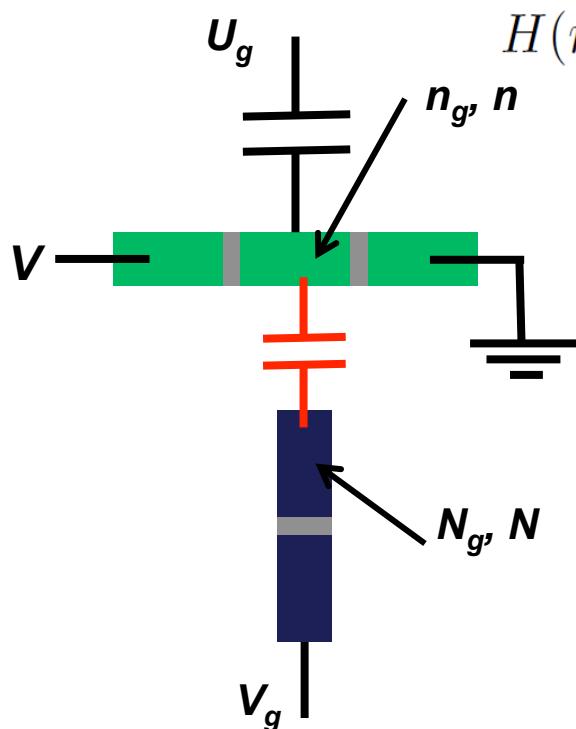
$$\mathcal{C} \frac{d\delta T}{dt} = -G_{\text{th}} \delta T$$

$$\tau = \mathcal{C}/G_{\text{th}}$$

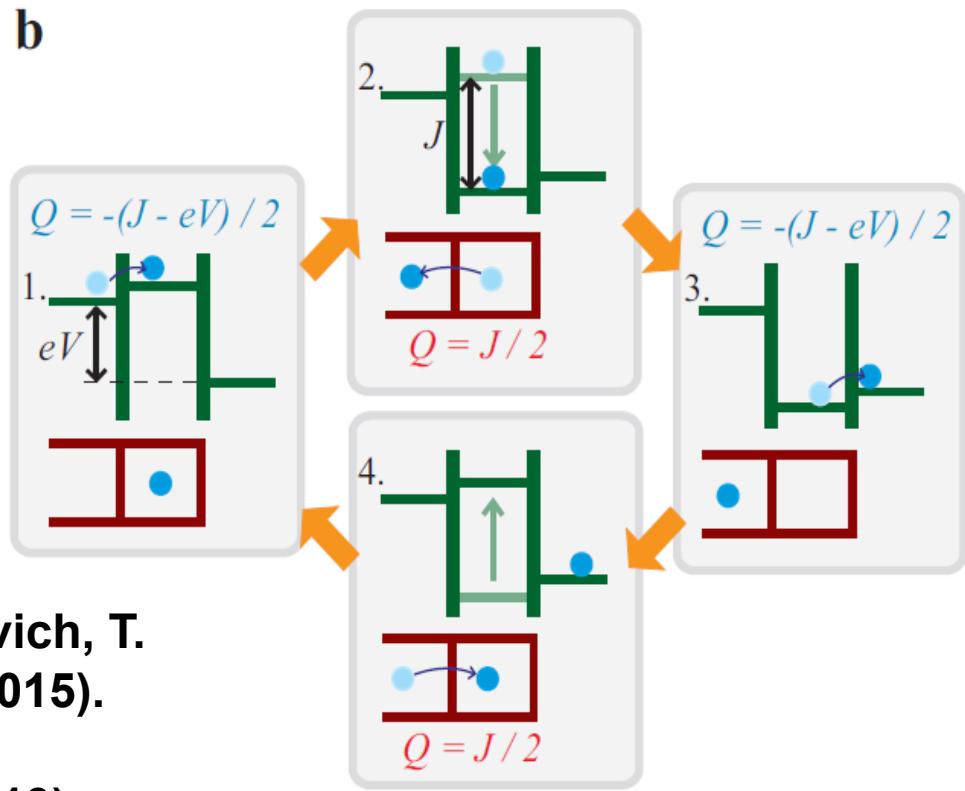


# Autonomous Maxwell's demon

System and Demon: all in one  
Realization in a circuit:



$$H(n, N) = E_s(n-n_g)^2 + E_d(N-N_g)^2 + 2J(n-n_g)(N-N_g)$$

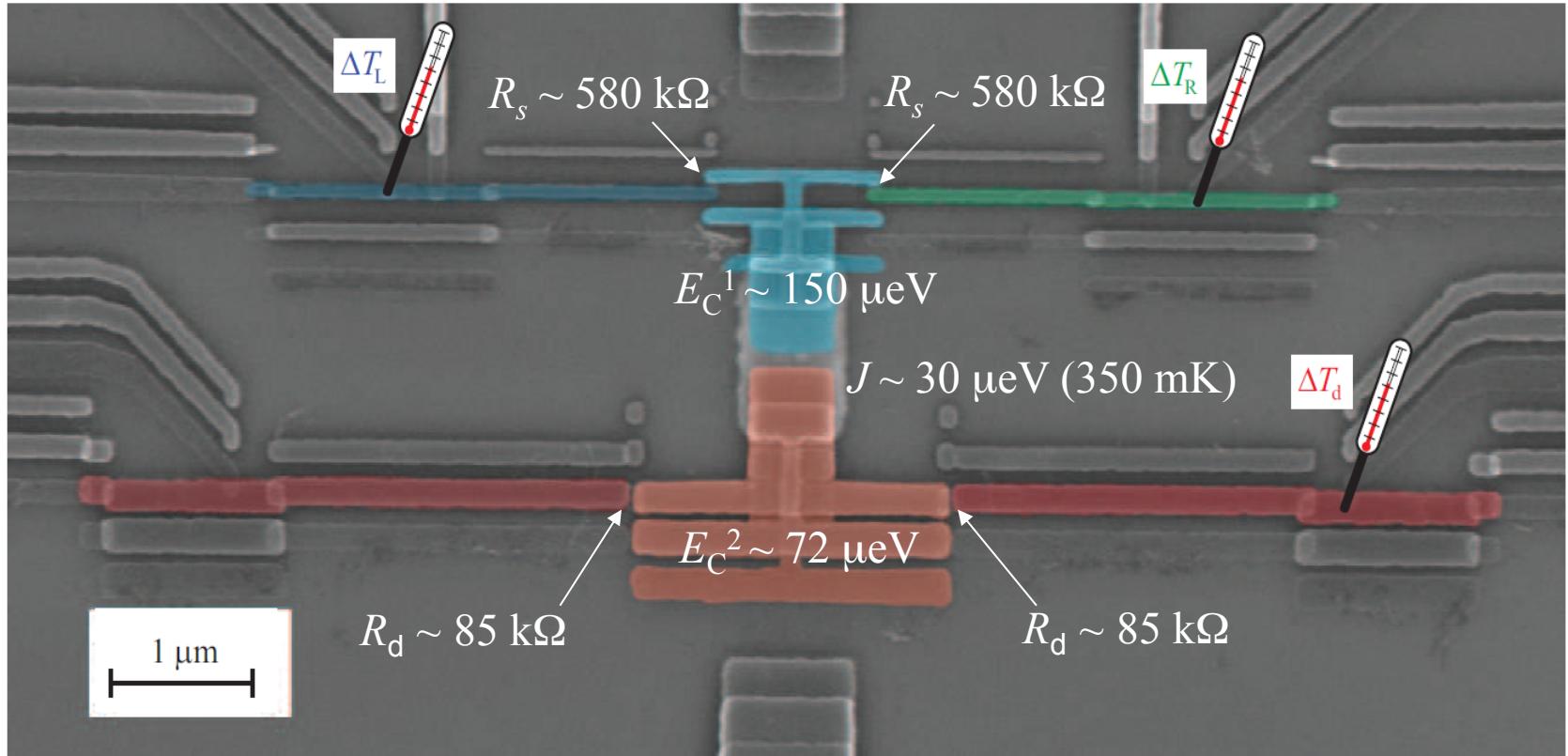


J. V. Koski, A. Kutvonen, I. M. Khaymovich, T. Ala-Nissila, and JP, PRL 115, 260602 (2015).

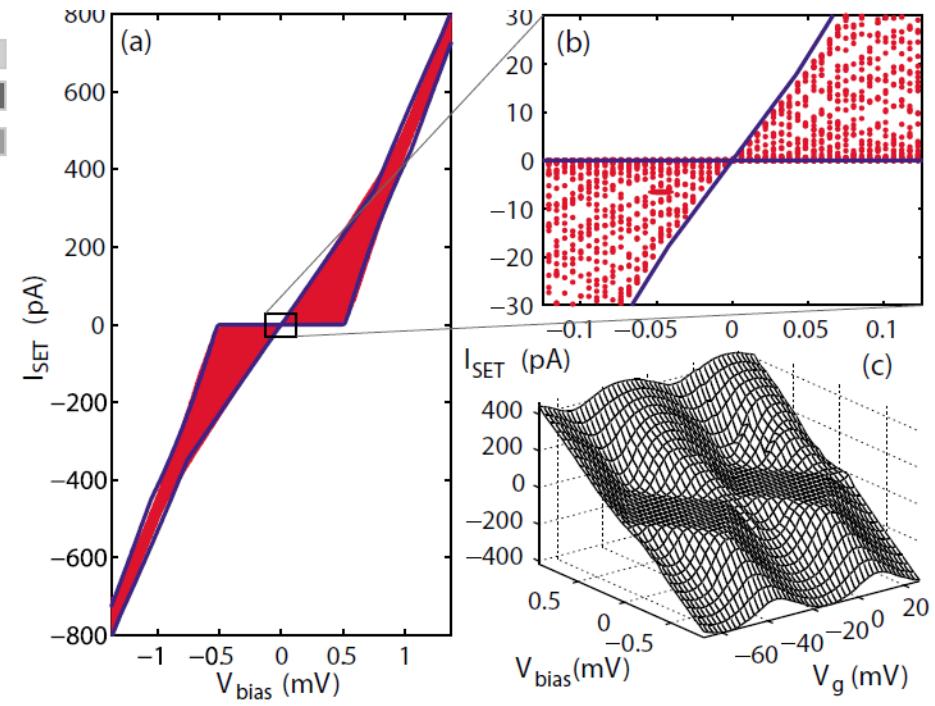
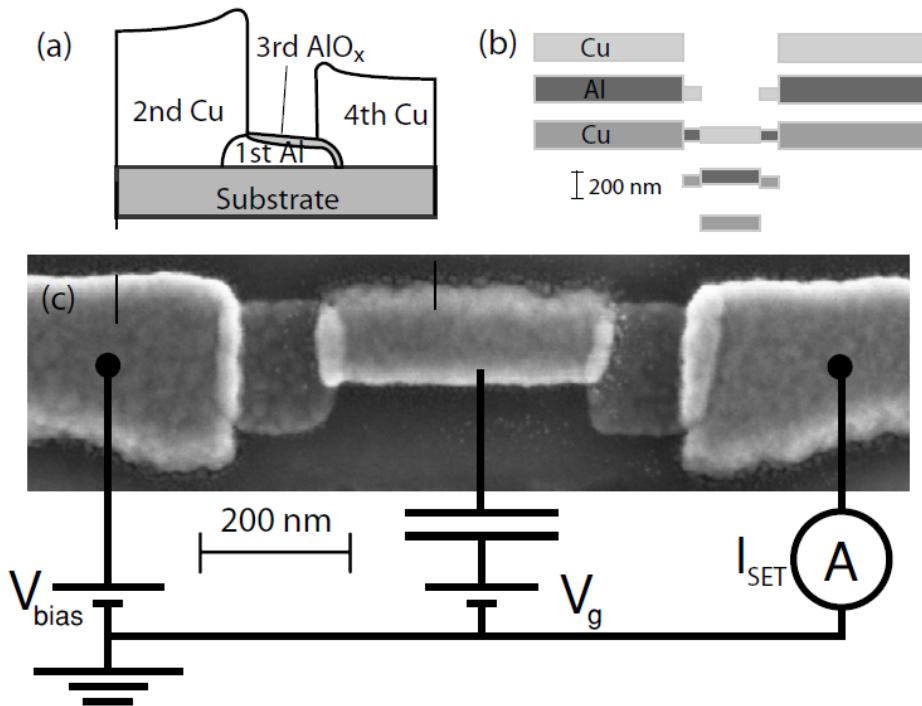
P. Strasberg et al., PRL 110, 040601 (2013).

# Autonomous Maxwell's demon – information-powered refrigerator

Image of the actual device

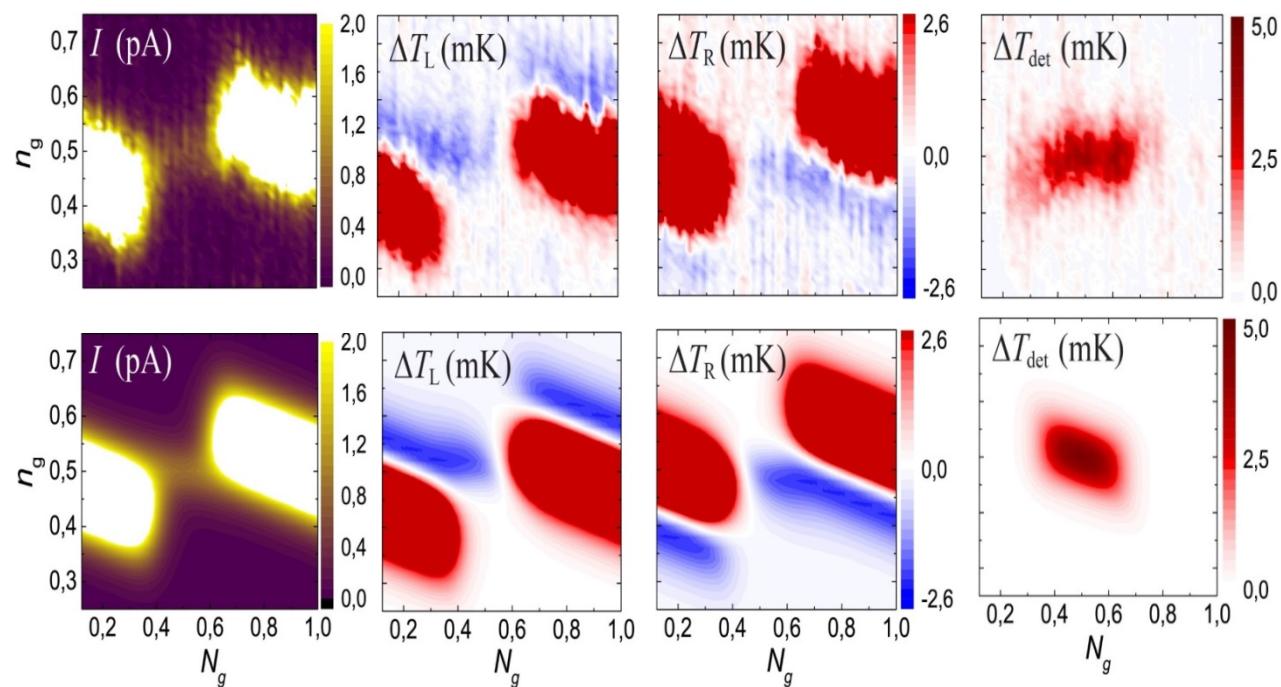
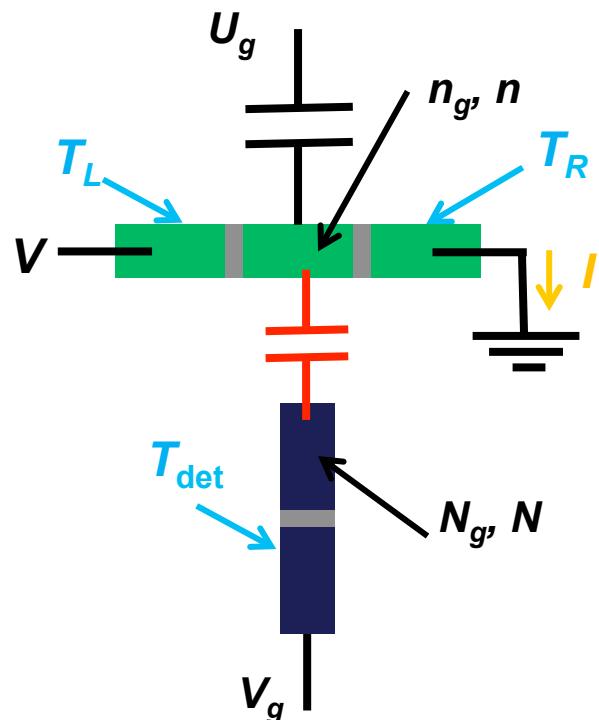


# Technique to produce fully normal tunnel junctions and SETs



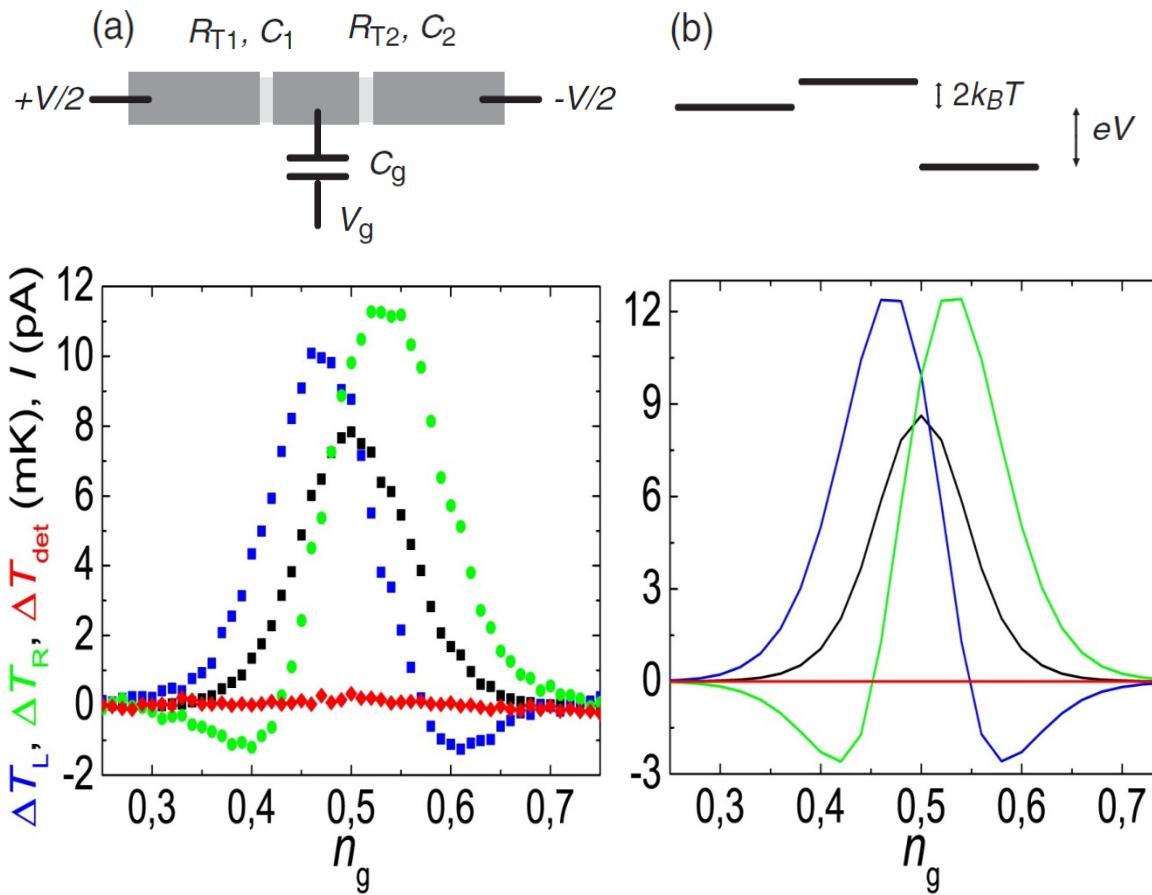
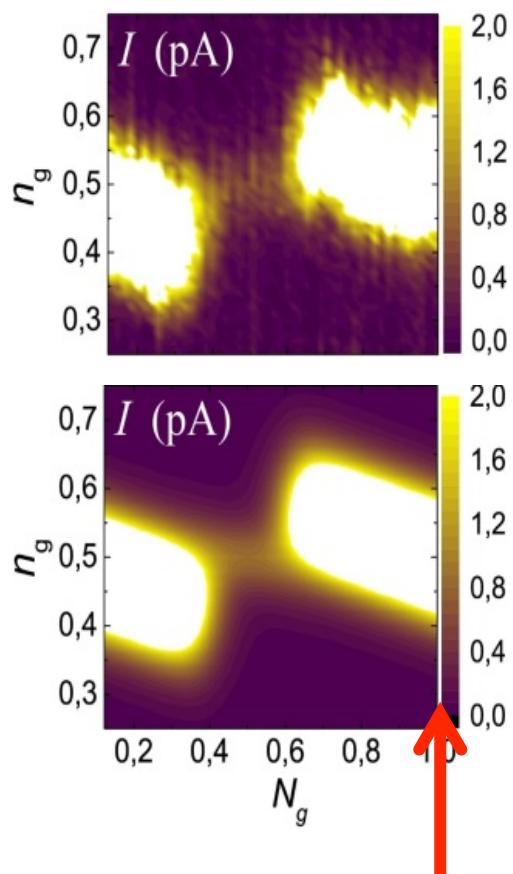
Laterally proximized tunnel junctions:  
J. Koski et al., Appl. Phys. Lett. **98**, 203501 (2011).

# Current and temperatures at different gate positions



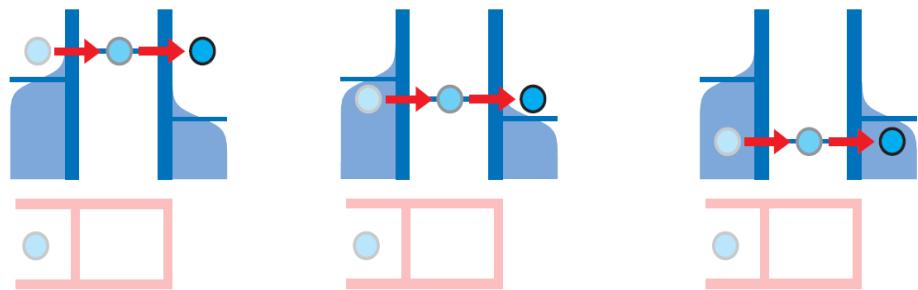
$V = 20 \mu\text{V}$ ,  $T = 50 \text{ mK}$

# $N_g = 1$ : No feedback control ("SET-cooler")

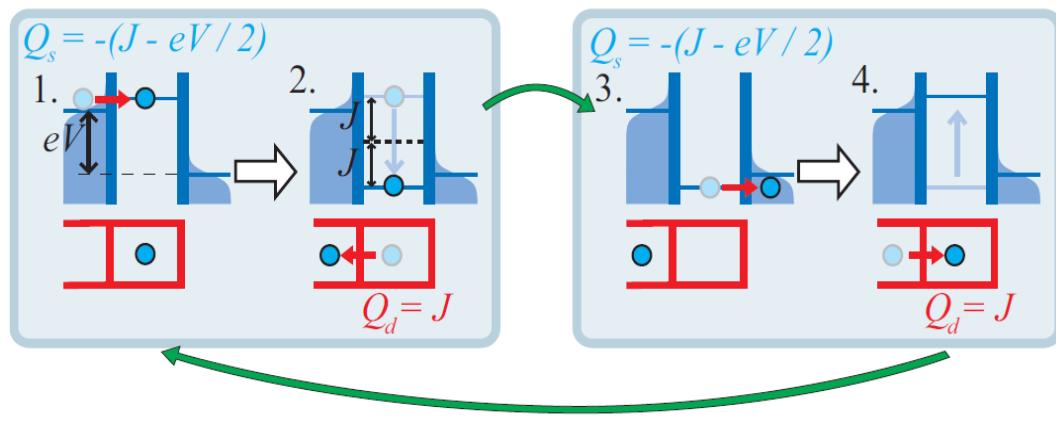
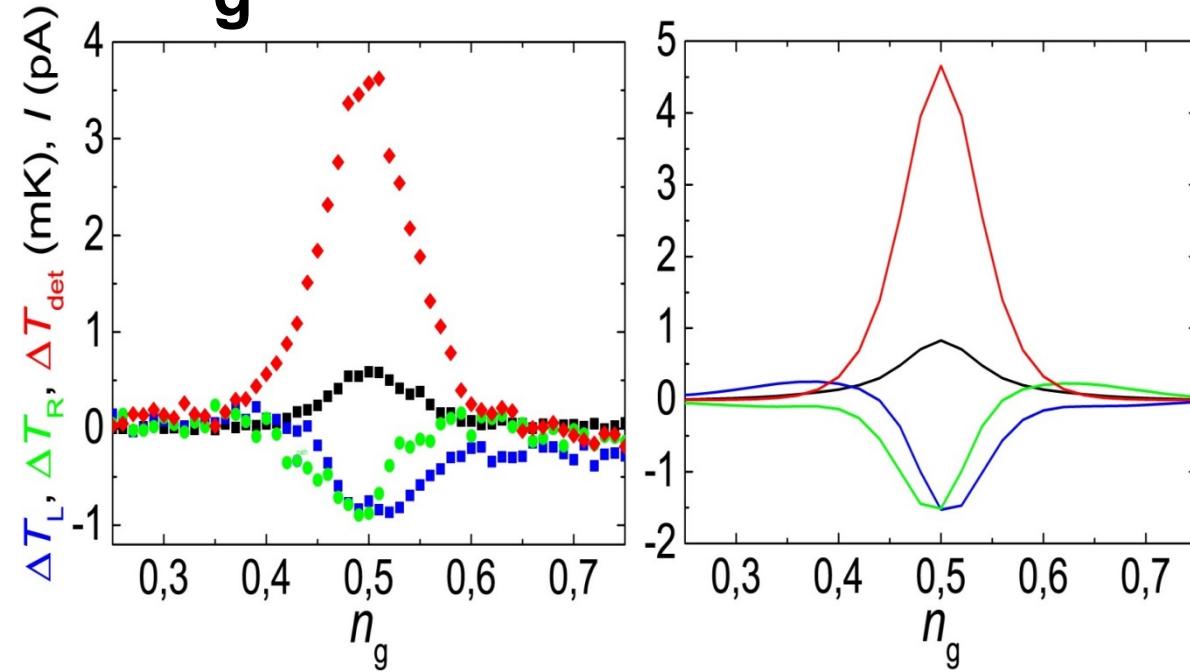


JP, J. V. Koski, and D. V. Averin, PRB **89**, 081309 (2014)

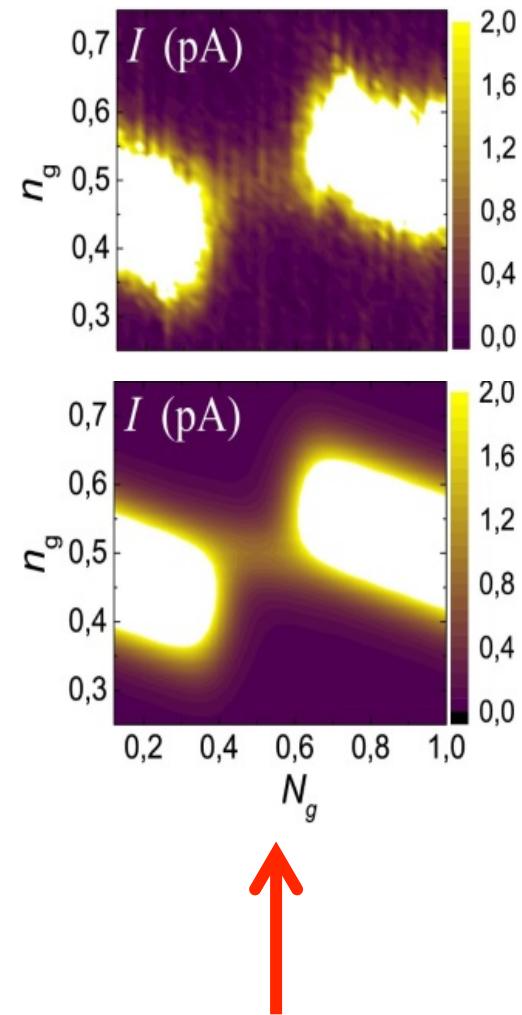
A. V. Feshchenko, J. V. Koski, and JP, PRB **90**, 201407(R) (2014)



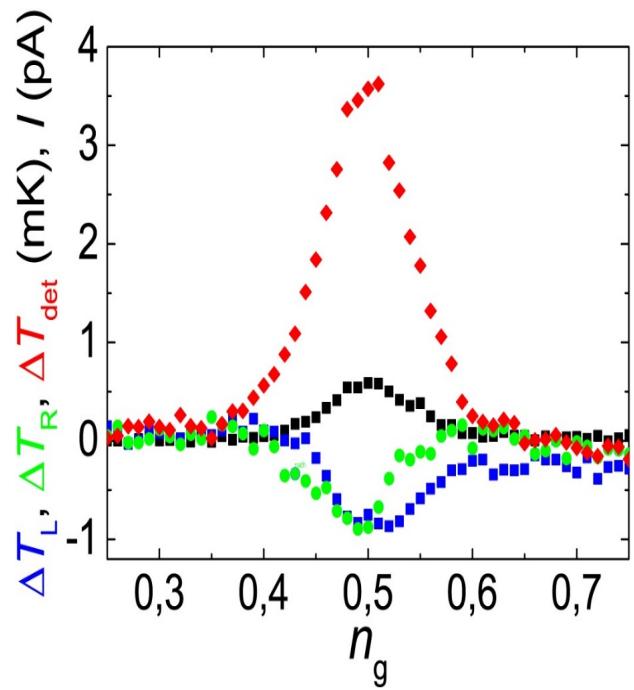
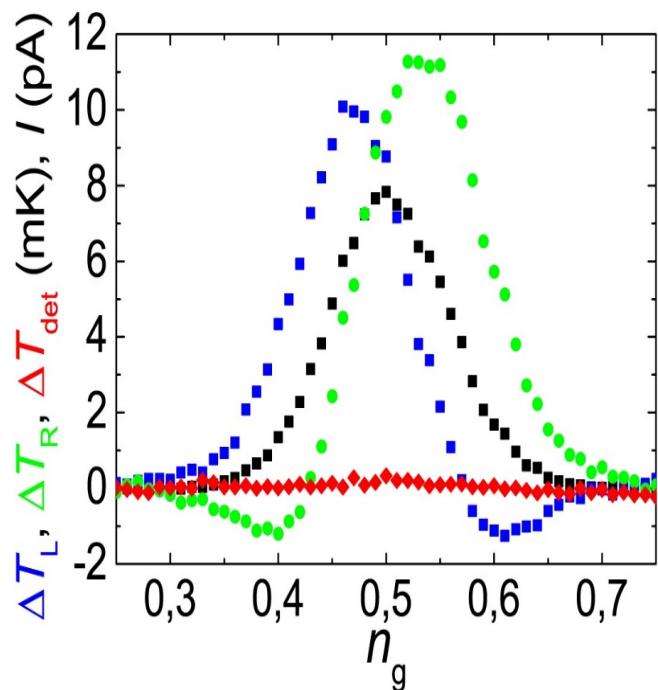
# $N_g = 0.5$ : feedback control (Demon)



Both  $T_L$  and  $T_R$  drop: entropy of the System decreases;  
 $T_{\text{det}}$  increases: entropy of the Demon increases



# Summary of the autonomous SET cooler demon experiment



current  $I$

